

Reliability-based Calibration of Design Code for Concrete Structures (ACI 318)

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ACI 318 Code

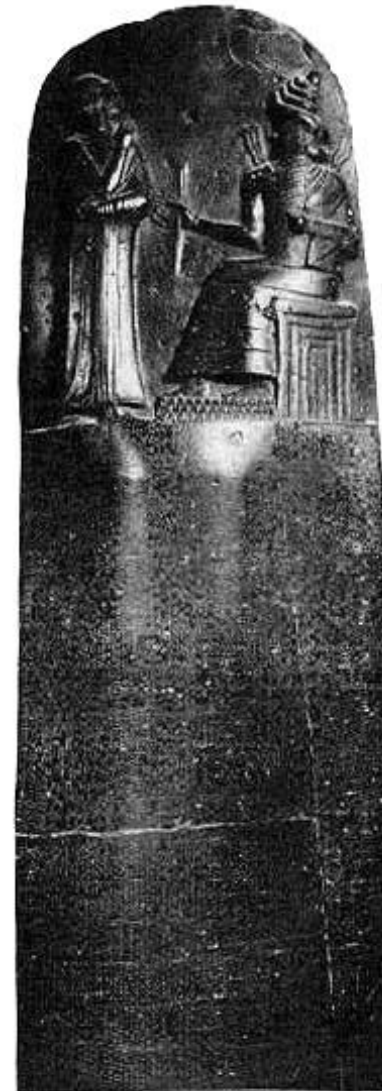
Outline

- Objectives
- New material test data
- Resistance parameters
- Reliability analysis
- Resistance factors
- Further developments

DESIGN CODES HISTORICAL PERSPECTIVE



- A. If a builder build a house for a man and do not make its construction firm and the house which he has built collapse and cause the death of the owner of the house - that builder shall be put to death.
- B. If it cause the death of the son of the owner of the house - they shall put to death a son of that builder.
- C. If it cause the death of a slave of the owner of the house - he shall give to the owner of the house a slave of equal value.
- D. If it destroy properly, he shall restore whatever it destroyed, and because he did not make the house which he built firm and it collapsed, he shall rebuild the house which collapsed at his own expense.
- E. If a builder build a house for a man and do not make its construction meet the requirements and a wall fall in, that builder shall strengthen the wall at his own expense.



ACI 318 Code

- The basic document for design of concrete (R/C and P/C) buildings in USA
- ACI 318 specifies resistance factors and design resistance
- ACI 318 specifies load factors
- ACI 318 does not specify design load, reference is made to other codes

ACI 318-99
ACI 318R-99

**Building Code Requirements for
Structural Concrete (318-99)
and Commentary (318R-99)**

Reported by ACI Committee 318



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Why Calibration of ACI 318?

- Current load factors were adopted in 1950's
- Introduction of the new code with loads and load factors, ASCE 7 (American Society of Civil Engineers)
- Load factors specified in ASCE 7 are already adopted for steel design (AISC) and wood (NDS)
- Problems with mixed structures (steel and concrete)

Minimum Design Loads for Buildings and Other Structures

This document uses both the
International System of Units (SI)
and customary units

Load factors specified by ACI 318 and ASCE 7

The design formula
specified
by ACI 318-99 Code

$$1.4 D + 1.7 L < \phi R$$

$$0.75 (1.4 D + 1.7 L + 1.7 W) < \phi R$$

$$0.9 D + 1.3 W < \phi R$$

$$0.75 (1.4 D + 1.7 L + 1.87 E) < \phi R$$

The design formula specified
by ASCE-7 Standard

$$1.4 D < \phi R$$

$$1.2 D + 1.6 L < \phi R$$

$$1.2 D + 1.6 L + 0.5 S < \phi R$$

$$1.2 D + 0.5 L + 1.6 S < \phi R$$

$$1.2 D + 1.6 W + 0.5 L + 0.5 S < \phi R$$

$$1.2 D + 1.0 E + 0.5 L + 0.2 S < \phi R$$

$$0.9 D - (1.6 W \text{ or } 1.0 E) < \phi R$$



Objectives of Calibration of ACI 318

- Determine resistance factors, ϕ , corresponding to the new load factors (ASCE 7)
- Reliability of the designed structures cannot be less the predetermined minimum level
- Maintain a competitive position of concrete structures
- If needed, identify the need for changes of load factors in the ASCE 7

Code Calibration Procedure

- Selection of representative structural types and materials
- Formulate limit state functions, identify load and resistance parameters
- Develop statistical models for load and resistance parameters
- Develop the reliability analysis procedure
- Select the target reliability level(s)
- Determine load and resistance factors

Considered Structural Components

- Beams (reinforced concrete, prestressed concrete)
- Slabs (reinforced concrete, prestressed concrete)
- Columns (reinforced concrete, prestressed concrete, tied and spiral, axial and eccentric)
- Plain concrete

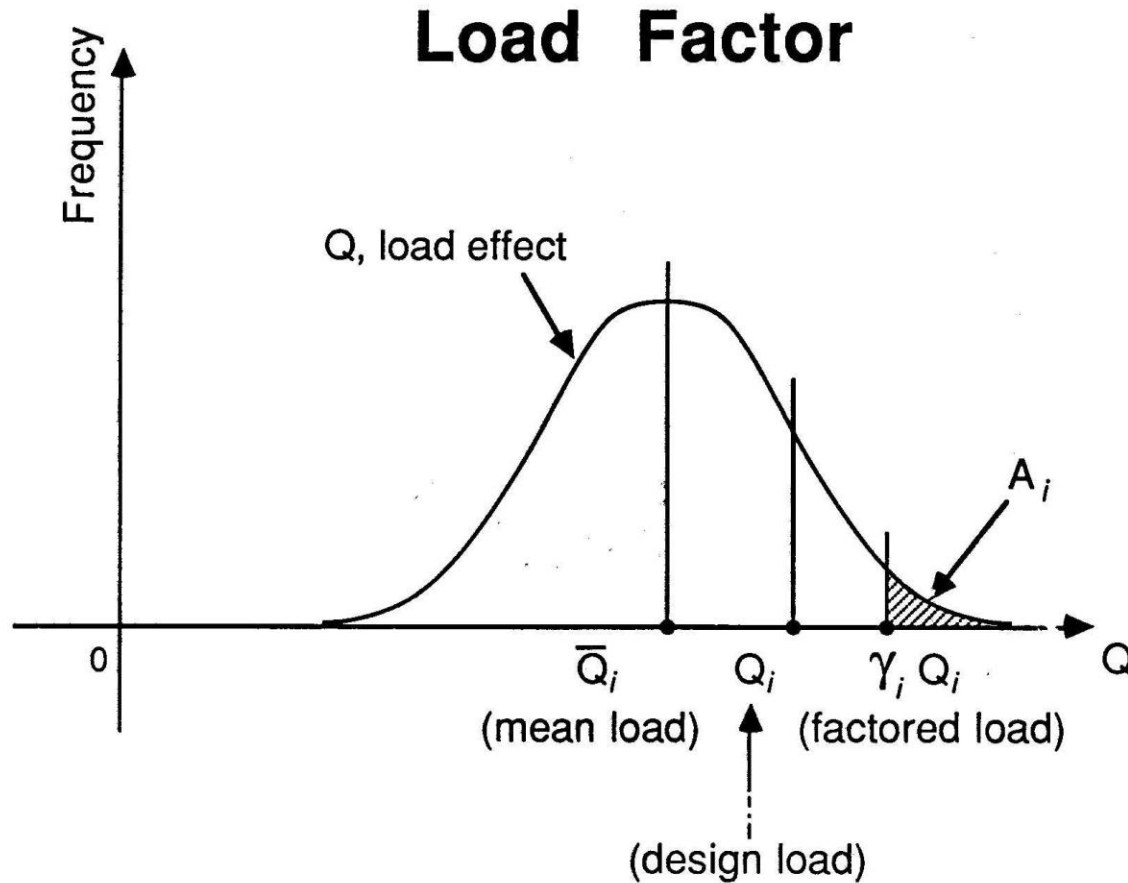
Considered Load Components

- D = dead load
- L = live load
- S = snow
- W = wind
- E = earthquake
- Load combinations

Assumed Statistical Data

- Dead load
 $\lambda = 1.03-1.05, V = 0.08-0.10$
- Live load
 $\lambda = 1.00, V = 0.20$
- Wind
 $\lambda = 0.80, V = 0.35$
- Snow
 $\lambda = 0.80, V = 0.25$
- Earthquake
 $\lambda = 0.65, V = 0.55$

Load Factor



Considered Materials

- Concrete (cast-in-place and precast)
 - Ordinary concrete
 - Light weight concrete
 - High strength concrete ($f'_c \geq 45$ MPa)
- Reinforcing steel bars
- Prestressing steel strands

Considered Cases

- Old
 - Statistical data for materials from 1970's
 - Design according to ACI 318-99
- New
 - Statistical data for materials from 2001-05
 - Design according to proposed ACI 318

Objectives

- Update the materials strength models using new statistical data
- Update the resistance models for reliability analysis
- Calculate reliability indices for components designed using ACI 318-12
- Provide a basis for selection of resistance factors

Parameters of Resistance

- Material : uncertainty in the strength of material, modulus of elasticity, cracking stresses, and chemical composition.
- Fabrication : uncertainty in the overall dimensions of the component which can affect the cross-section area, moment of inertia, and section modulus.
- Analysis : uncertainty resulting from approximate methods of analysis and idealized stress/strain distribution models.

Parameters of Resistance

$$R = R_n M F P$$

where :

R_n = nominal value of resistance

M = material factor

F = fabrication factor

P = professional factor

Parameters of Resistance

- The mean value of R is

$$\mu_R = R_n \mu_M \mu_F \mu_P$$

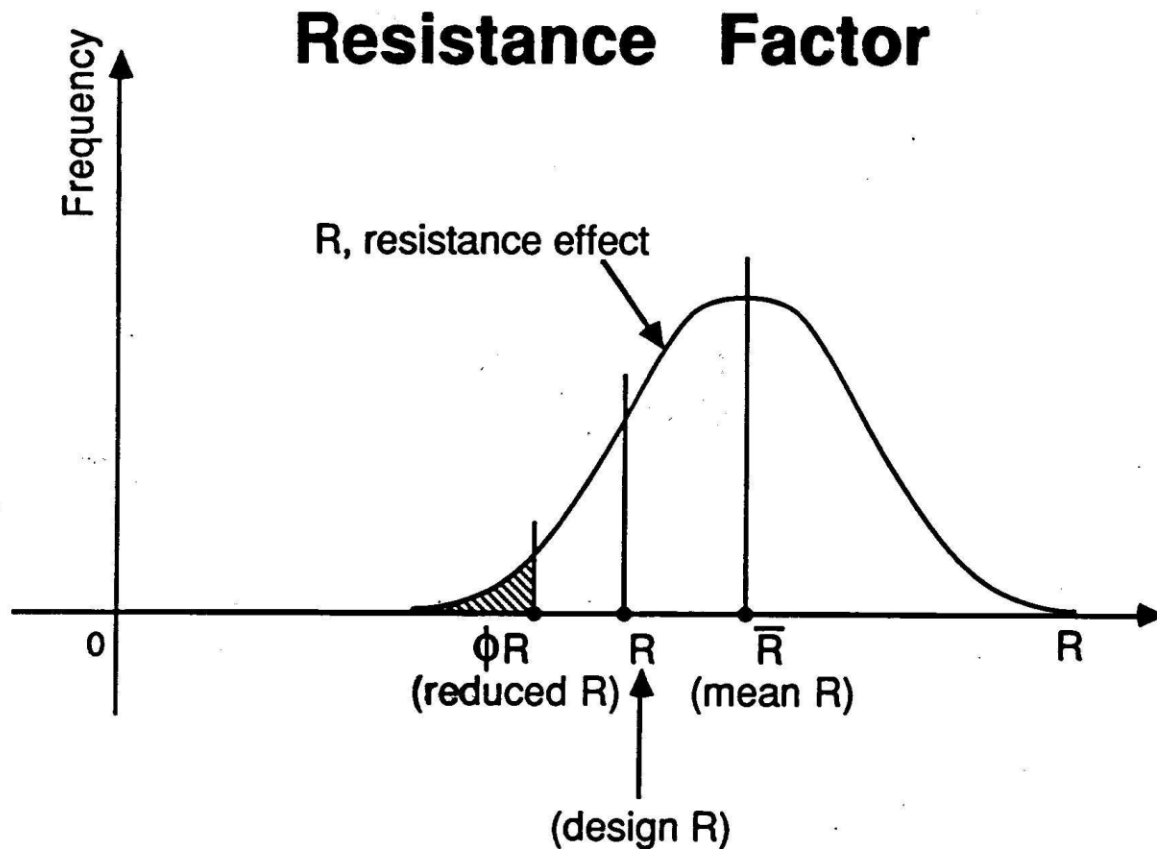
- Coefficient of variation

$$V_R = \sqrt{(V_M)^2 + (V_F)^2 + (V_P)^2}$$

- Bias factor

$$\lambda_R = \lambda_M \lambda_F \lambda_P$$

Resistance Factor



ϕ is calibrated to get $\beta = \beta_T$

Material Factor

- Available data-base from 1970's (MacGregor)
- Concrete industry provided test results (2000-2001 and 2003), gathered for this calibration
- Code Calibration of ACI 318 (2005) is based on these recent test results

Concrete Strength

- Compressive strength - cylinders 6 x 12 in (150 x 300 mm)
- Mostly 28 day strength, for precast concrete also 56 day strength





MAX PLATEN

Results of Material Tests

- Cumulative distribution functions (CDF)
- For an easier interpretation of the results, CDF's are plotted on the normal probability paper
- CDF of a normal random variable is represented by a straight line
- Any straight line on the normal probability paper represents a normal CDF

Strength of Ordinary Concrete

Ready mix concrete

3,000 psi (21 MPa)

3,500 psi (24 MPa)

4,000 psi (28 MPa)

4,500 psi (31 MPa)

5,000 psi (35 MPa)

6,000 psi (42 MPa)

Plant-cast concrete

5,000 psi (35 MPa)

5,500 psi (38 MPa)

6,000 psi (42 MPa)

6,500 psi (45 MPa)



Strength of Concrete

Light-weight concrete

3,000 psi (21 MPa)

3,500 psi (24 MPa)

4,000 psi (28 MPa)

5,000 psi (35 MPa)

High strength concrete

7,000 psi (49 MPa)

8,000 psi (56 MPa)

9,000 psi (62 MPa)

10,000 psi (70 MPa)

12,000 psi (84 MPa)



More Materials Data

- Compressive Strength of Ordinary Concrete, Ready mixed, f_c' : 3,000 3,500 4,000 4,500 5,000 and 6,000psi (21-42 MPa)
- Yield Stress of Reinforcing Steel Bars, Grade 60
Bar Sizes: #3, #4, #5, #6, #7, #8, #9, #10, #11 and #14 (9.5mm – 44 mm)
- Breaking Stress of Prestressing Steel (7-wire strands), Grade 270 (1865 MPa), Nominal Diameters: 0.5 in and 0.6 in (12.5-15 mm)

Ordinary Concrete – Number of Samples

Specified Compressive Strength of Concrete f'_c [psi]:

	3,000	3,500	4,000	4,500	5,000	6,000	
1	334		316		138	130	
2			156				
3	96		71		84		
4	82				66		
5	52						
6			54				
7	36						
8			60				
9			50				
10					206		
11					294		
12	1046	21	27	839			
13	350		274	298	2		
14	203	54	269		263		
15	424	8	220	164	8		
16	562	339	584	52	100		
17	116			90			
18	173	6	99	36	133		
19	180	99	533	80	422		
20			18		6		
21	8			2			
22	78		26	12			
23	276			346			
24			27				Total:
Total:	4016	527	2784	1919	1722	130	11098



Lightweight Concrete – Number of Samples

Strength, f'_c [psi]	3000	3500	4000	4500	5000	6000	6300	6800	7100
Source									
A					(286)				
B	282 (146)		180	1230 (752)	(79)	(517)			
C		417	542		(66)		876	392	517
D			334						
E			373						
F	61	132	246						
G	66	142	315		54 (52)				
H	100		82						
I*	100	42	140		368				
Total	755	733	2212	1982	905	517	876	392	517
Grand total	8889								

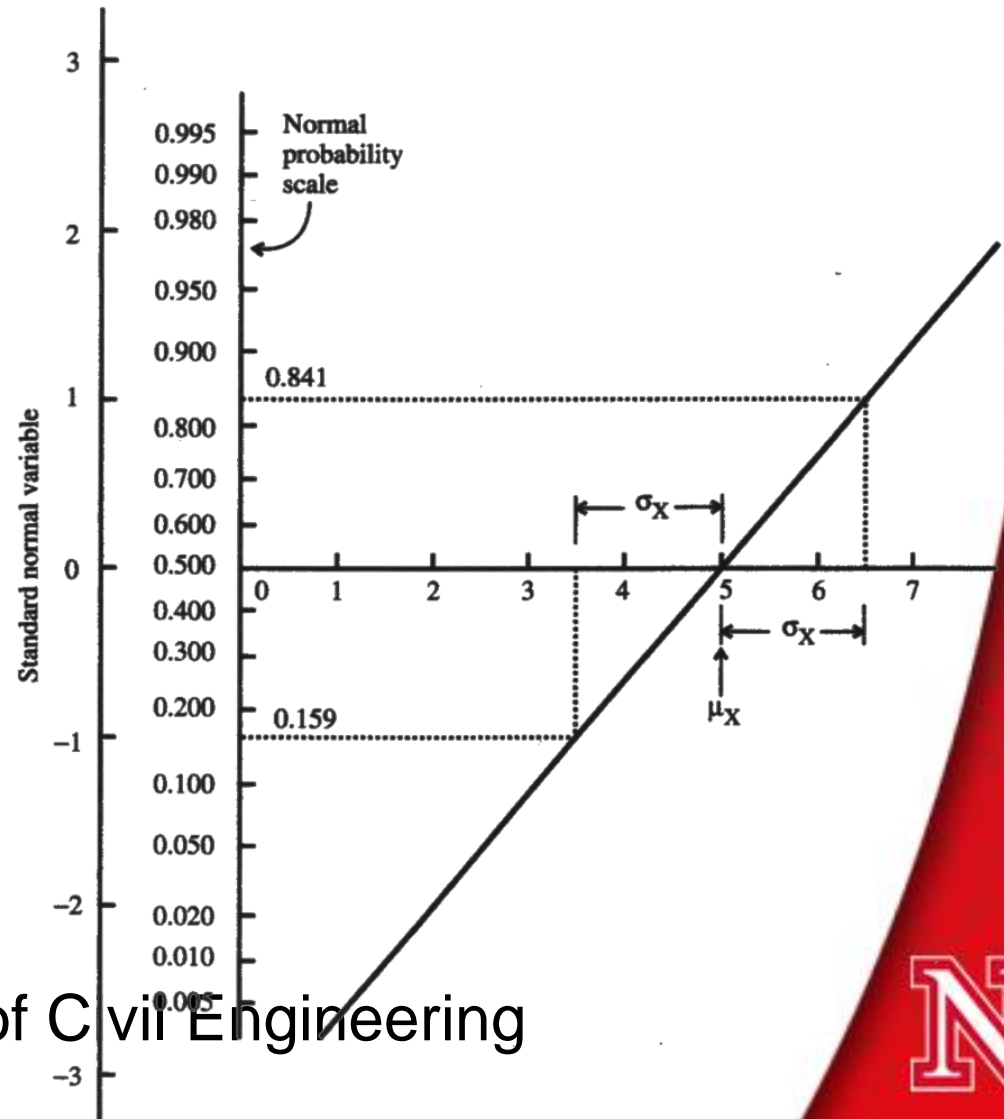


Presentation of Test Data

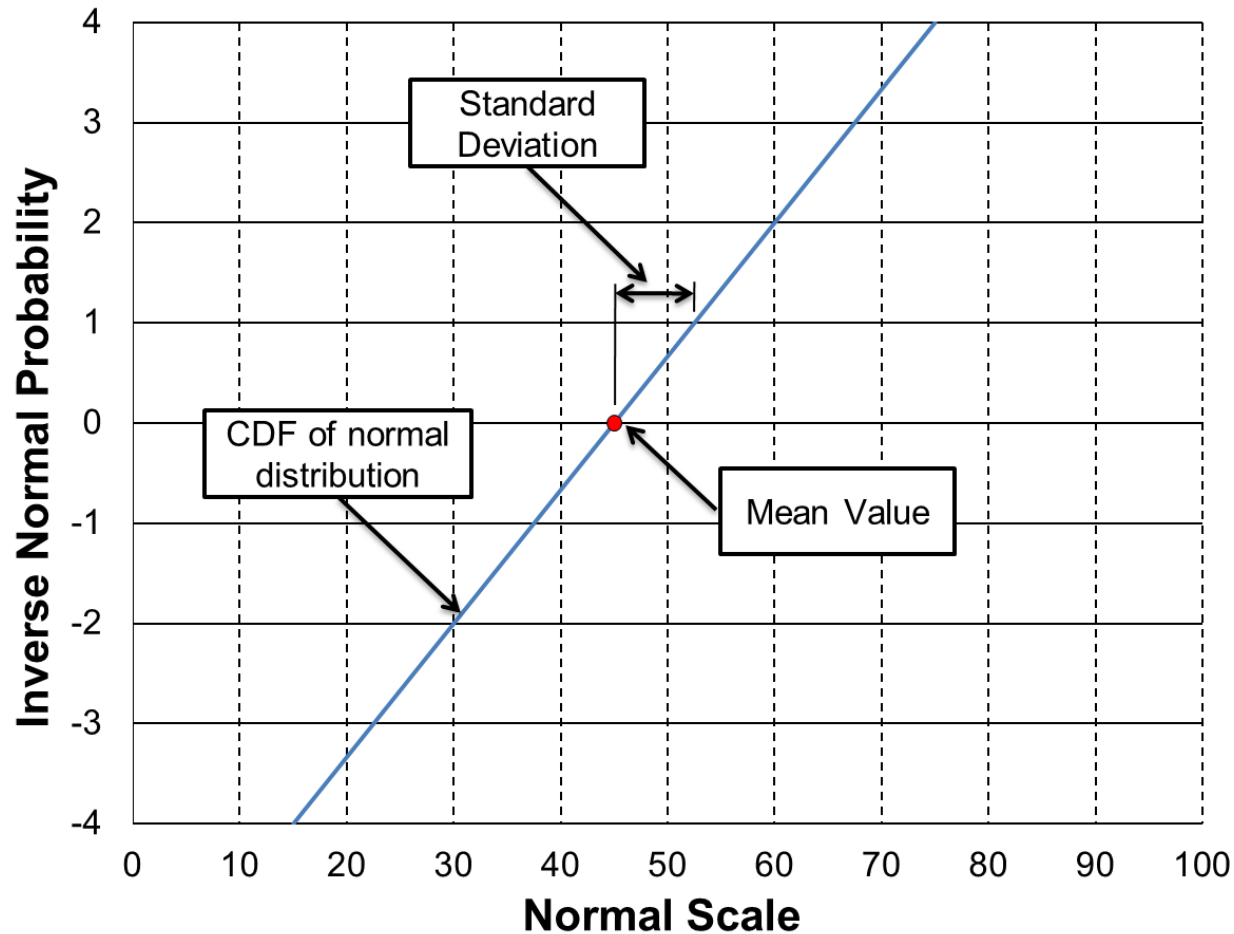
- Cumulative distribution functions (CDF) are plotted on the normal probability paper
- Vertical axis is the number of standard deviations from the mean value
- If CDF is close to a straight line, then the distribution is normal
- The mean and standard deviation can be read directly from the graph

Probability Paper

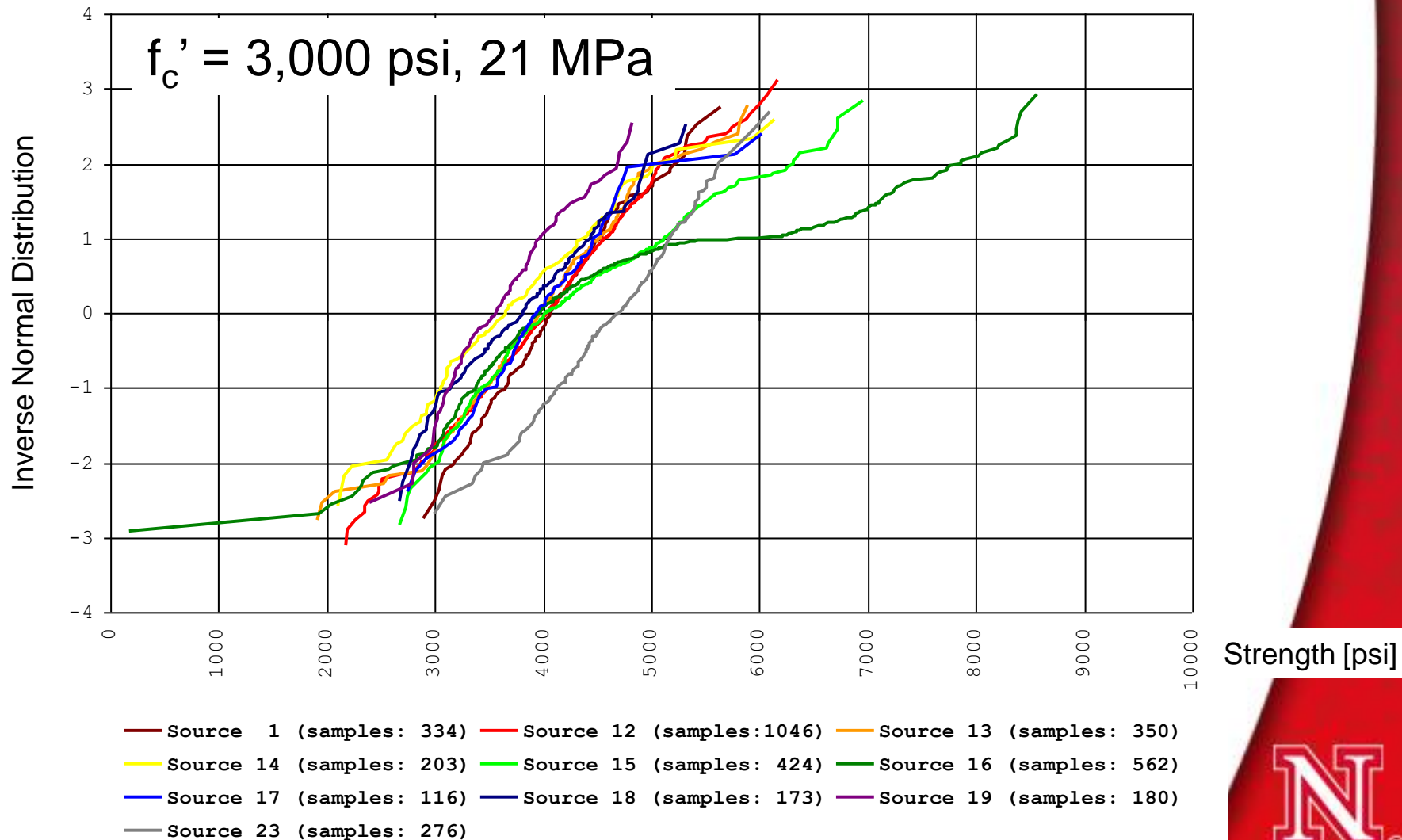
Data is plotted on the normal probability paper. A normal distribution function is represented by a straight line.



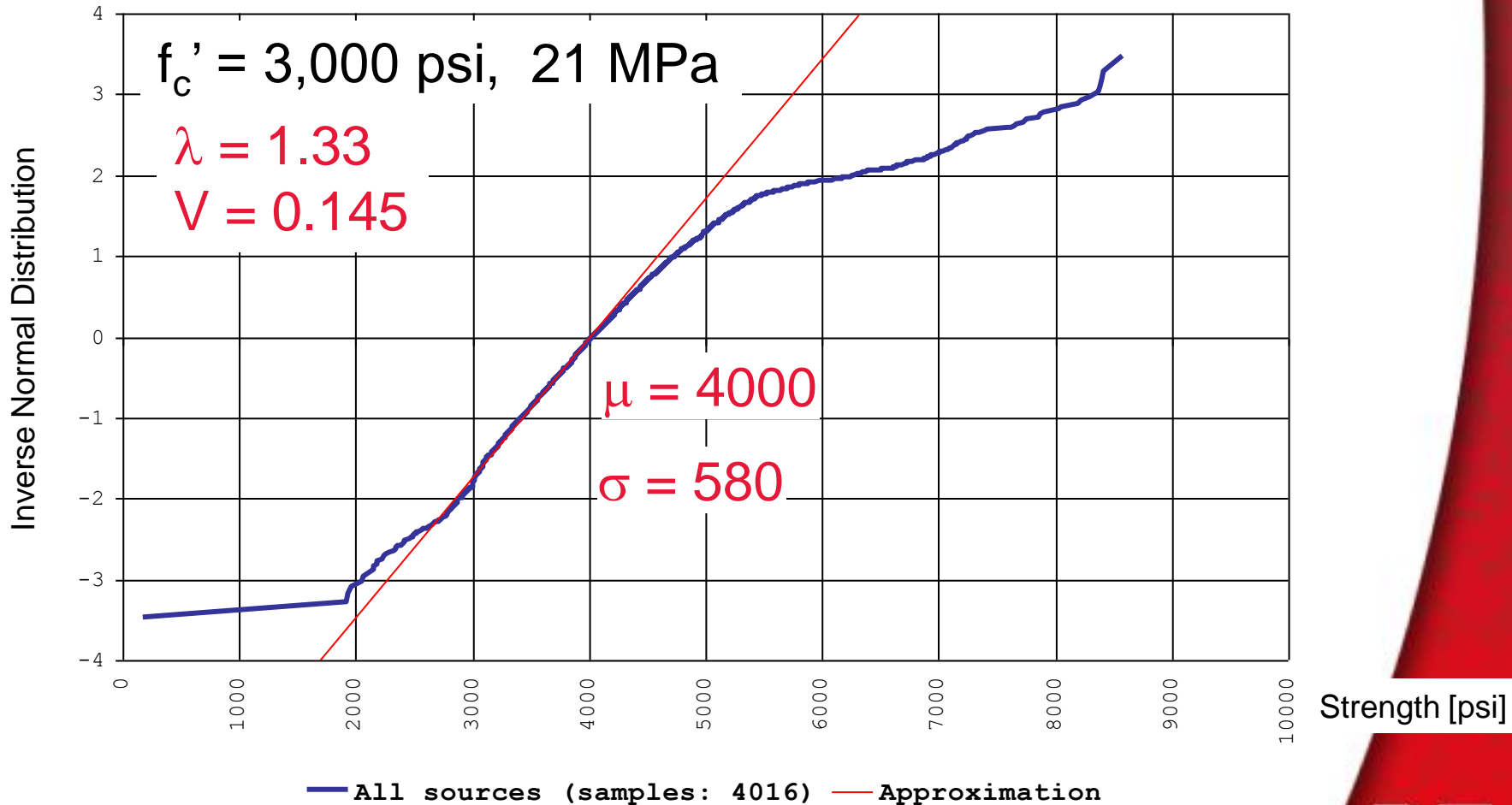
Probability Paper



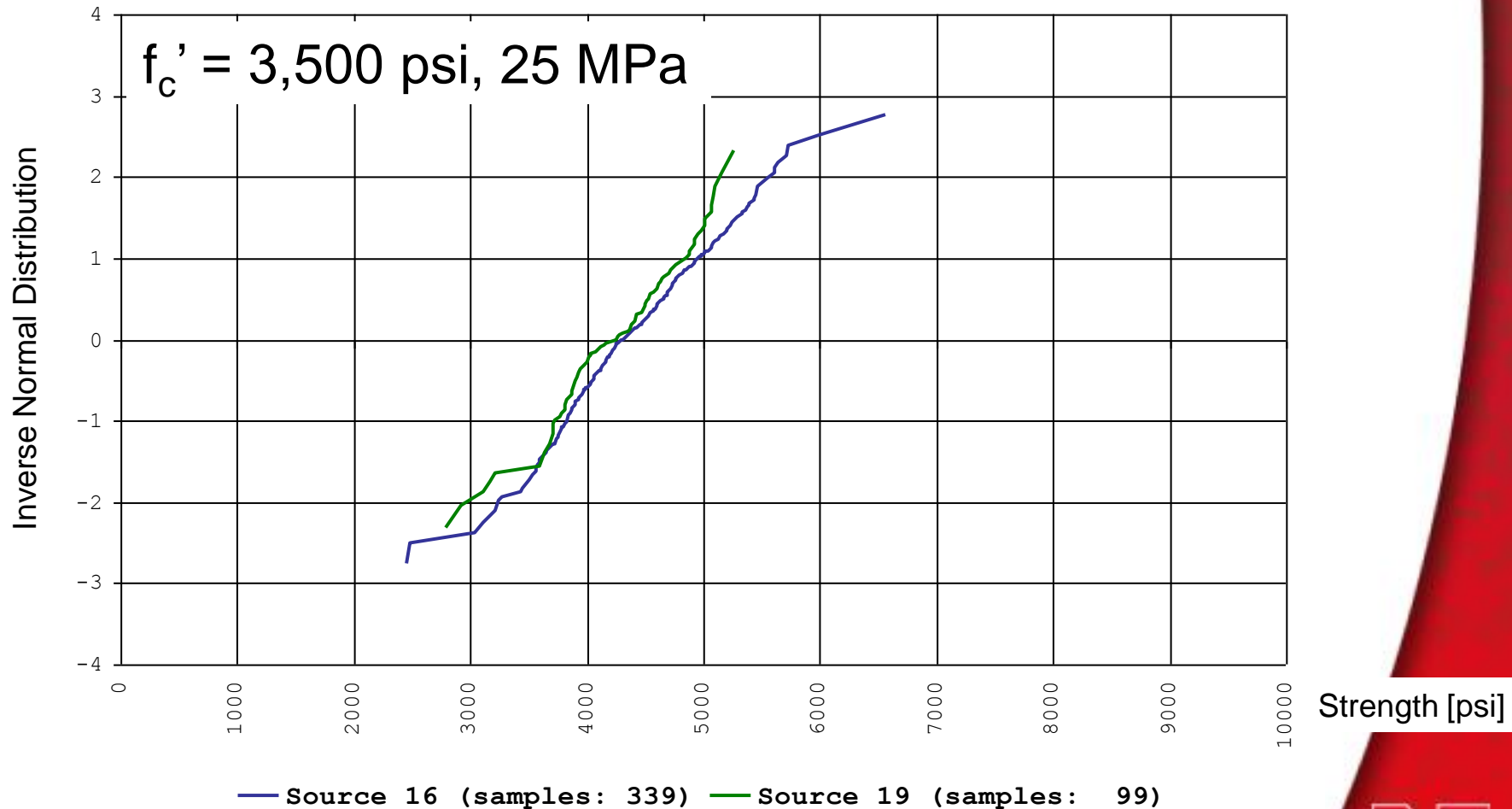
Ordinary Concrete – CDF of Strength



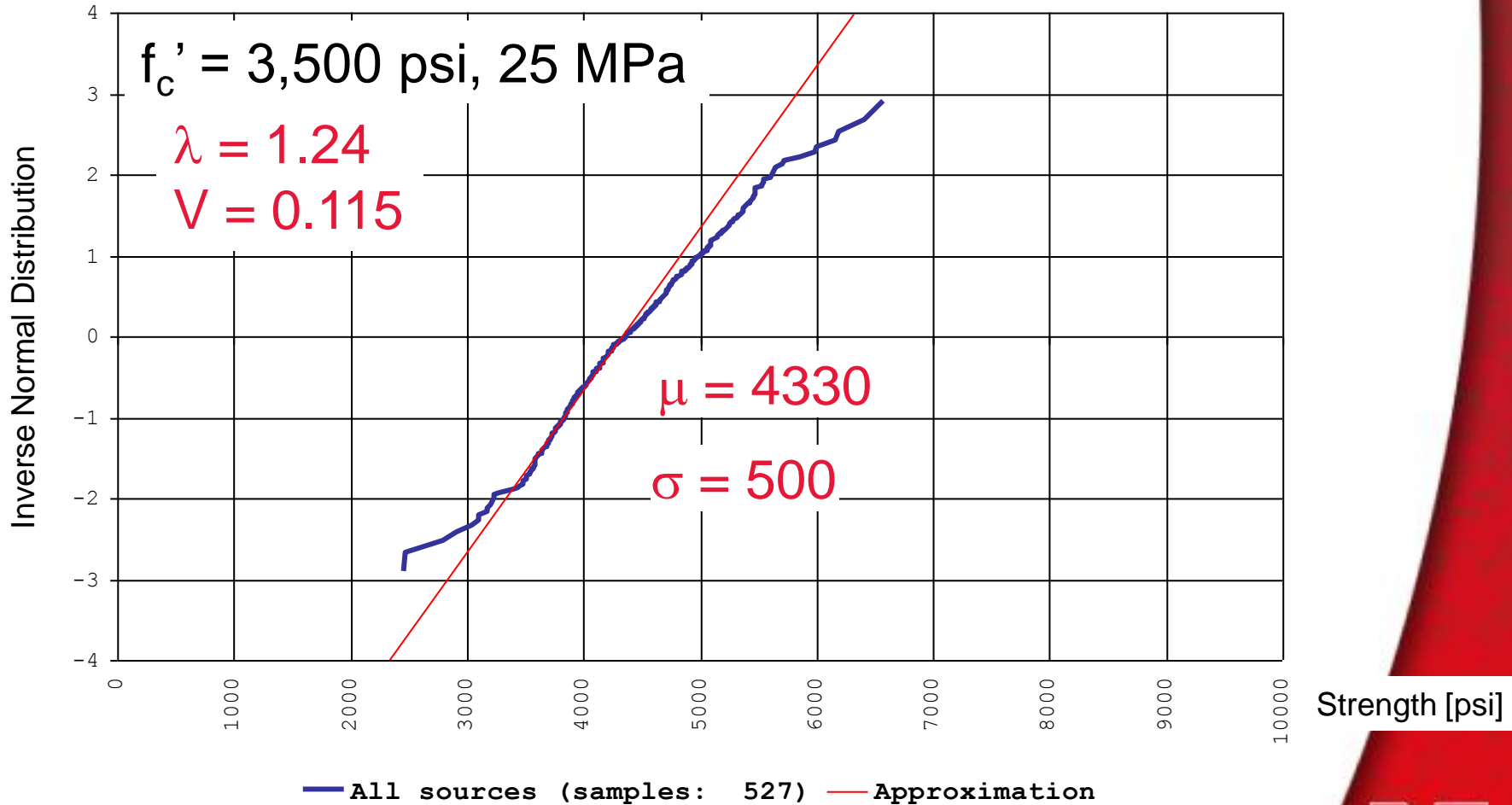
Ordinary Concrete – CDF of Strength



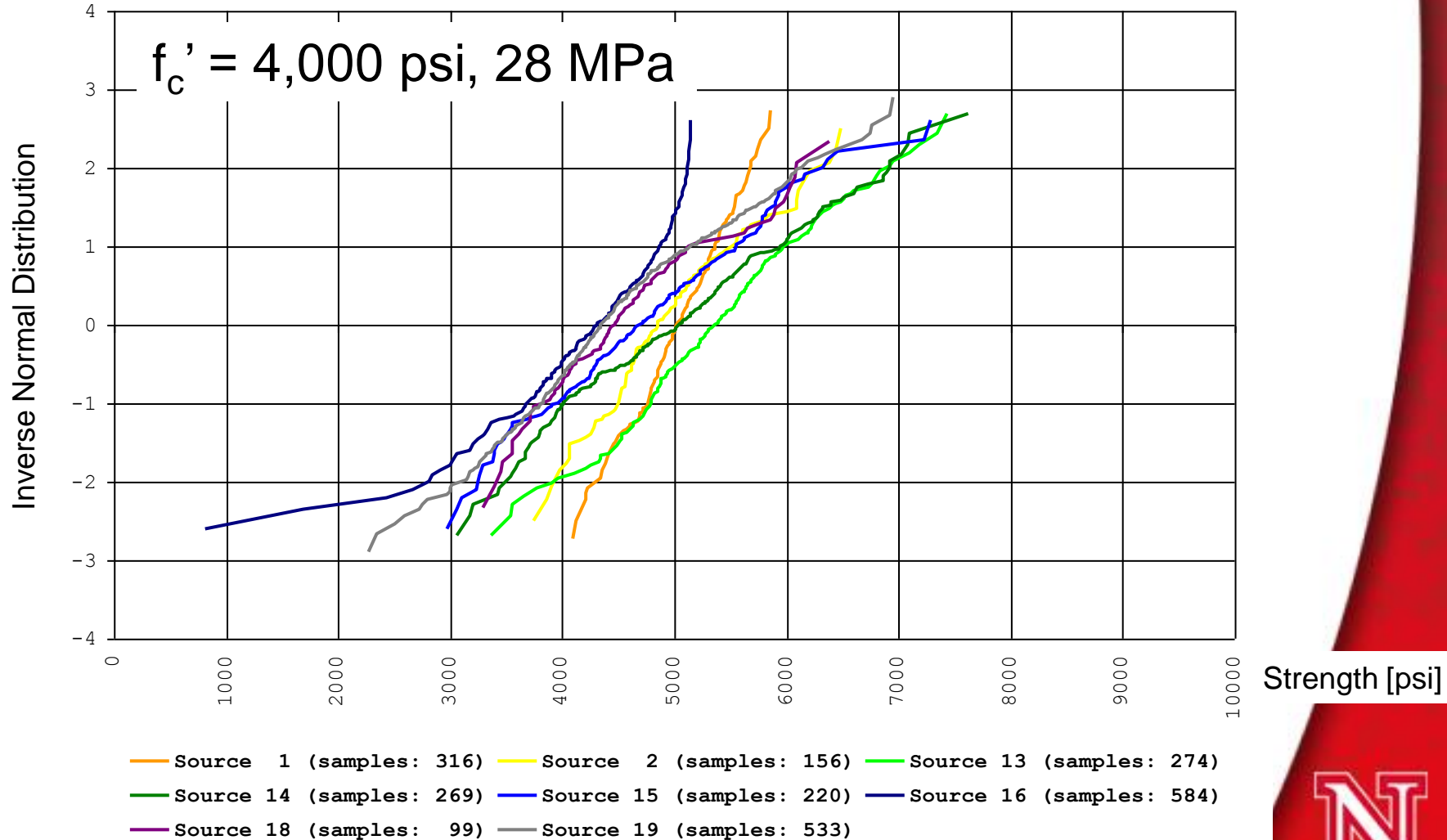
Ordinary Concrete – CDF of Strength



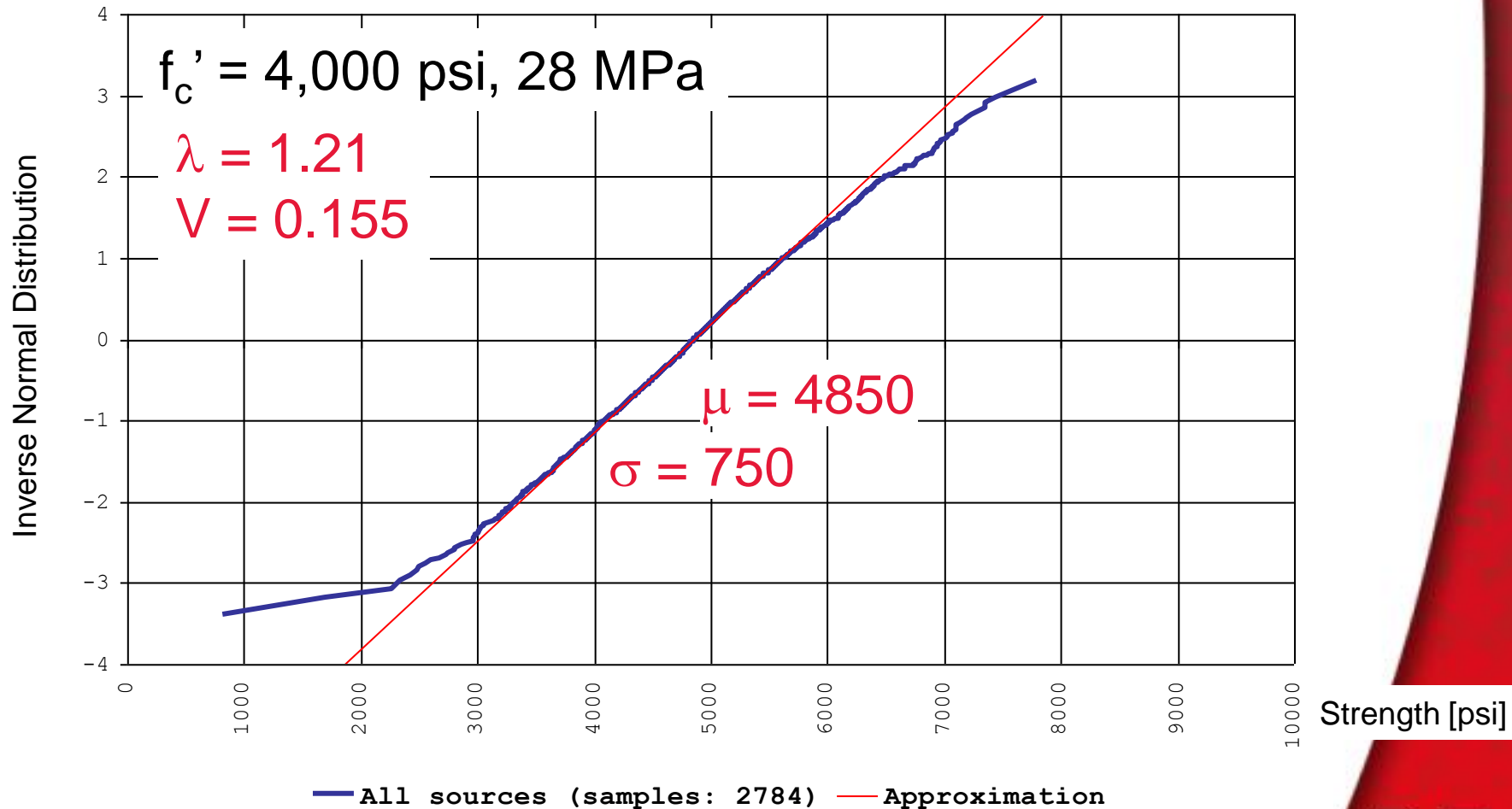
Ordinary Concrete – CDF of Strength



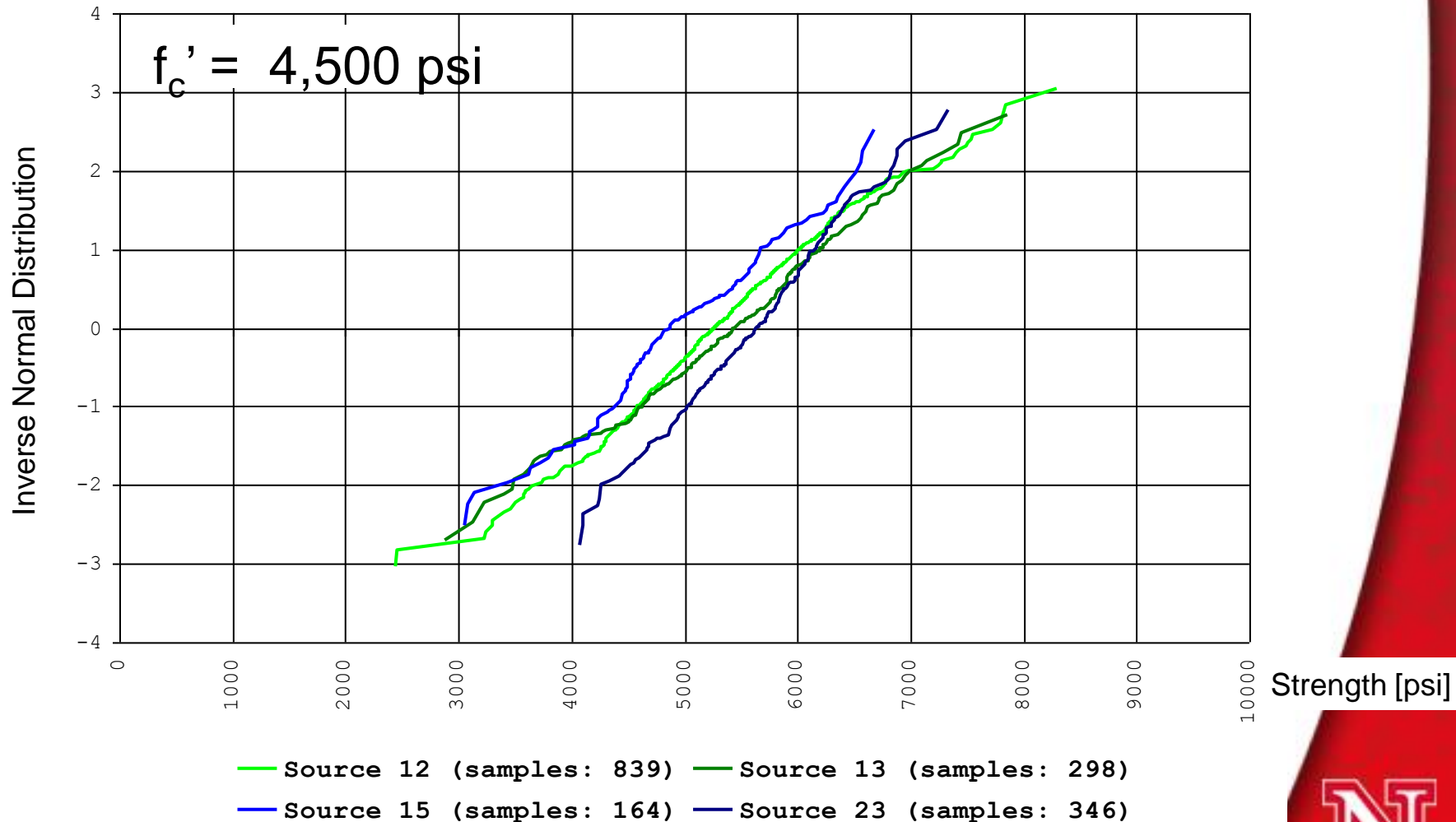
Ordinary Concrete – CDF of Strength



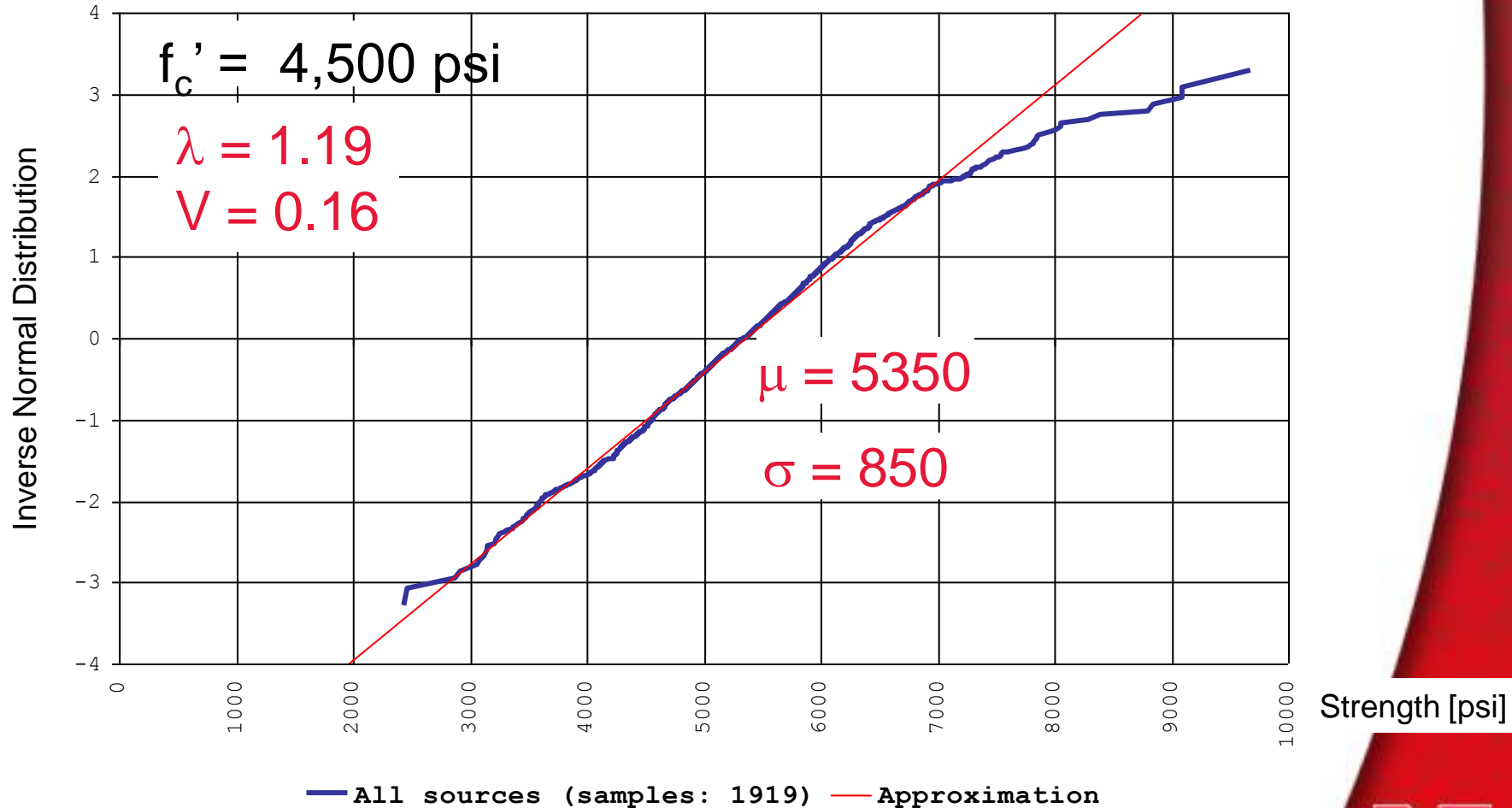
Ordinary Concrete – CDF of Strength



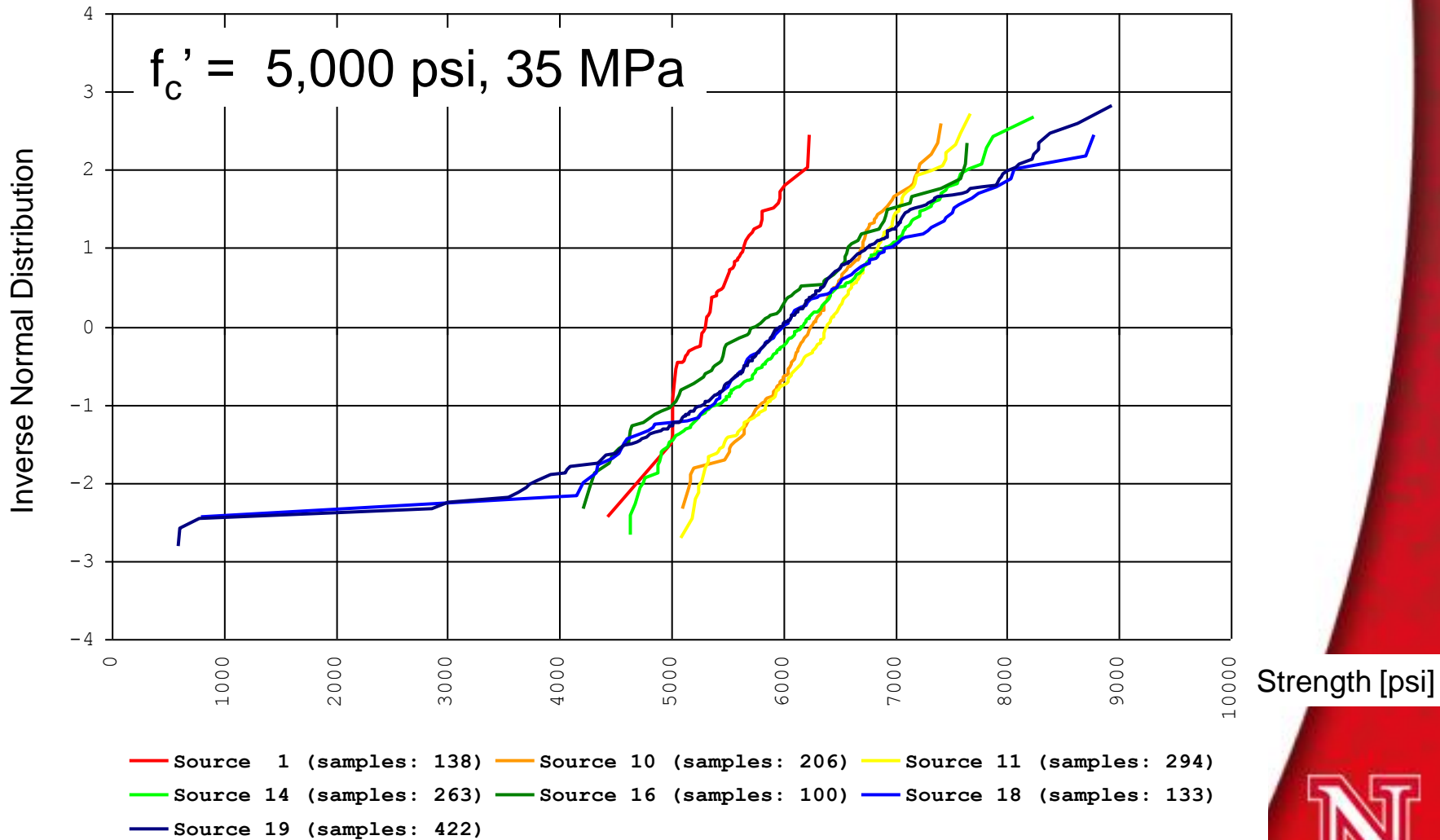
Ordinary Concrete – CDF of Strength



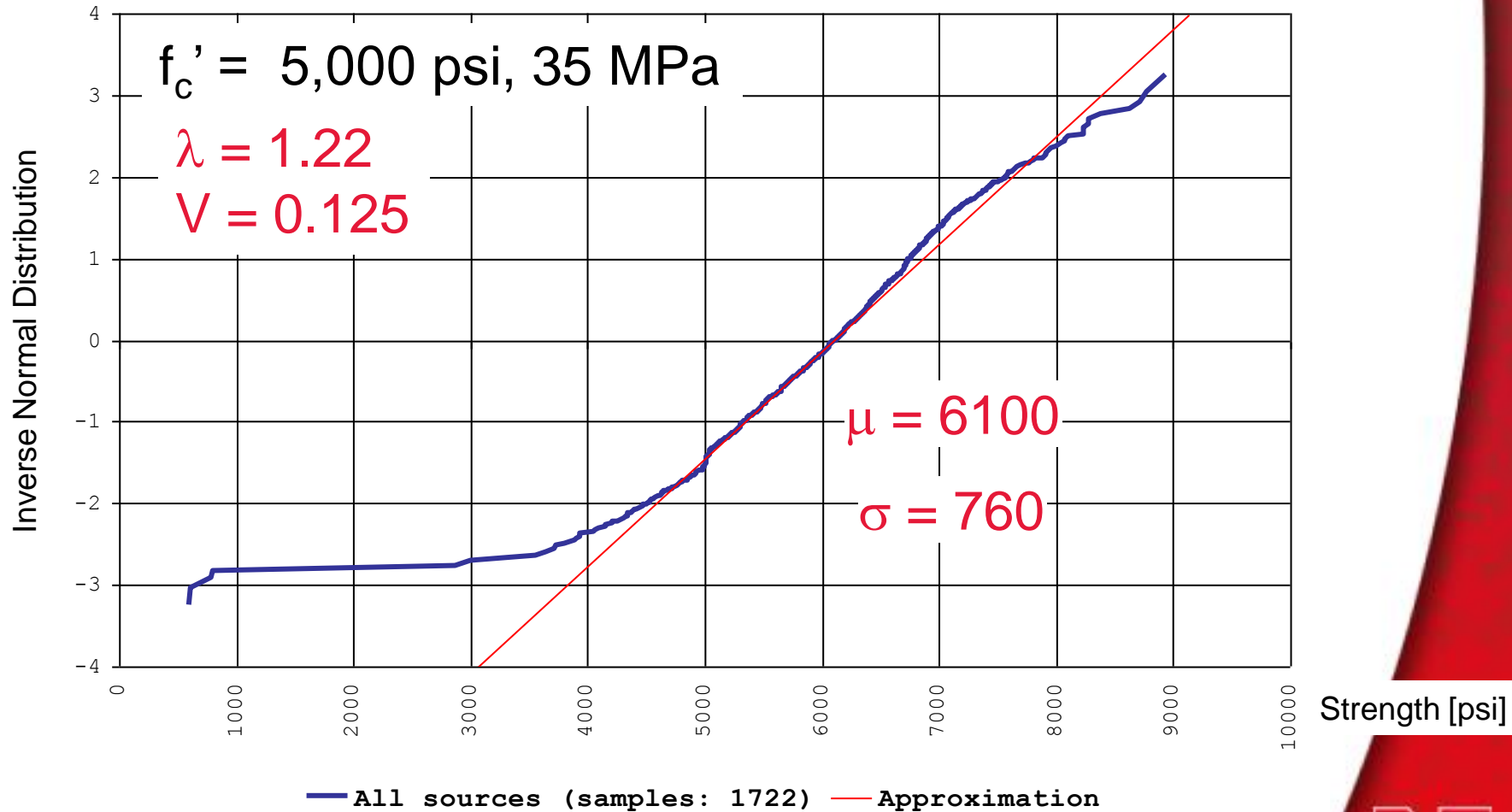
Ordinary Concrete – CDF of Strength



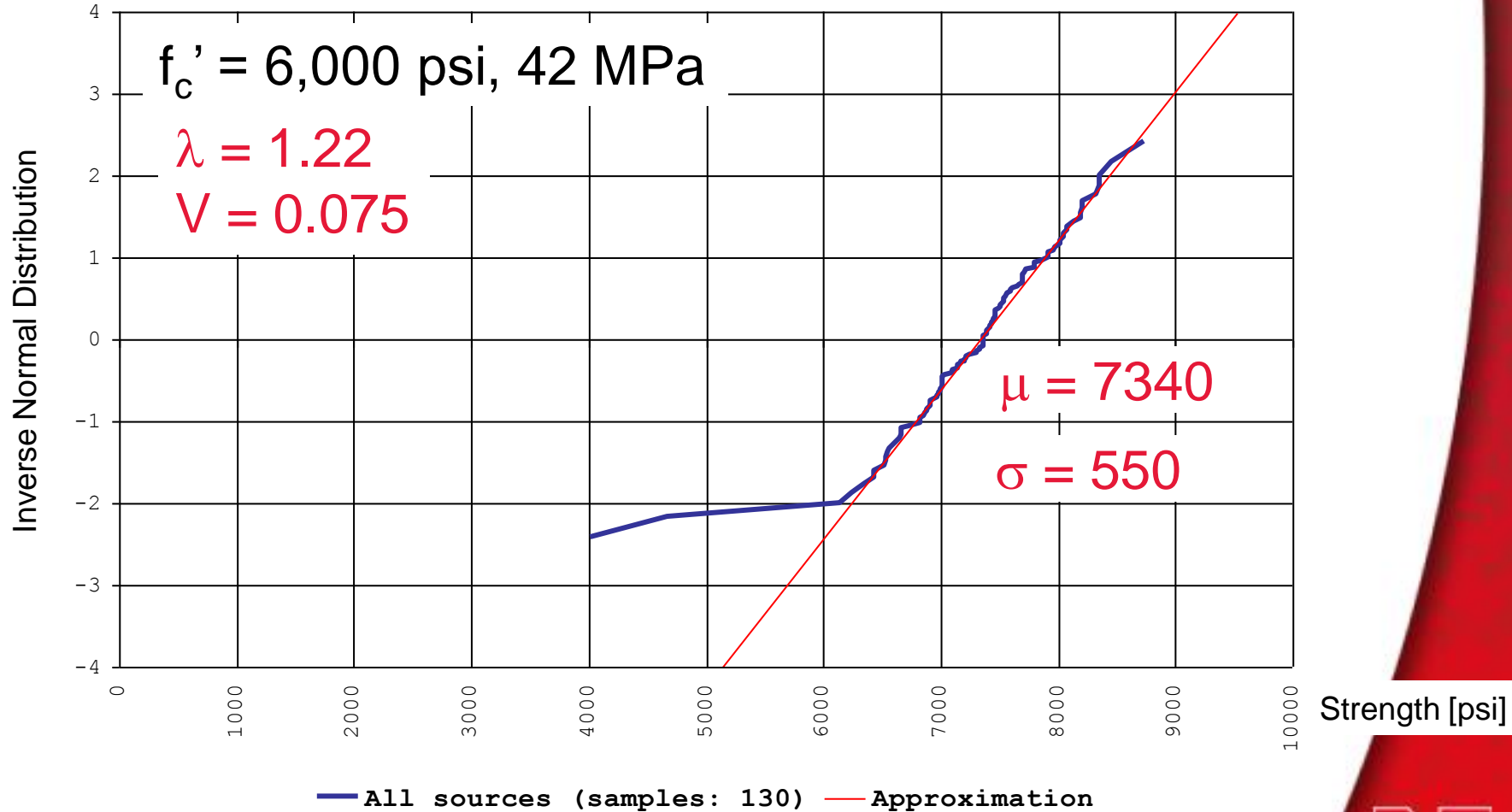
Ordinary Concrete – CDF of Strength



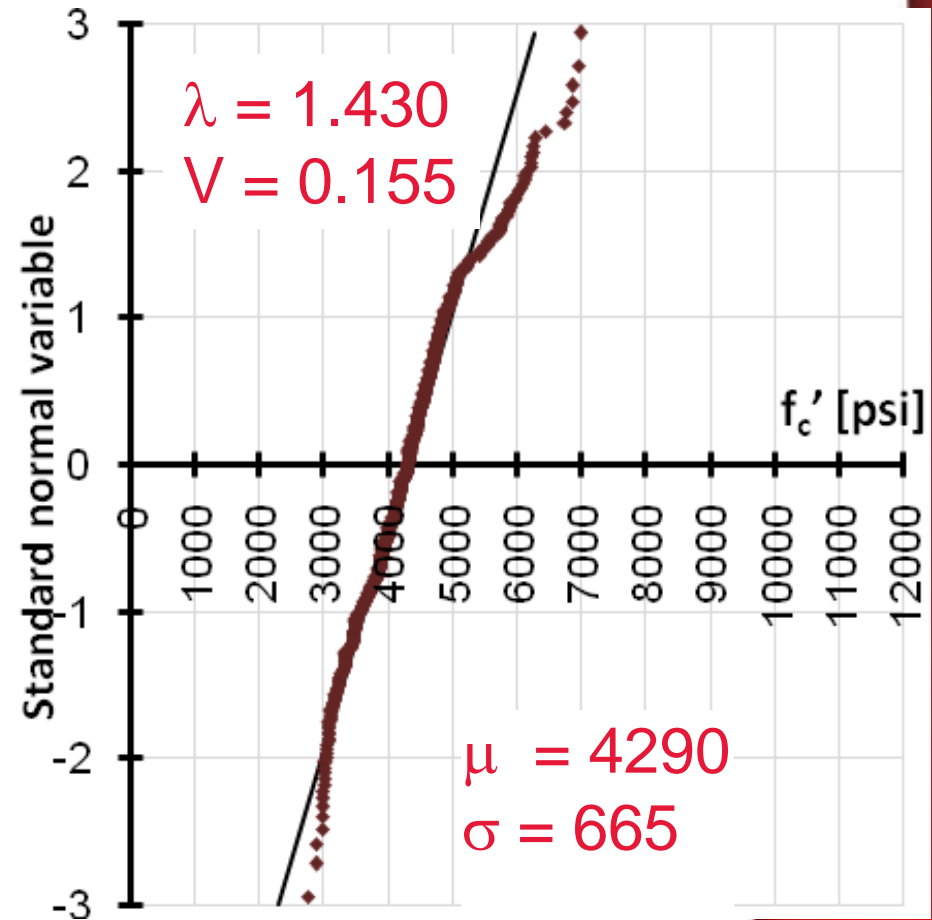
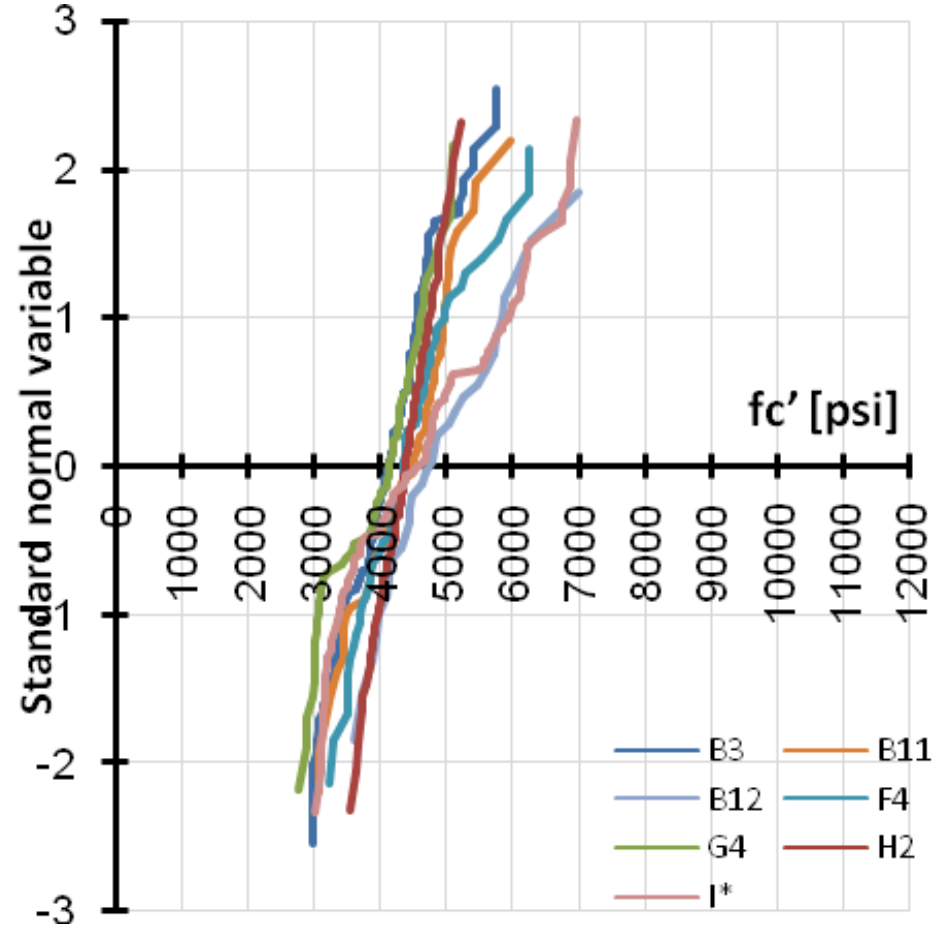
Ordinary Concrete – CDF of Strength



Ordinary Concrete – CDF of Strength



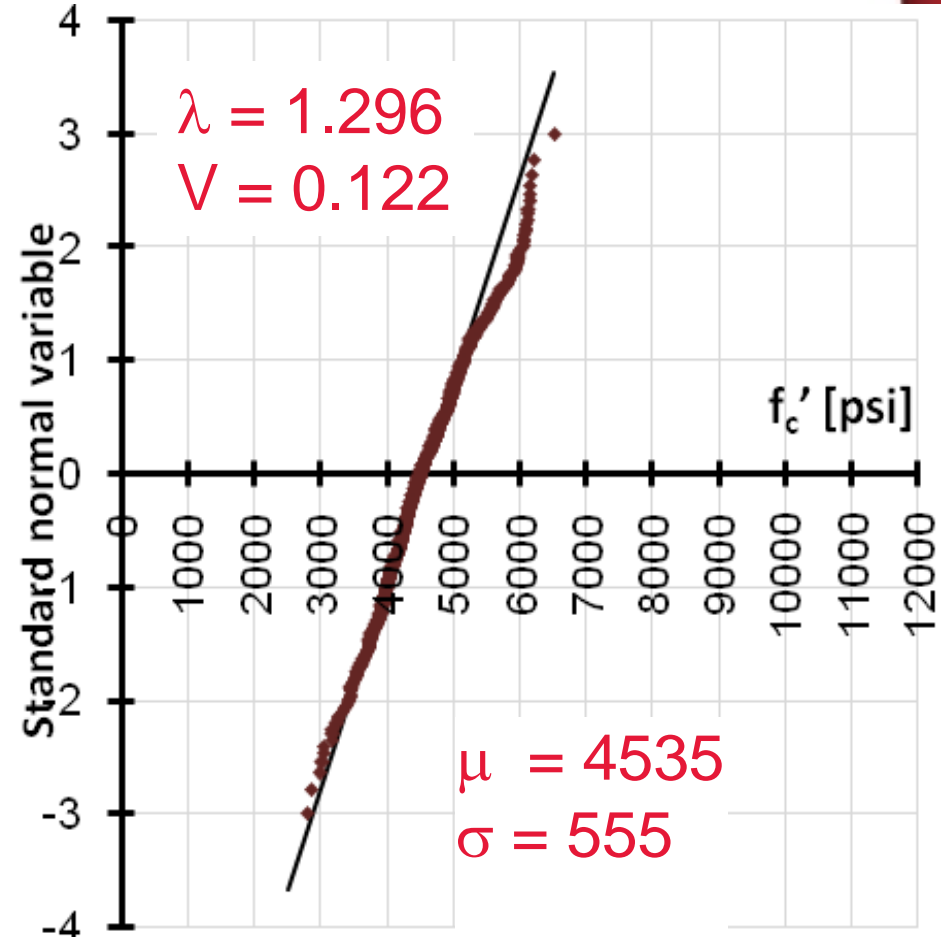
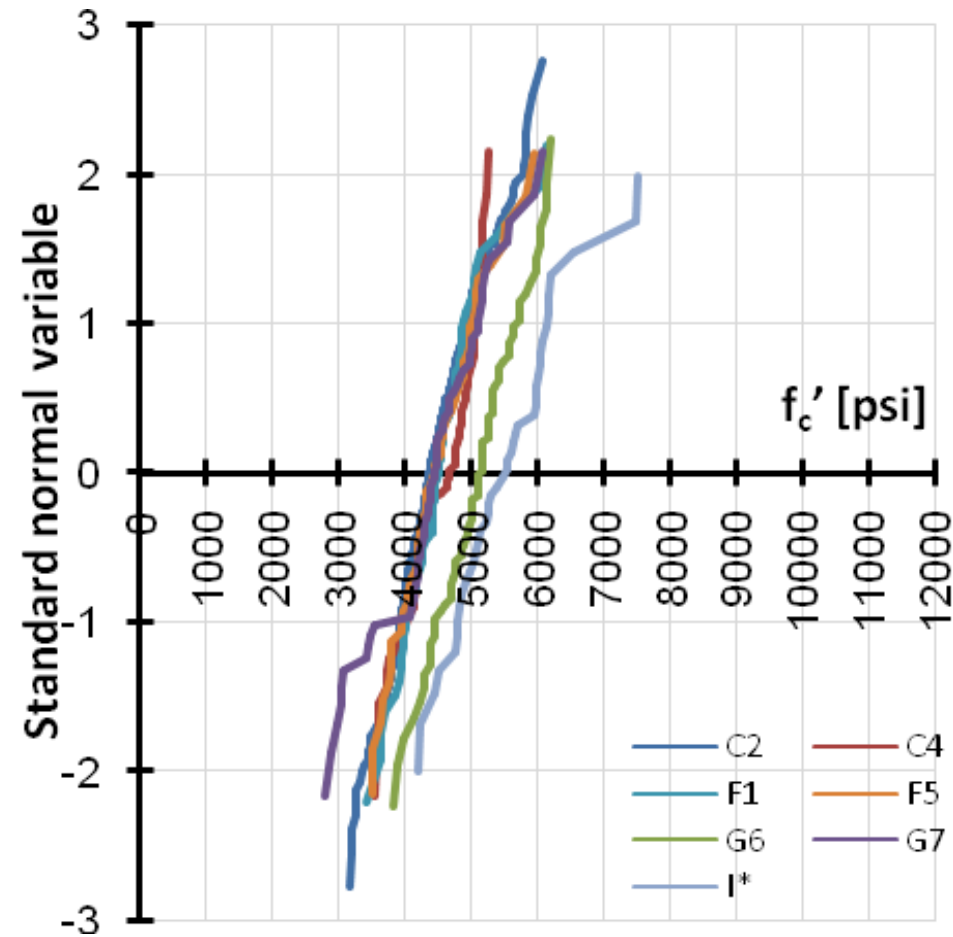
Lightweight Concrete – CDF of Strength



f_c' = 3000 psi, 21 MPa



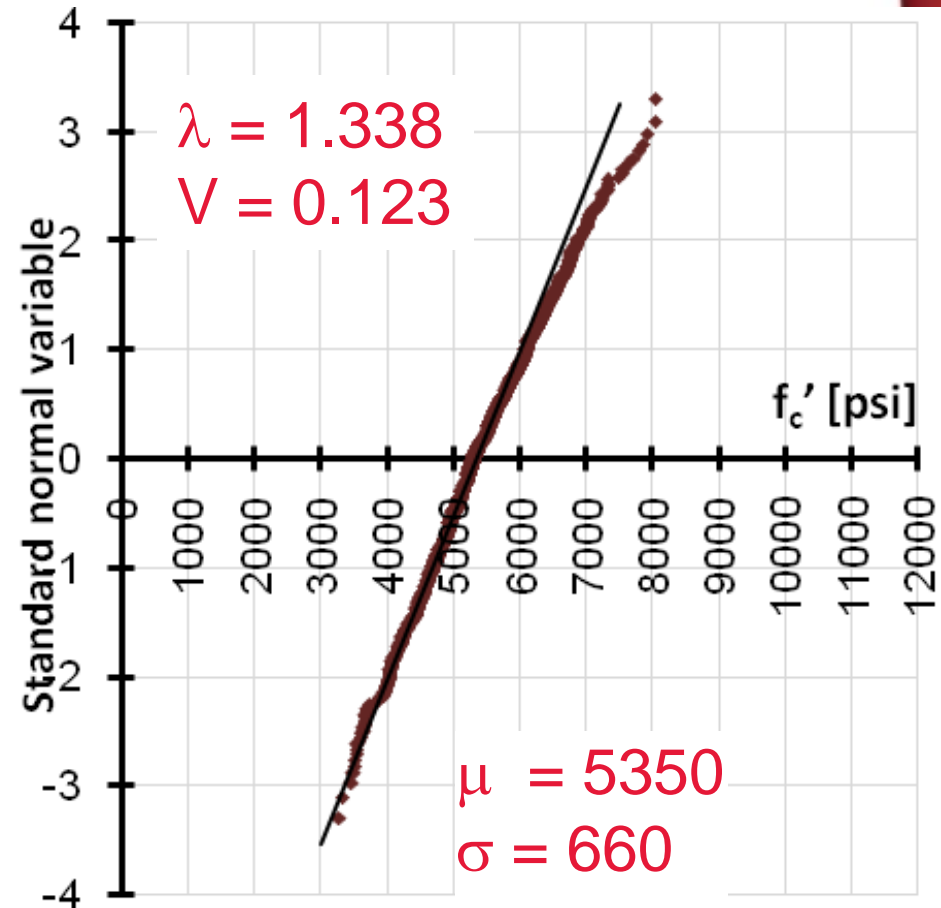
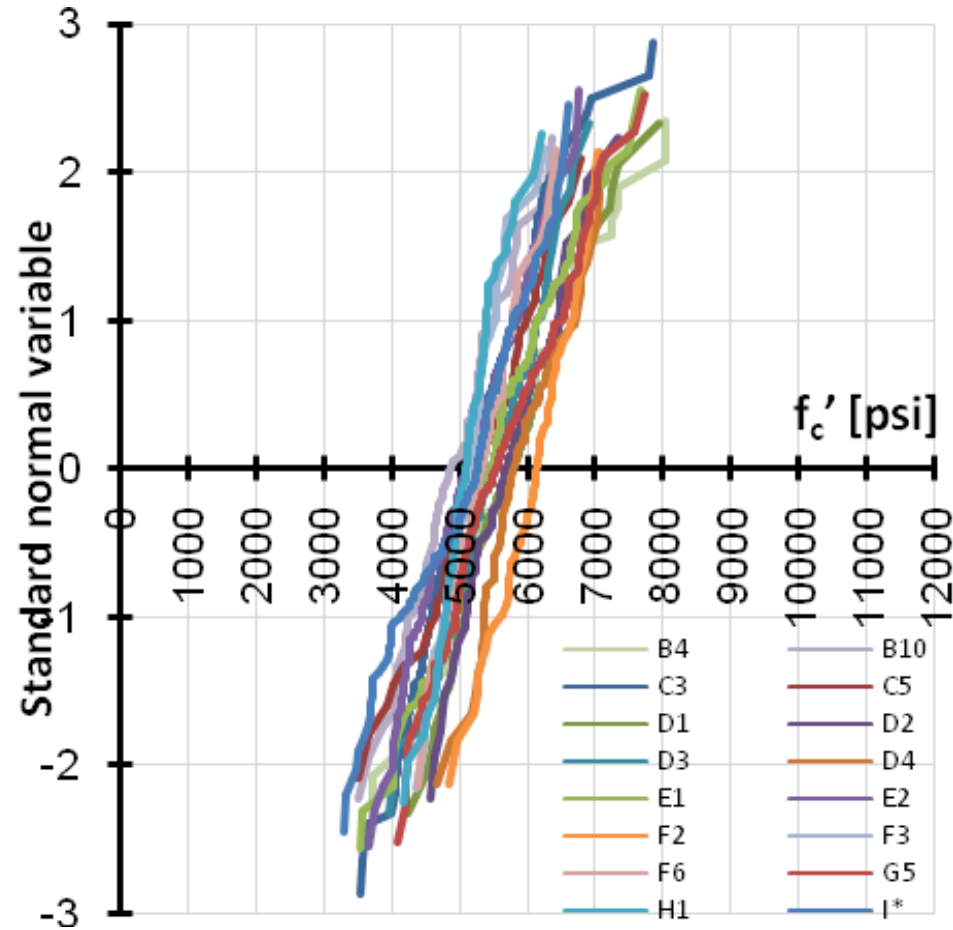
Lightweight Concrete – CDF of Strength



$f_c' = 3500$ psi, 25 MPa



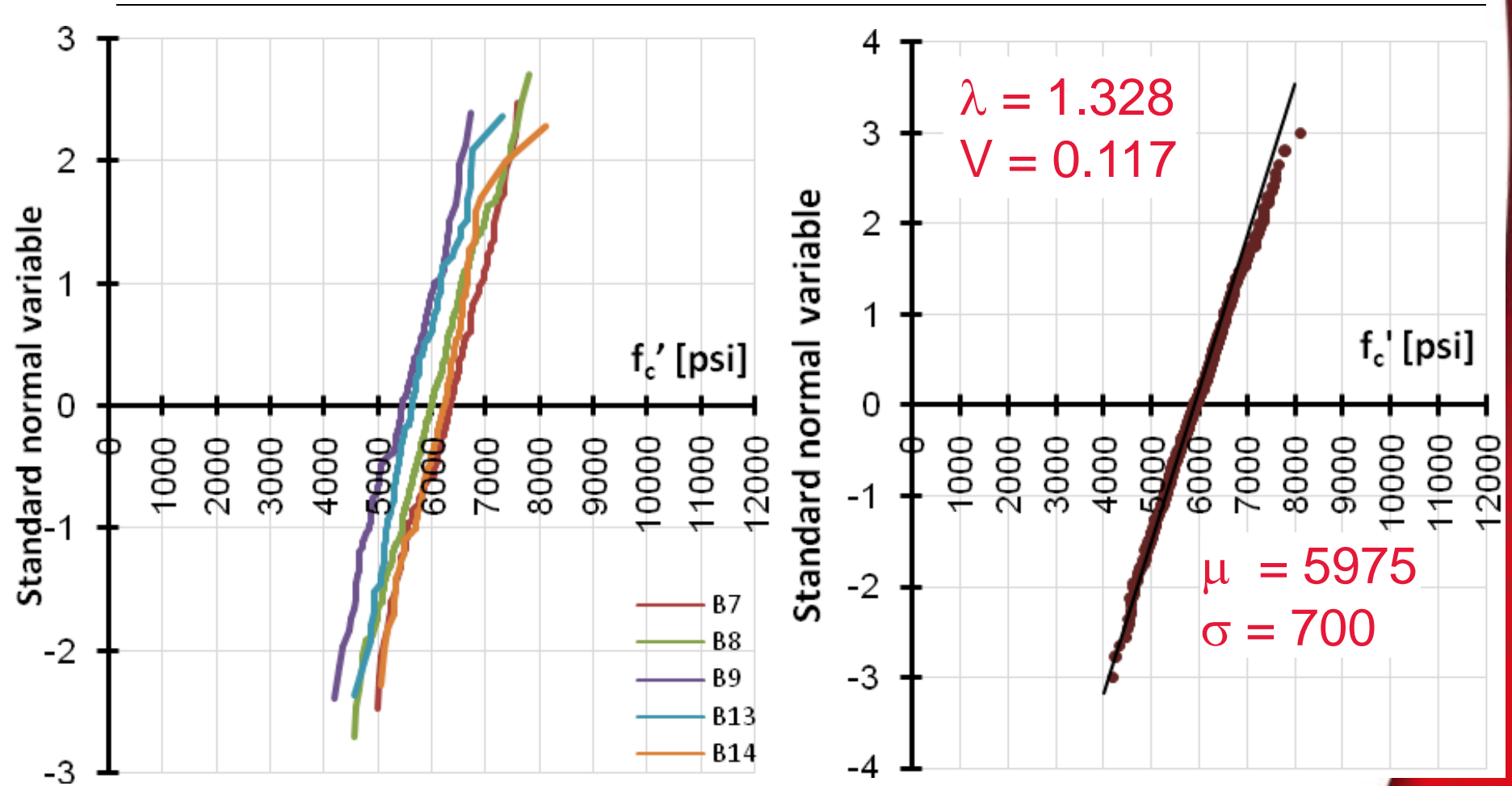
Lightweight Concrete – CDF of Strength



$f'_c = 4000$ psi, 28 MPa

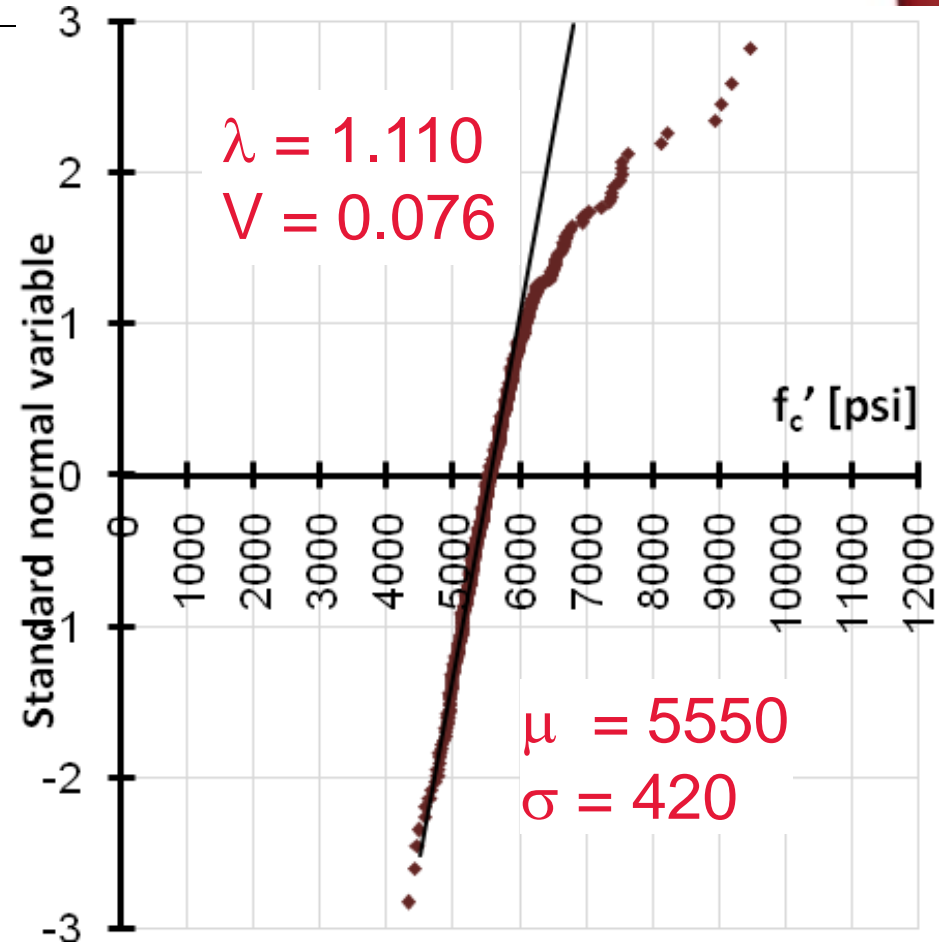
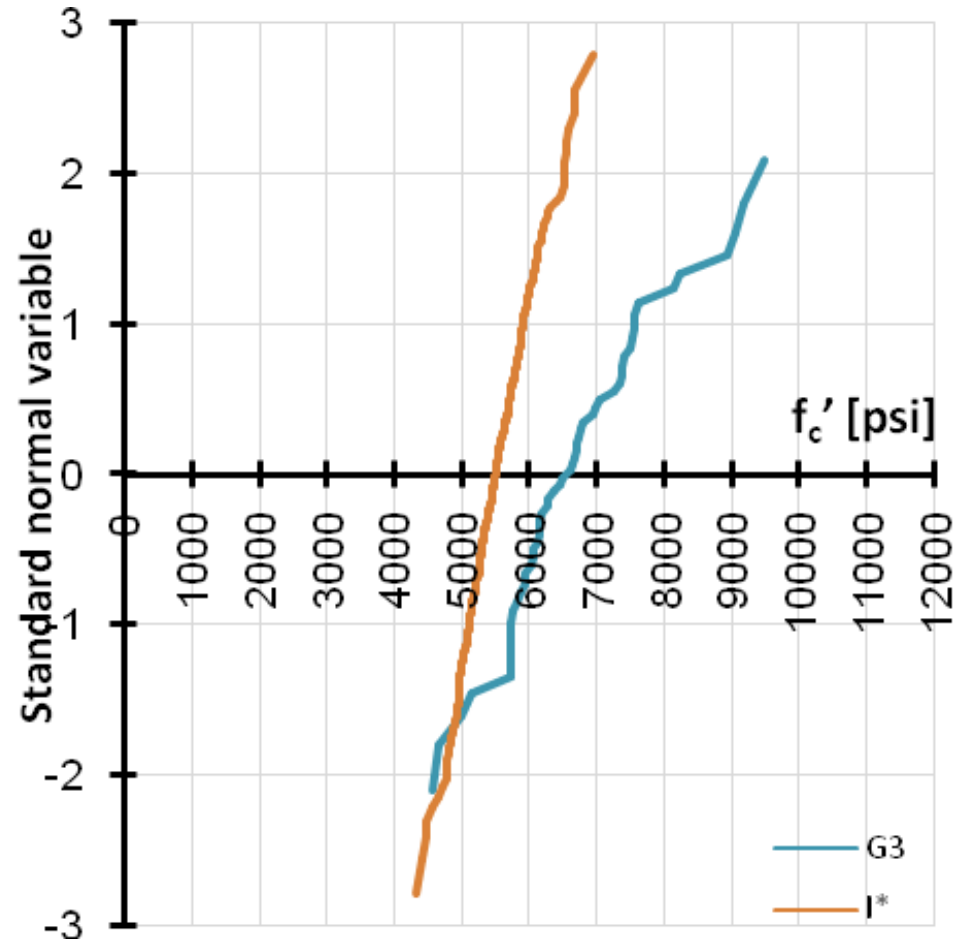


Lightweight Concrete – CDF of Strength



$f_c' = 4500$ psi , 32 MPa

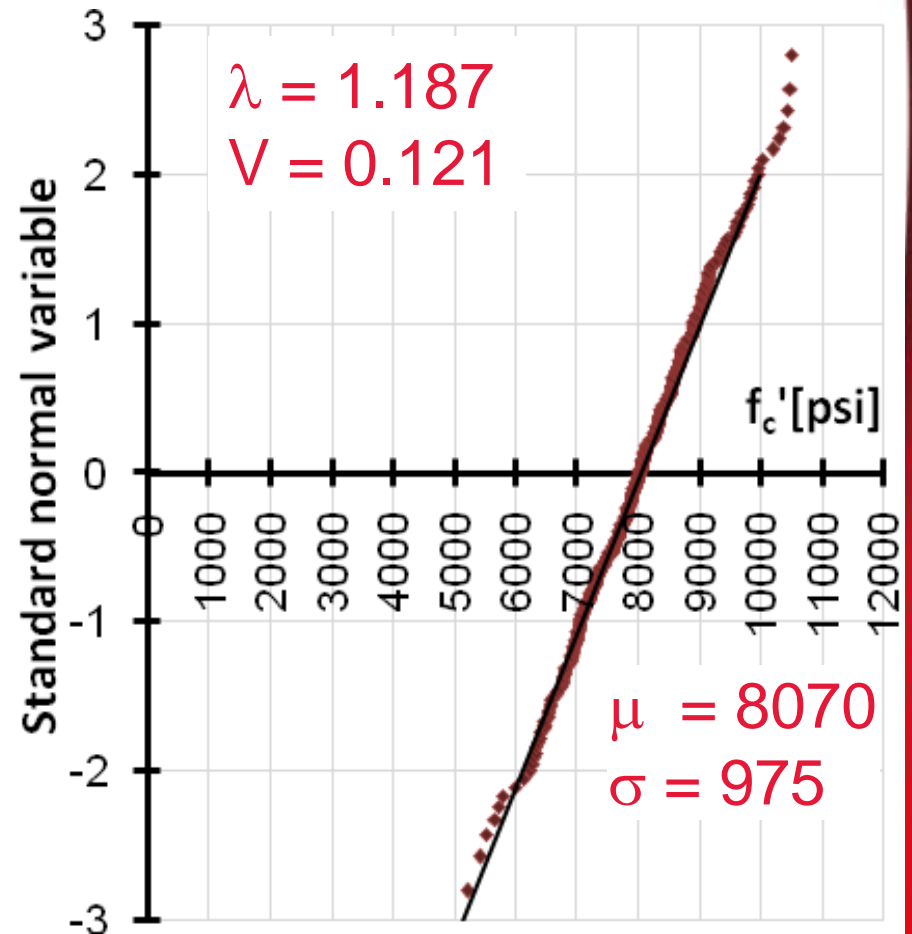
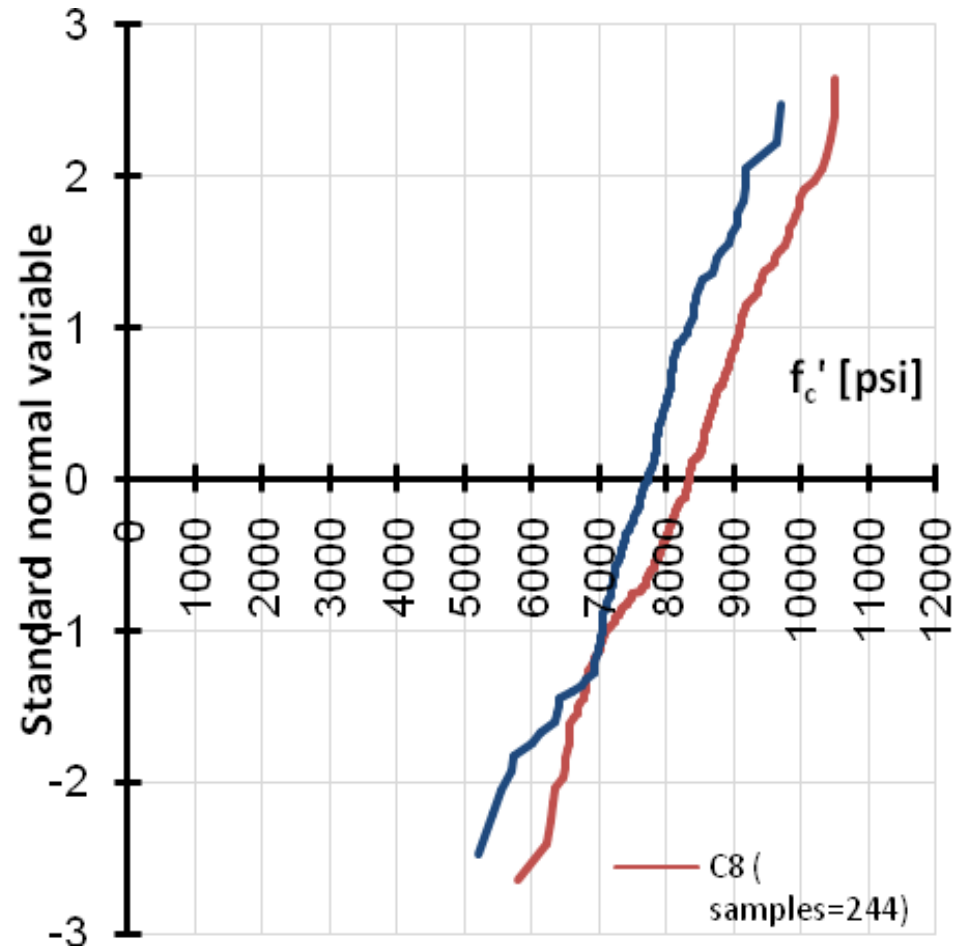
Lightweight Concrete – CDF of Strength



$f'_c = 5000$ psi , 35 MPa

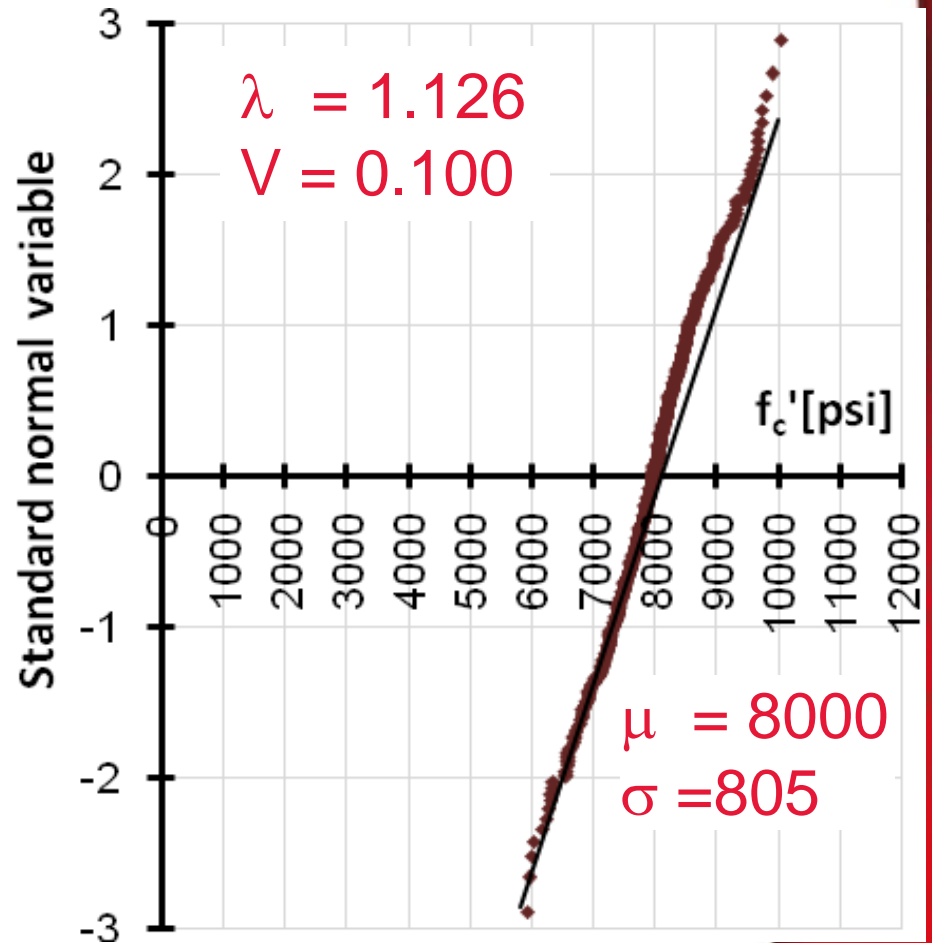
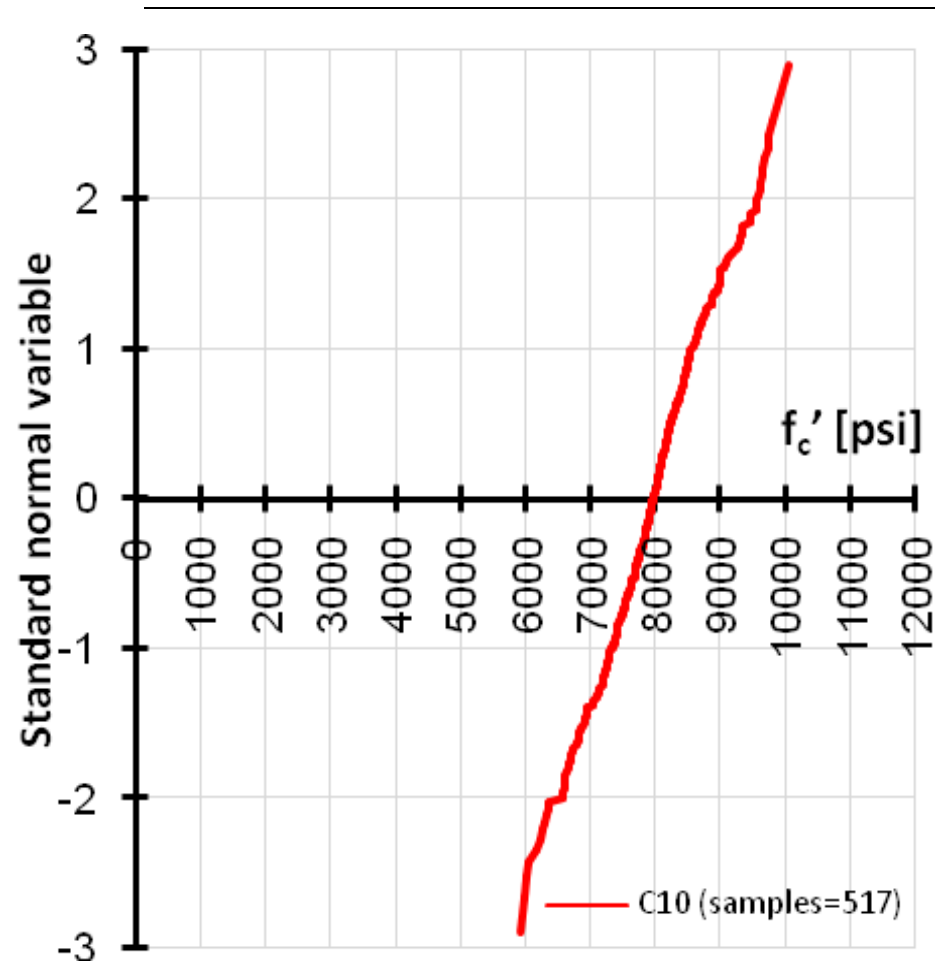


Lightweight Concrete – CDF of Strength



$f'_c = 6800$ psi , 48 MPa

Lightweight Concrete – CDF of Strength

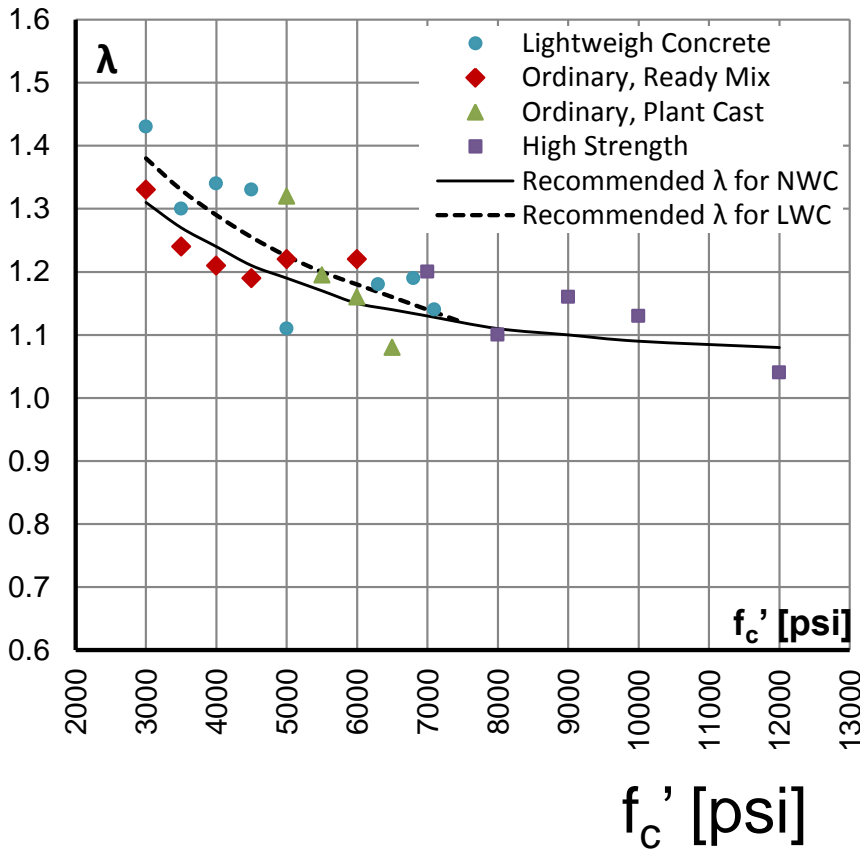


$f_c' = 7100$ psi, 49 MPa

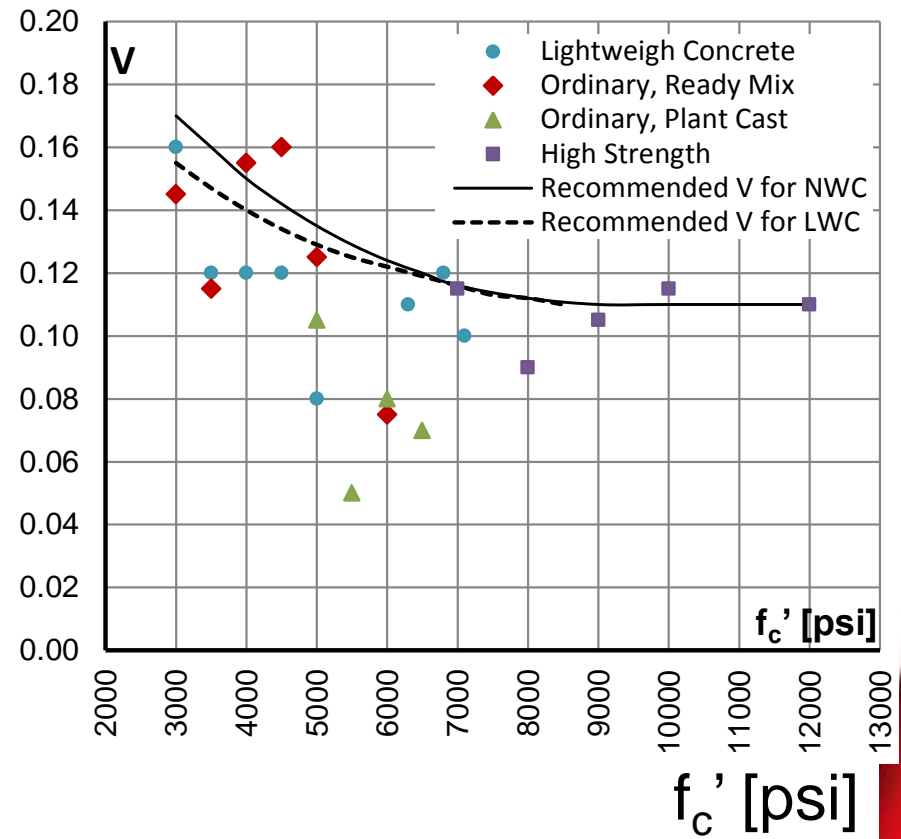


Summary of the Statistical Parameters for Concrete

λ



V



Bias Factor and Coefficient of Variation for Compressive Strength and Shear Strength of Concrete

Concrete Grade f'_c (psi)	Compressive strength		Shear Strength	
	λ	V	λ	V
3000, 21 MPa	1.31	0.17	1.31	0.205
3500	1.27	0.16	1.27	0.19
4000, 28 MPa	1.24	0.15	1.24	0.18
4500	1.21	0.14	1.21	0.17
5000	1.19	0.135	1.19	0.16
5500	1.17	0.13	1.17	0.155
6000, 42 MPa	1.15	0.125	1.15	0.15
6500	1.14	0.12	1.14	0.145
7000	1.13	0.115	1.13	0.14
8000	1.11	0.11	1.11	0.135
9000	1.10	0.11	1.10	0.135
10,000	1.09	0.11	1.09	0.135
12,000, 84 MPa	1.08	0.11	1.08	0.135

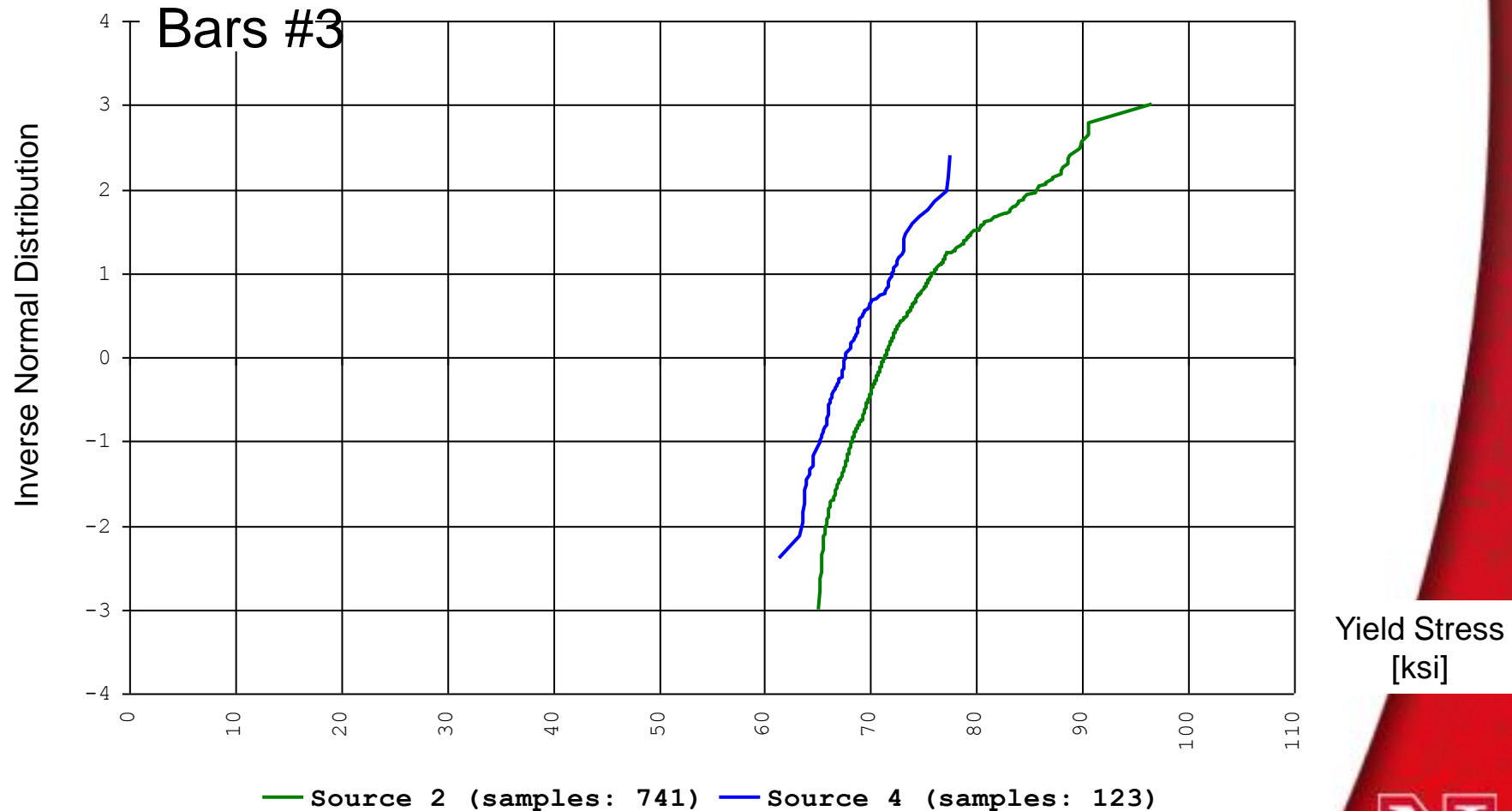


Reinforcing Steel Bars, Grade 60 (420 MPa) – Number of Samples

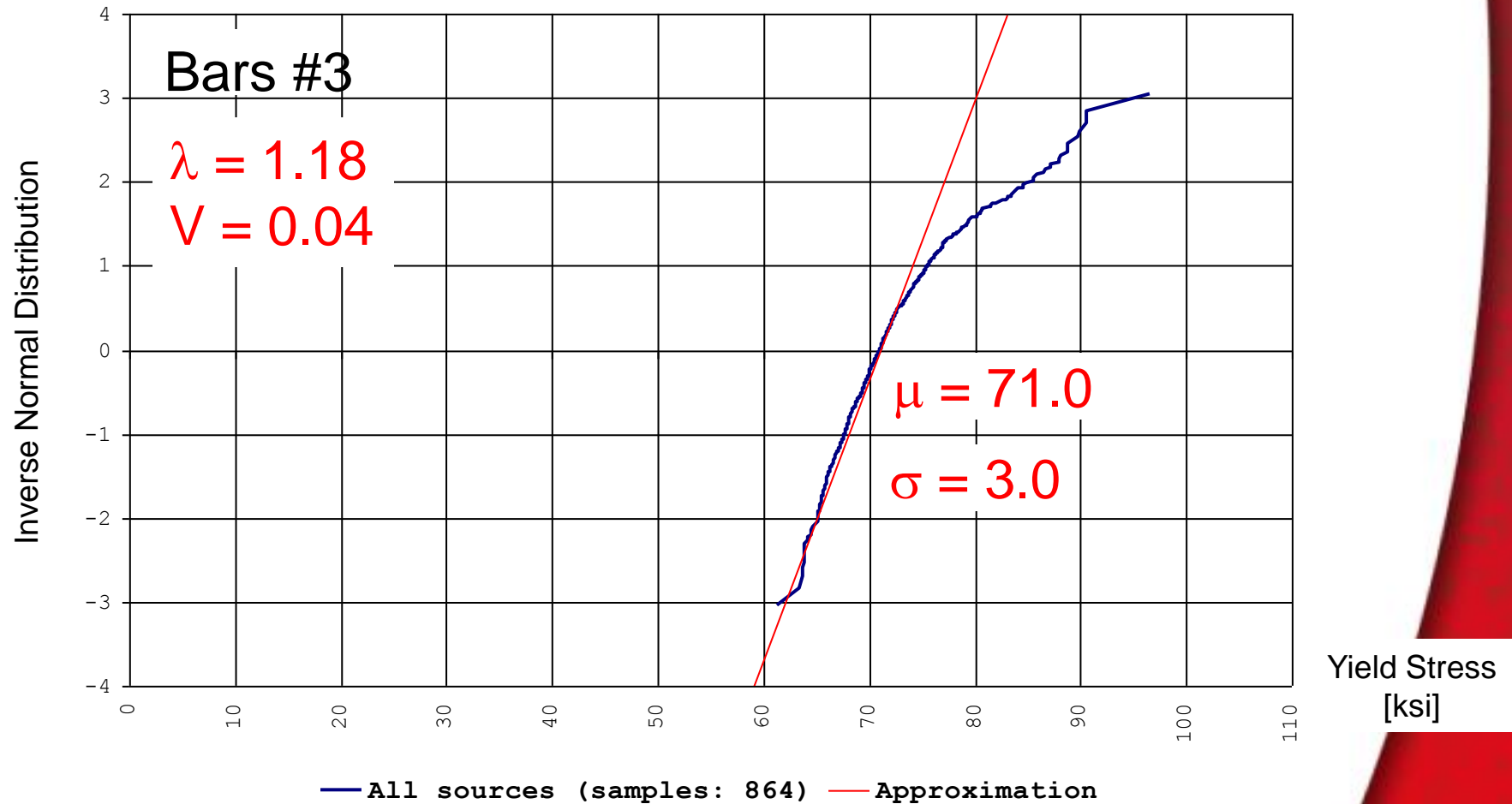
		Bar Size:										
		#3	#4	#5	#6	#7	#8	#9	#10	#11	#14	
Source:	1		60	60	60	60	60	60	60	60		
	2	741	2369	3333	1141	1318	1146	1290	825	1019		
	3		60	60	60	60	60	60	60	60	12	
	4	123	106	179	104	79	90	73	70	87		
	5		90	90	90	90	90	90	74	90		Total:
Total:	864	2685	3722	1455	1607	1446	1573	1089	1316	12	15769	



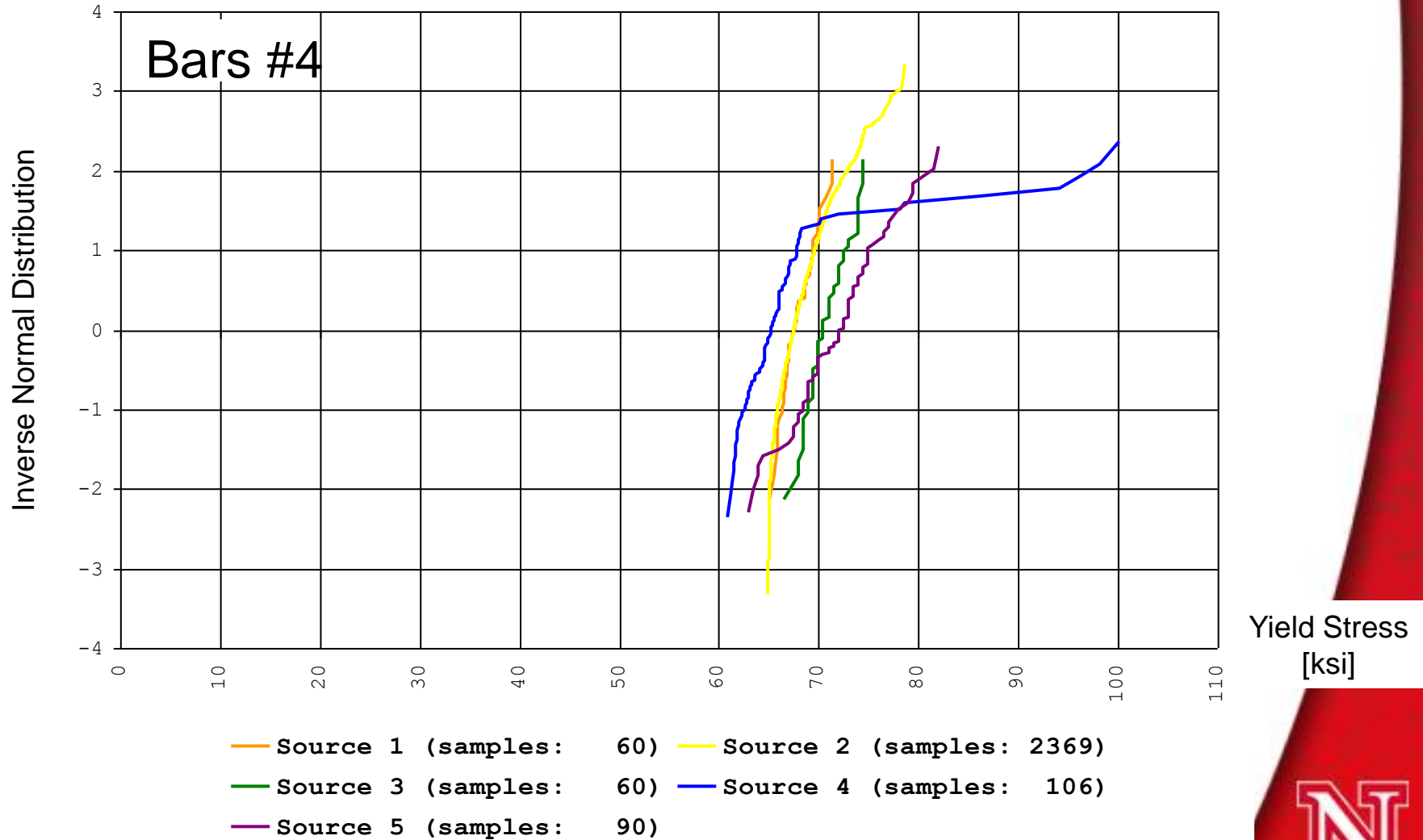
Reinforcing Steel Bars, Grade 60 – CDF of Yield Stress



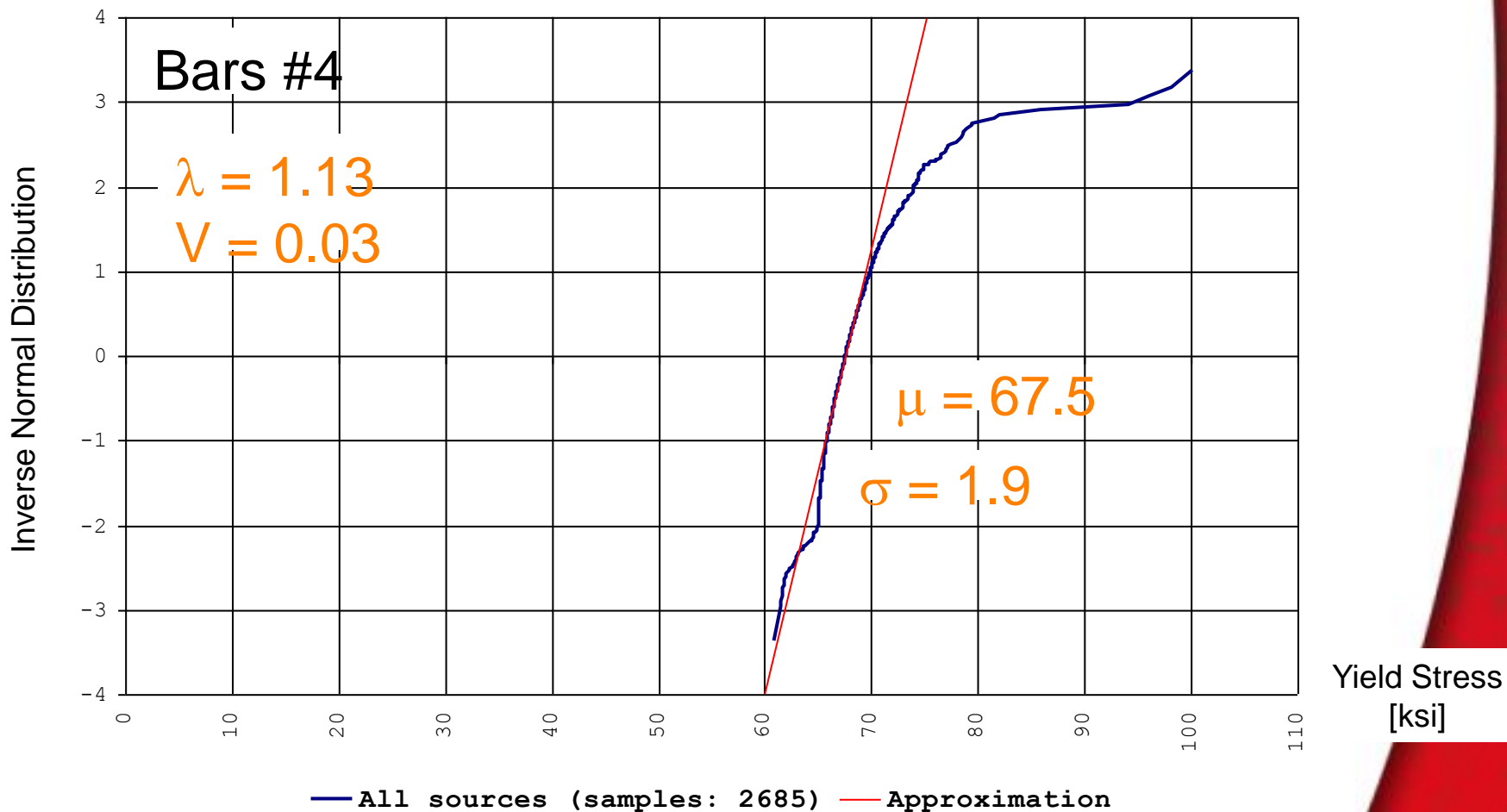
Reinforcing Steel Bars, Grade 60 – CDF of Yield Stress



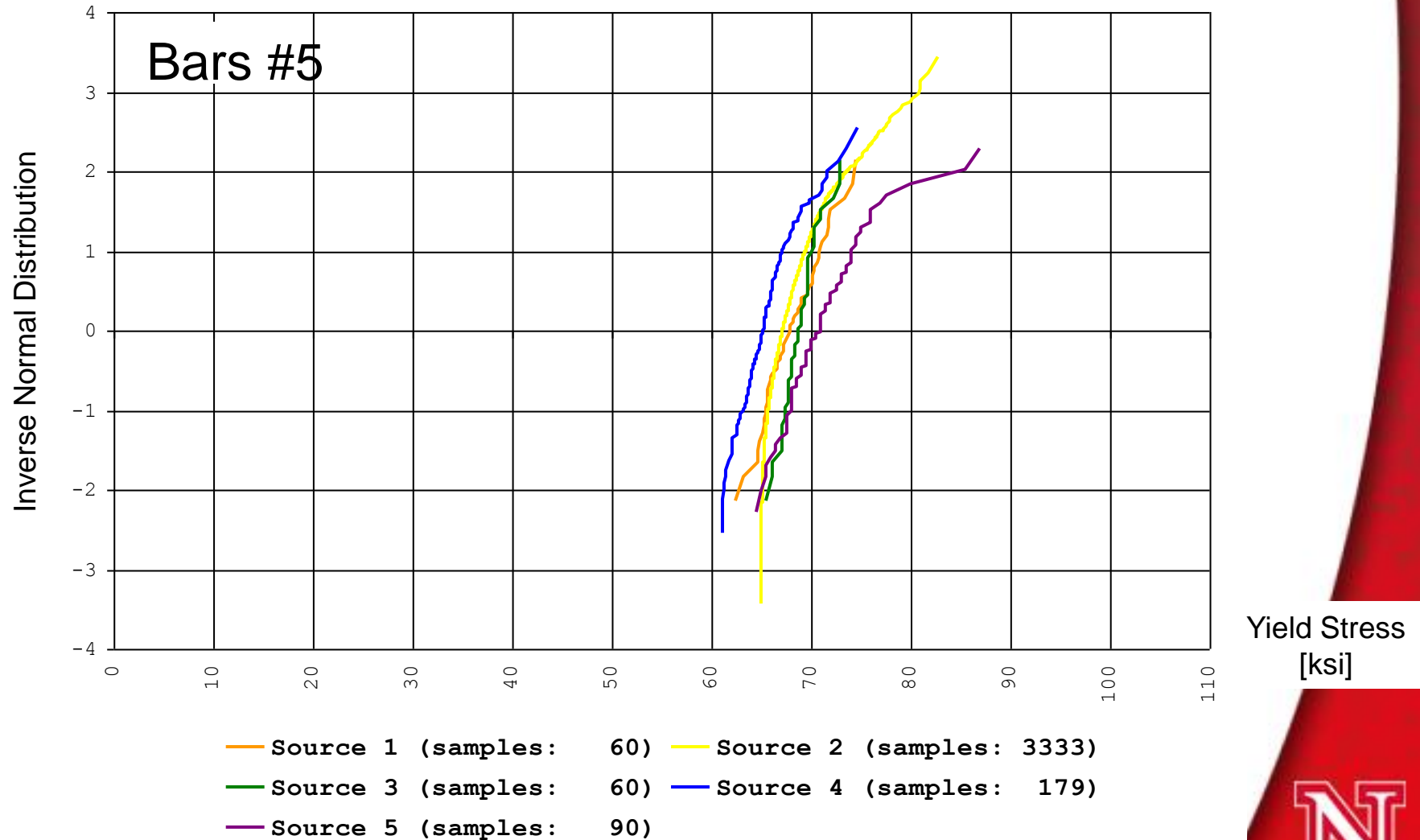
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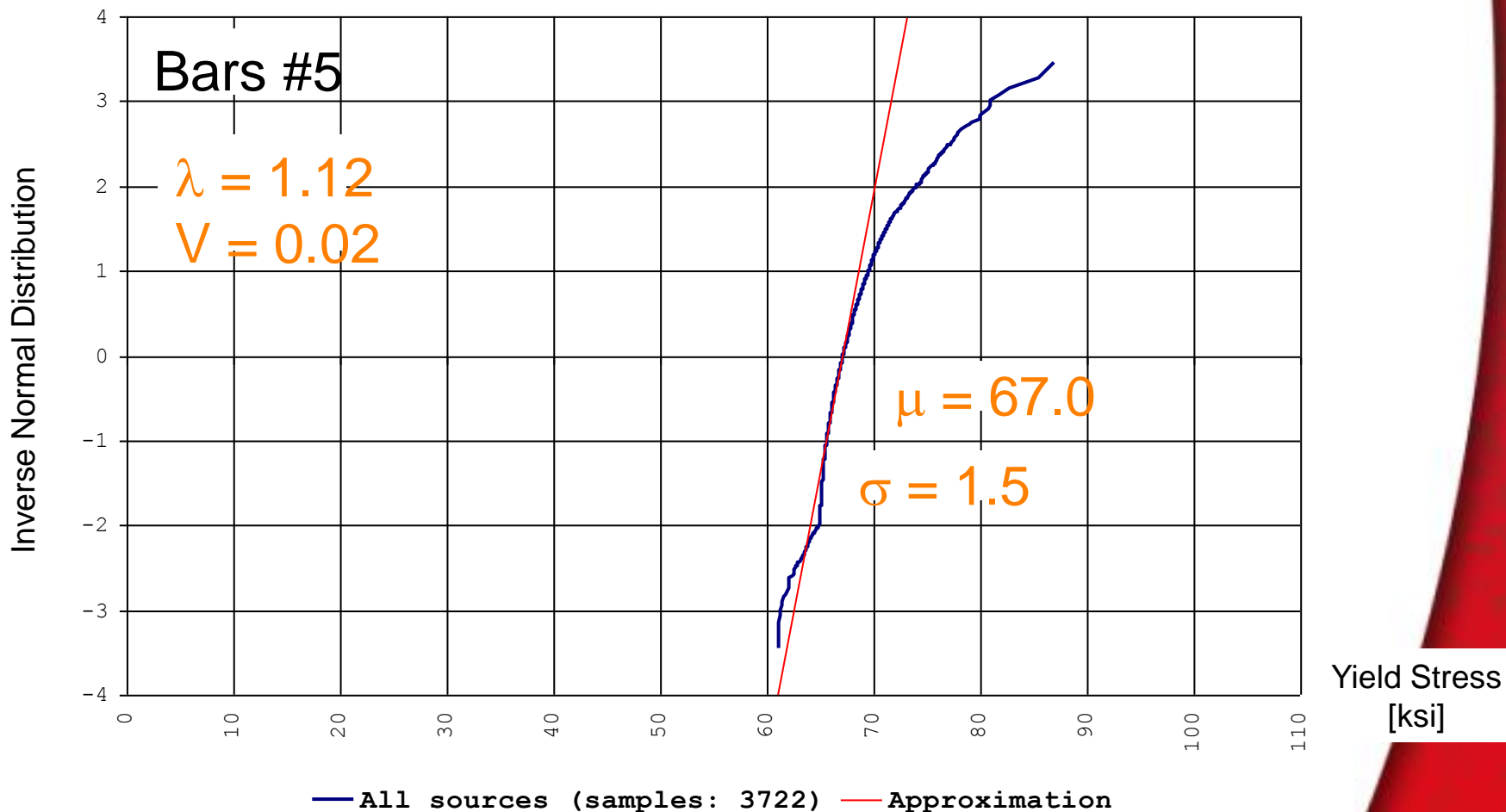
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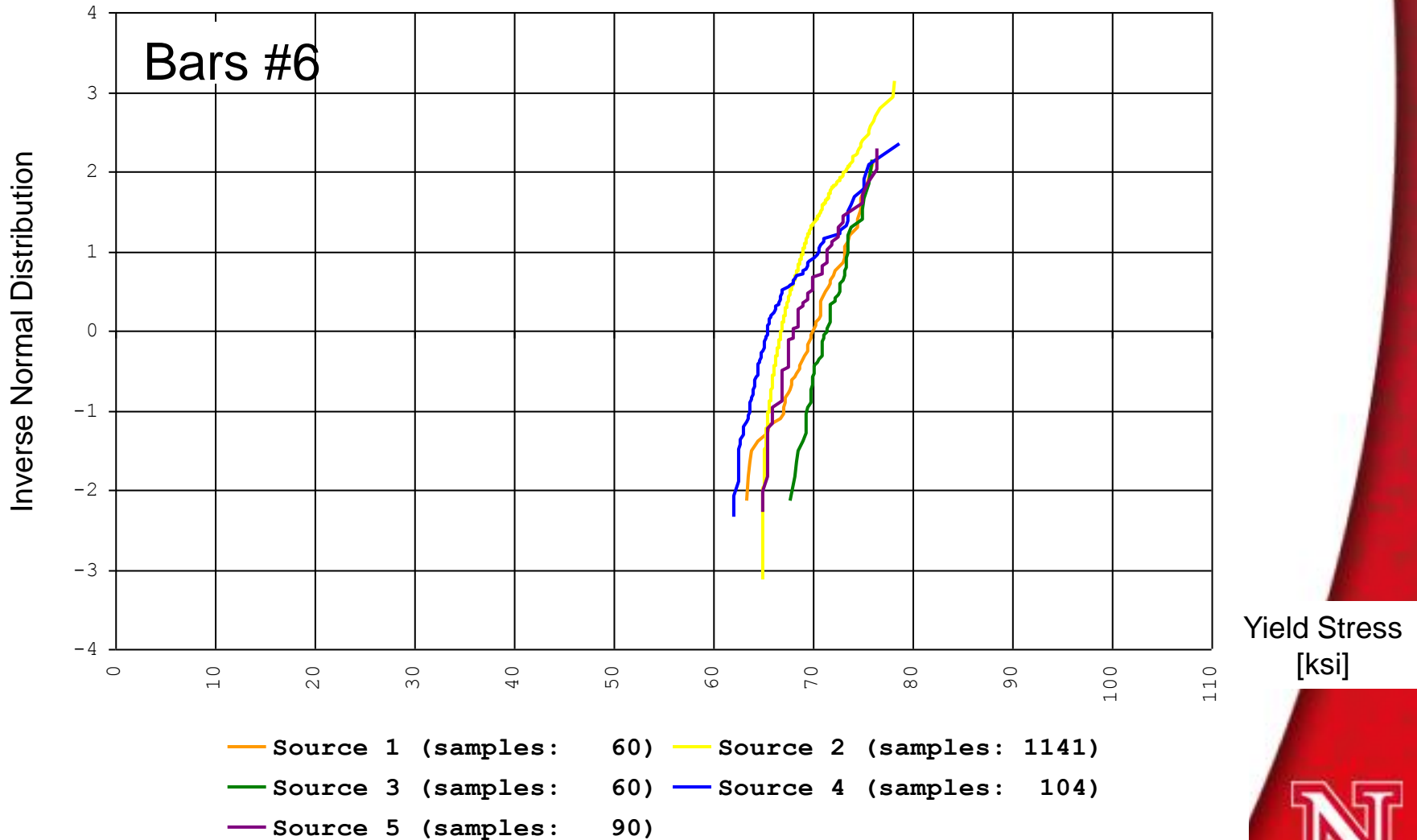
Reinforcing Steel Bars, Grade 60 – CDF of Yield Stress



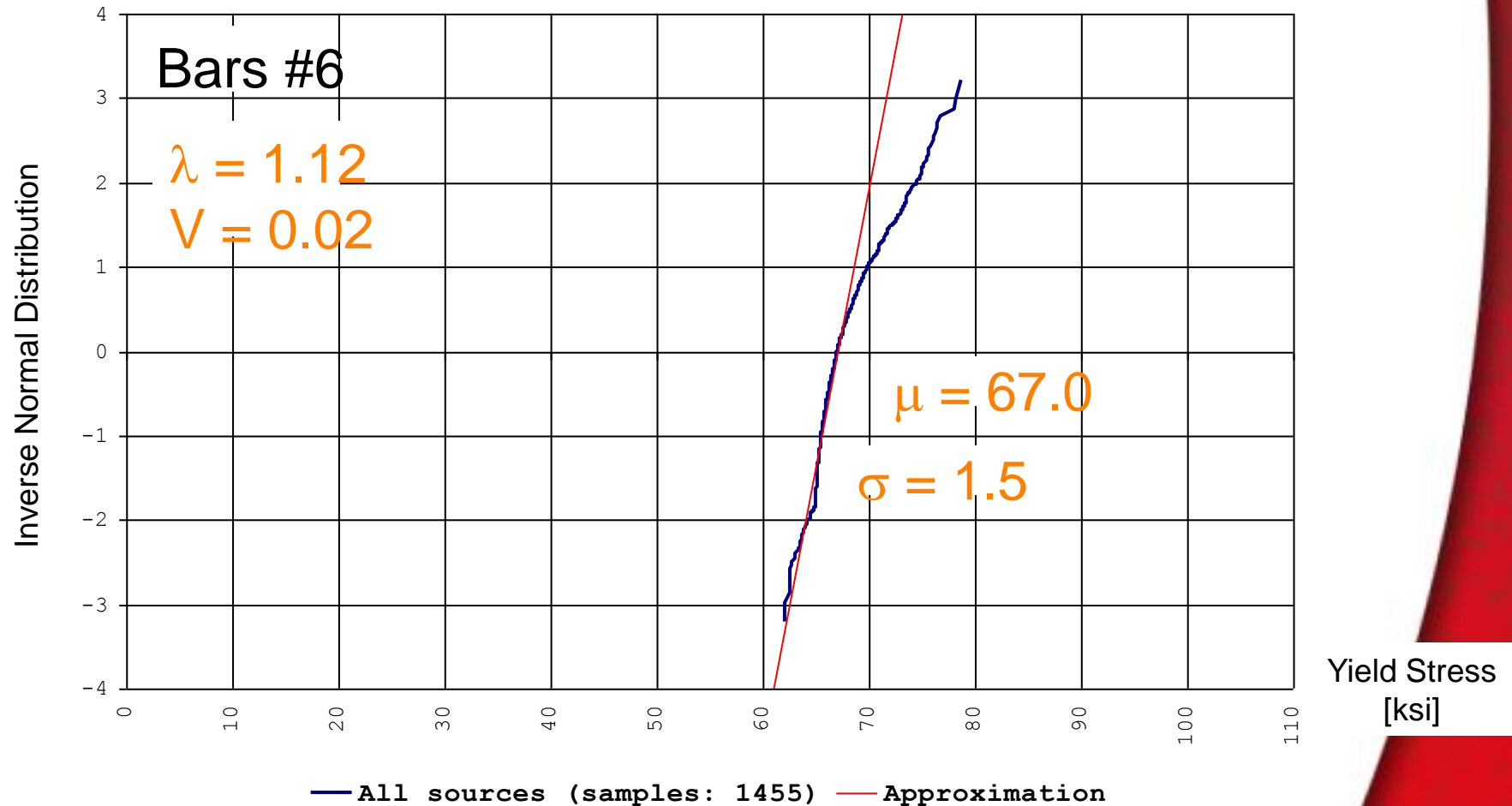
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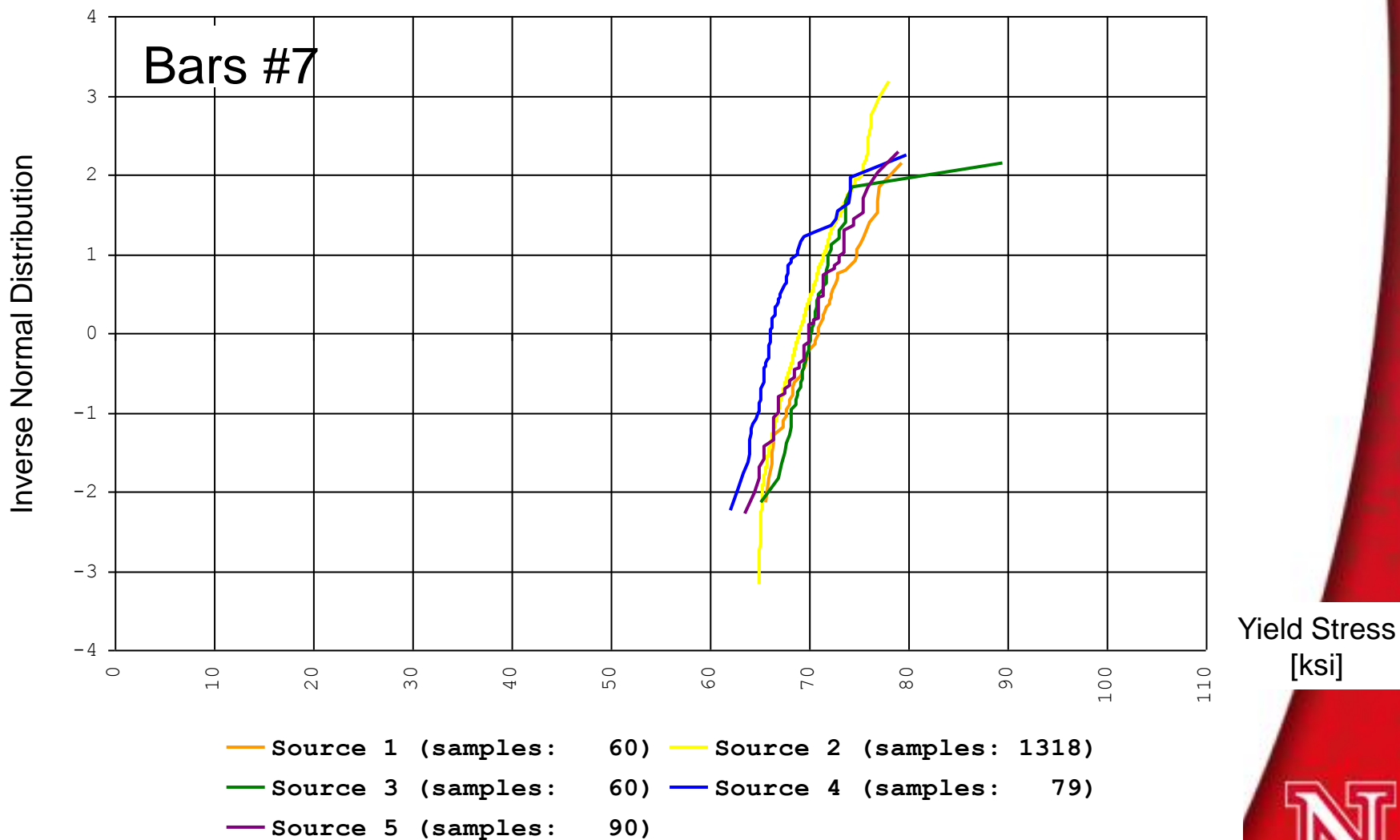
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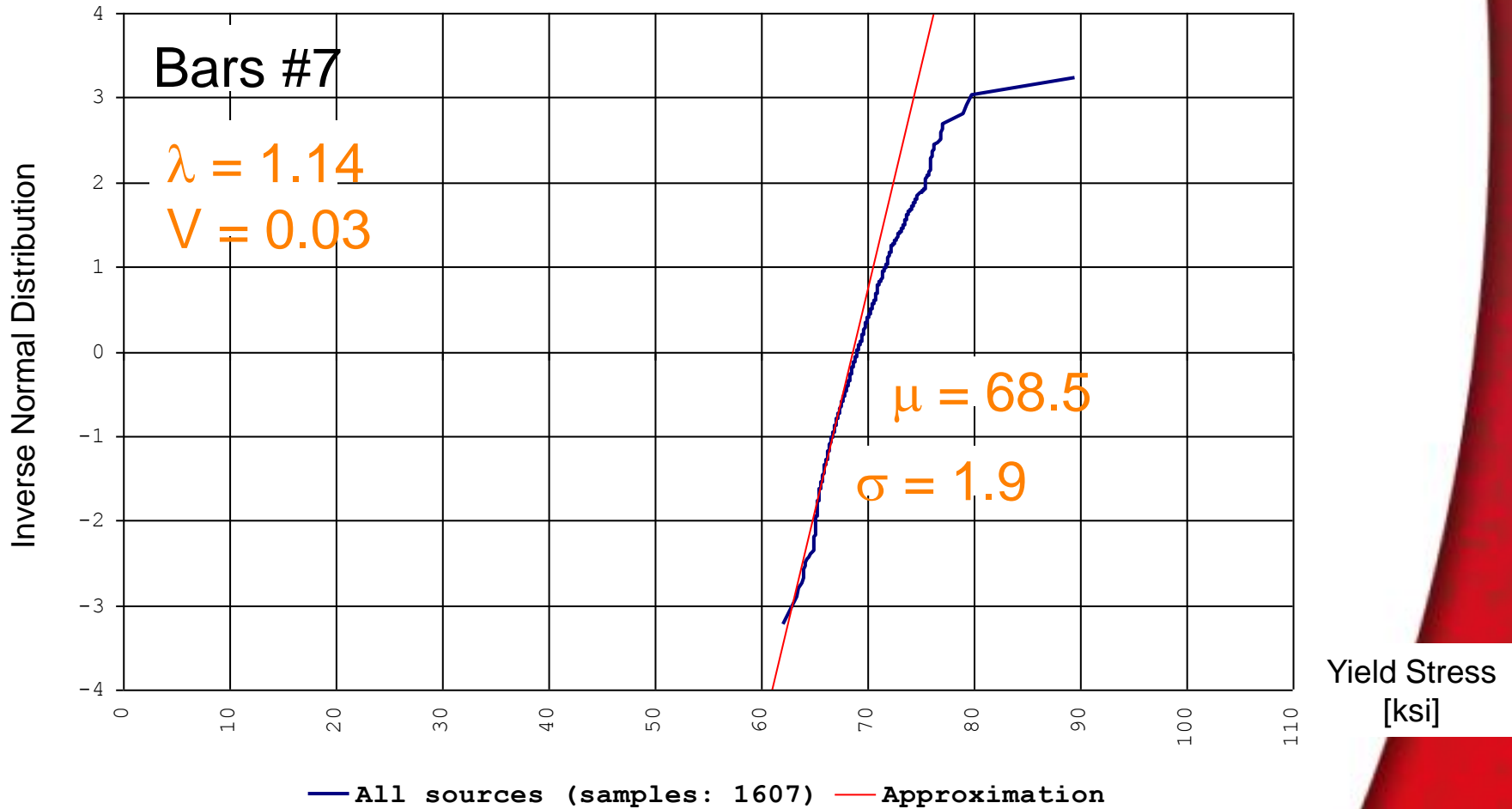
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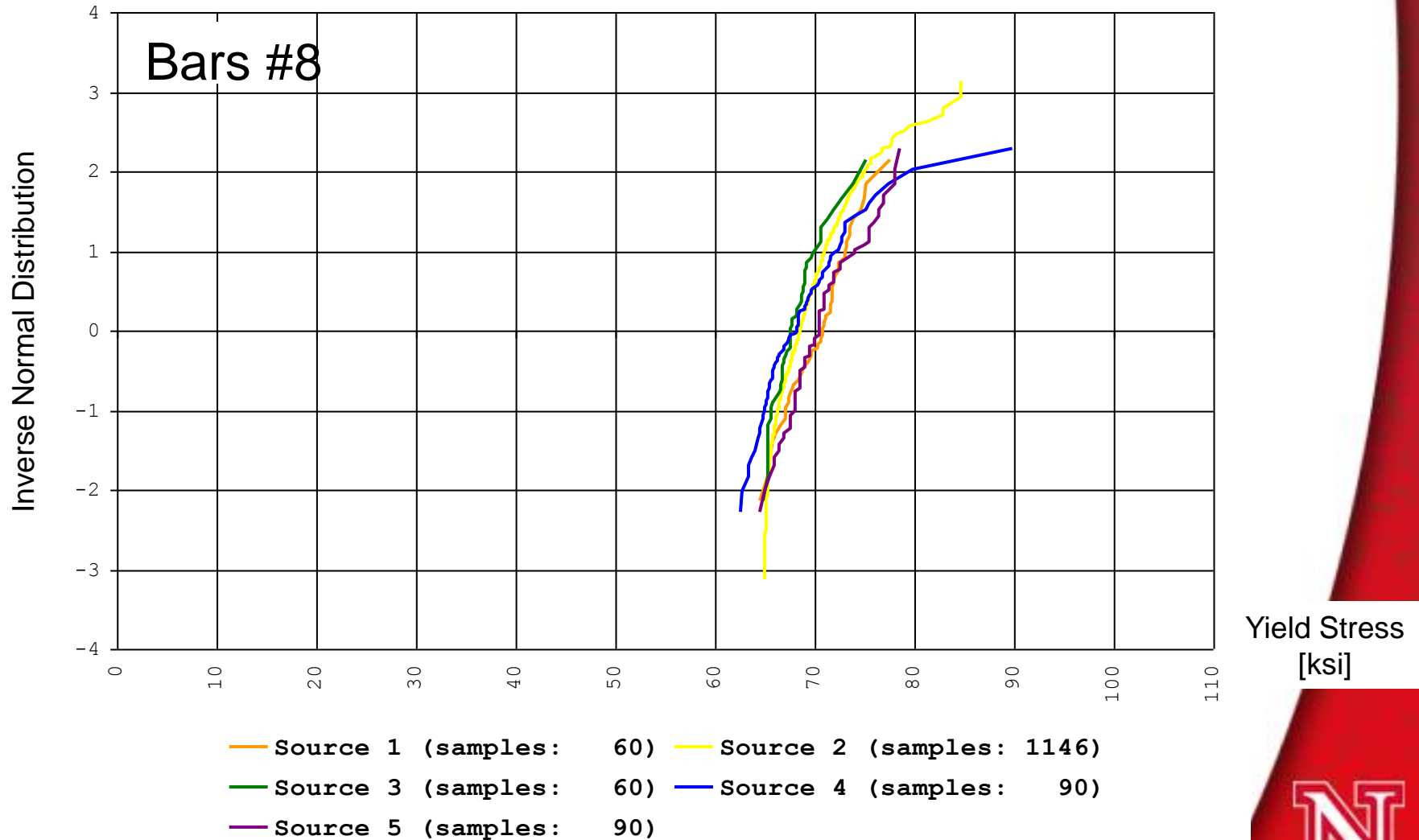
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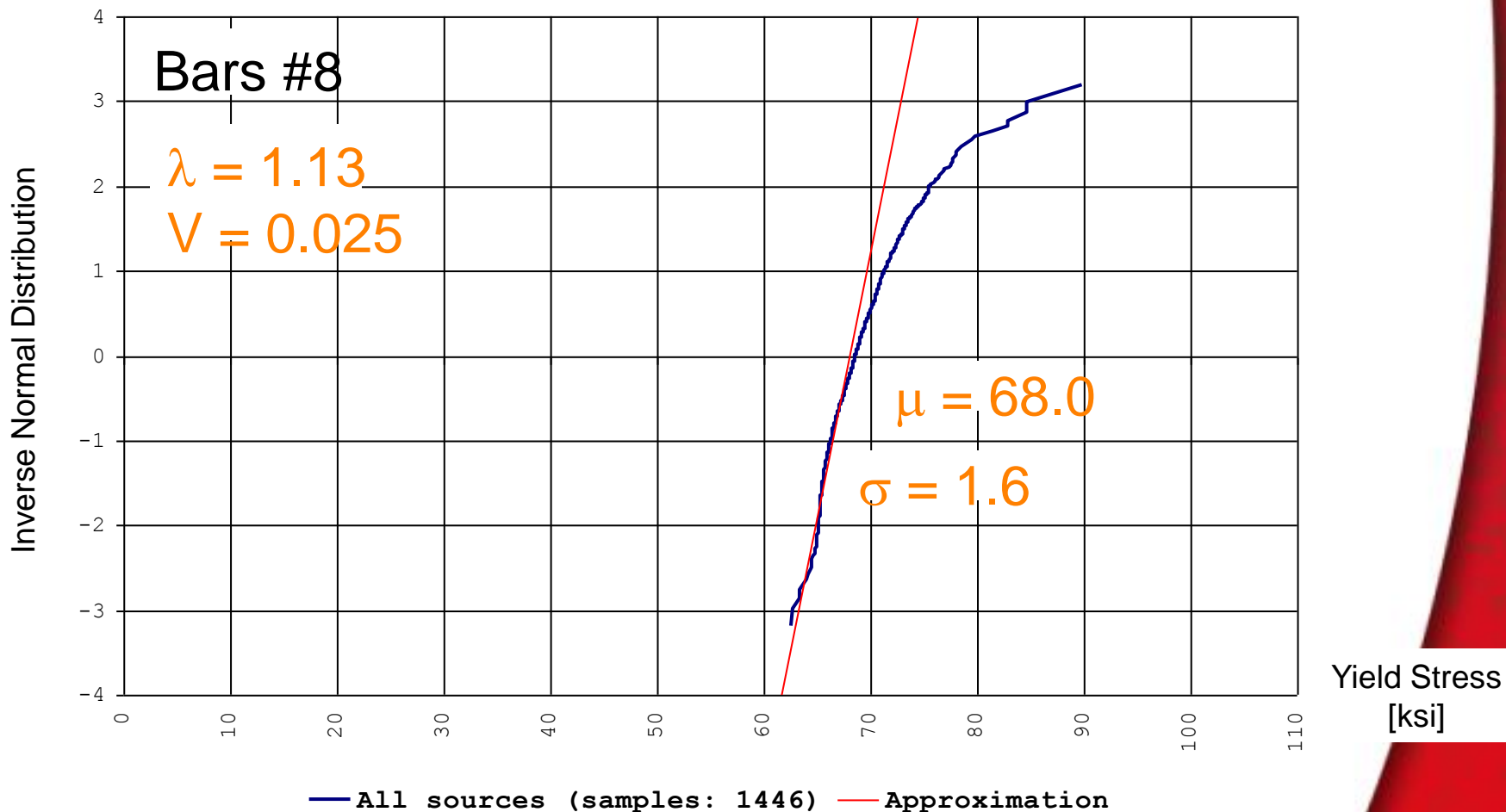
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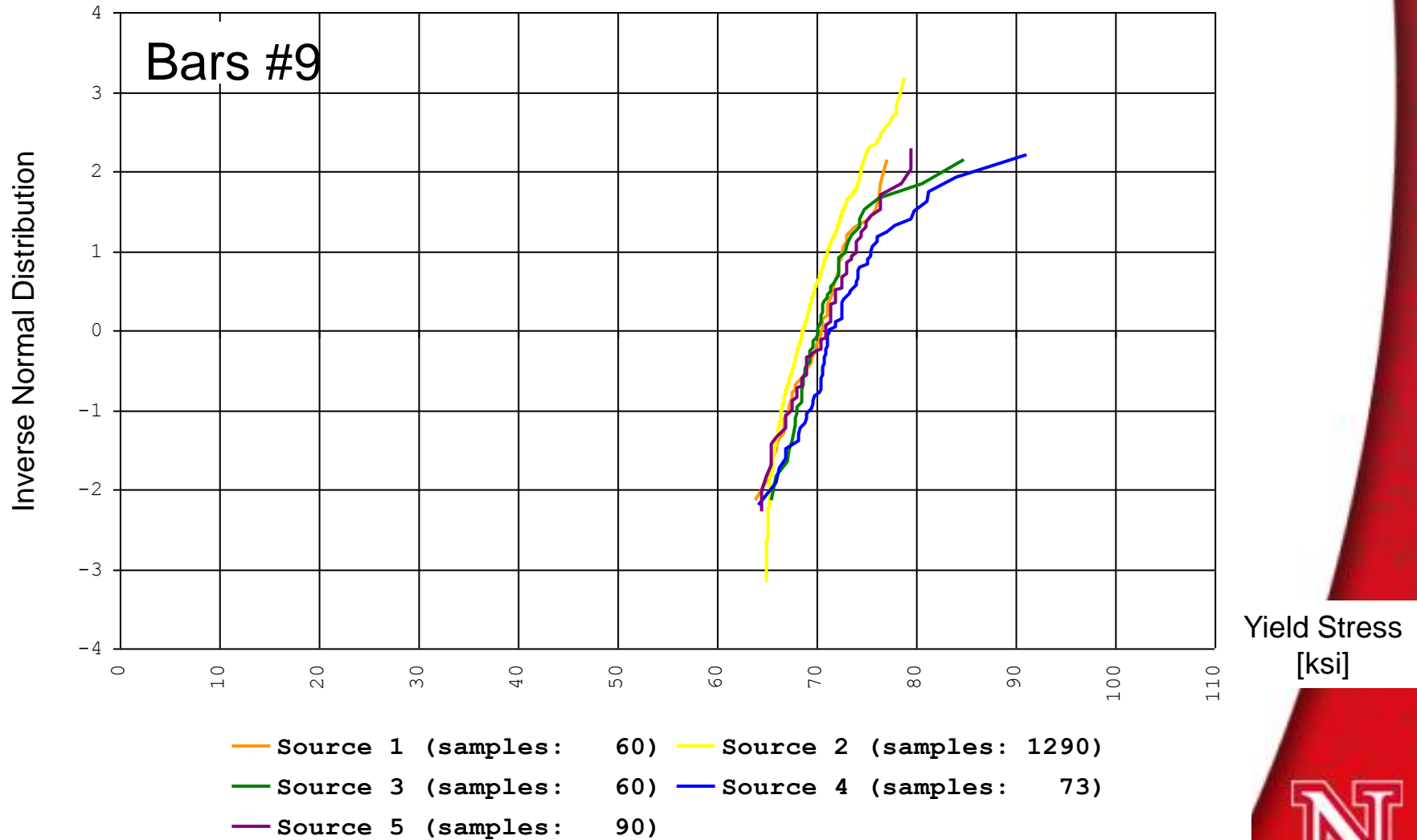
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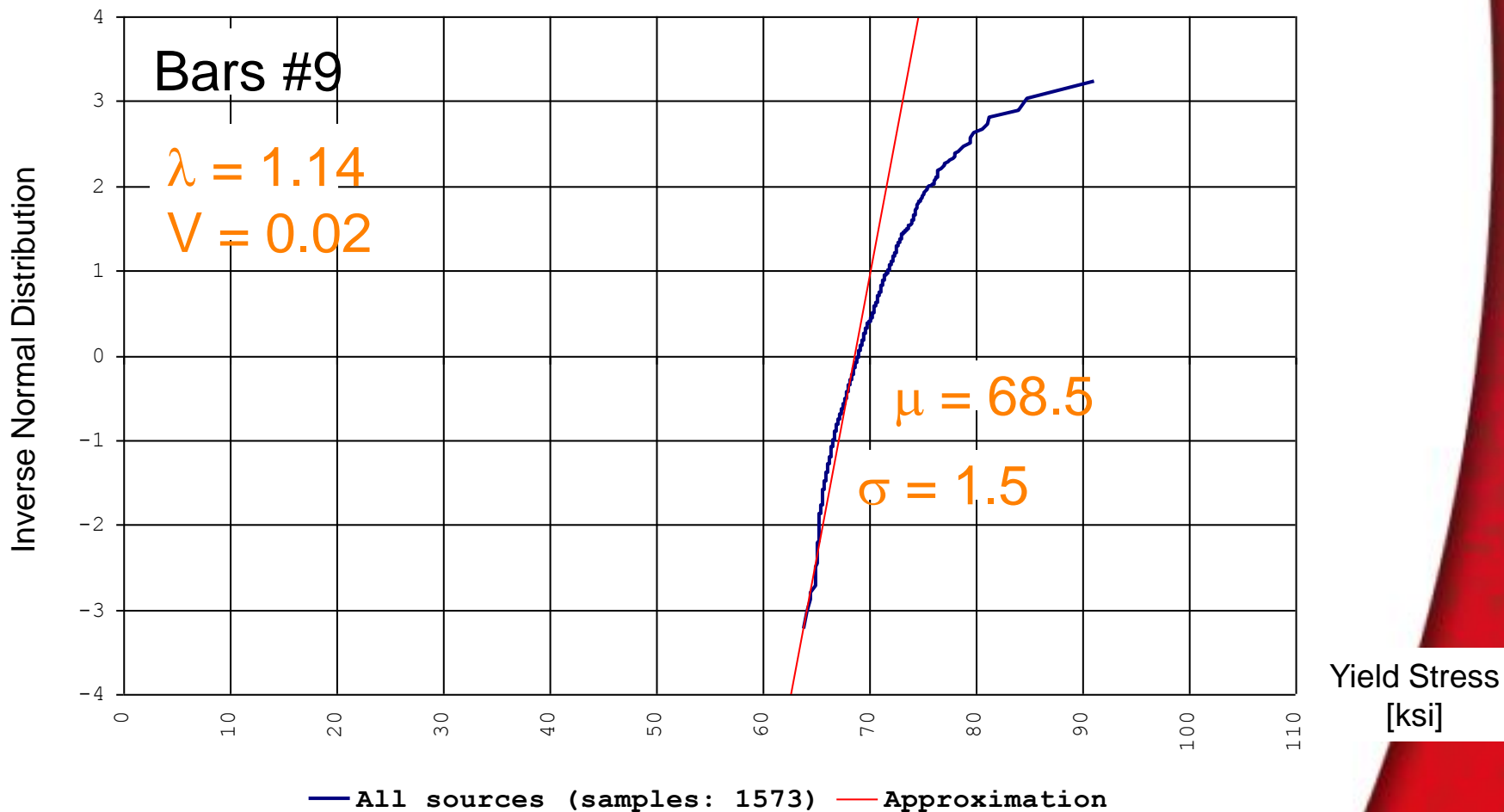
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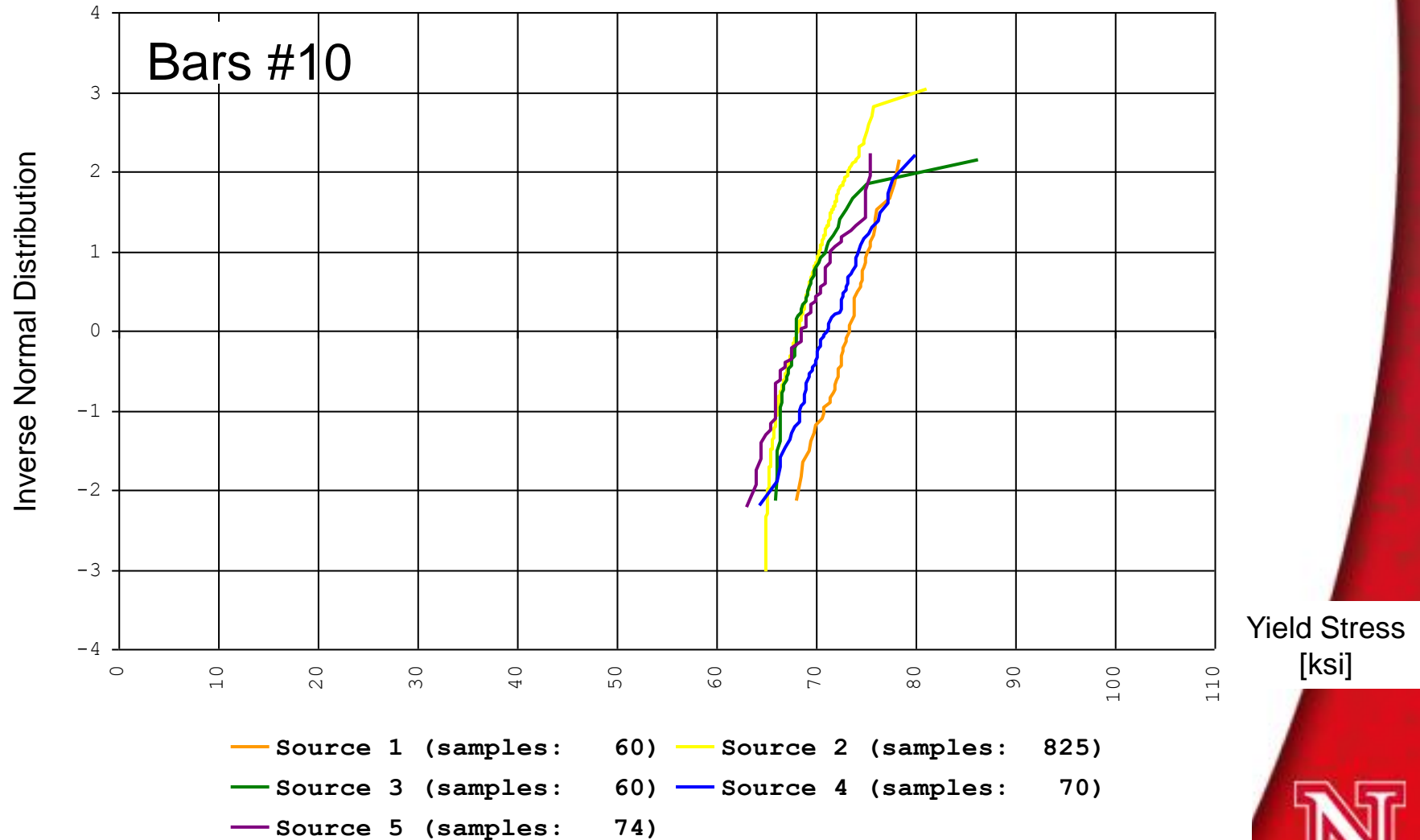
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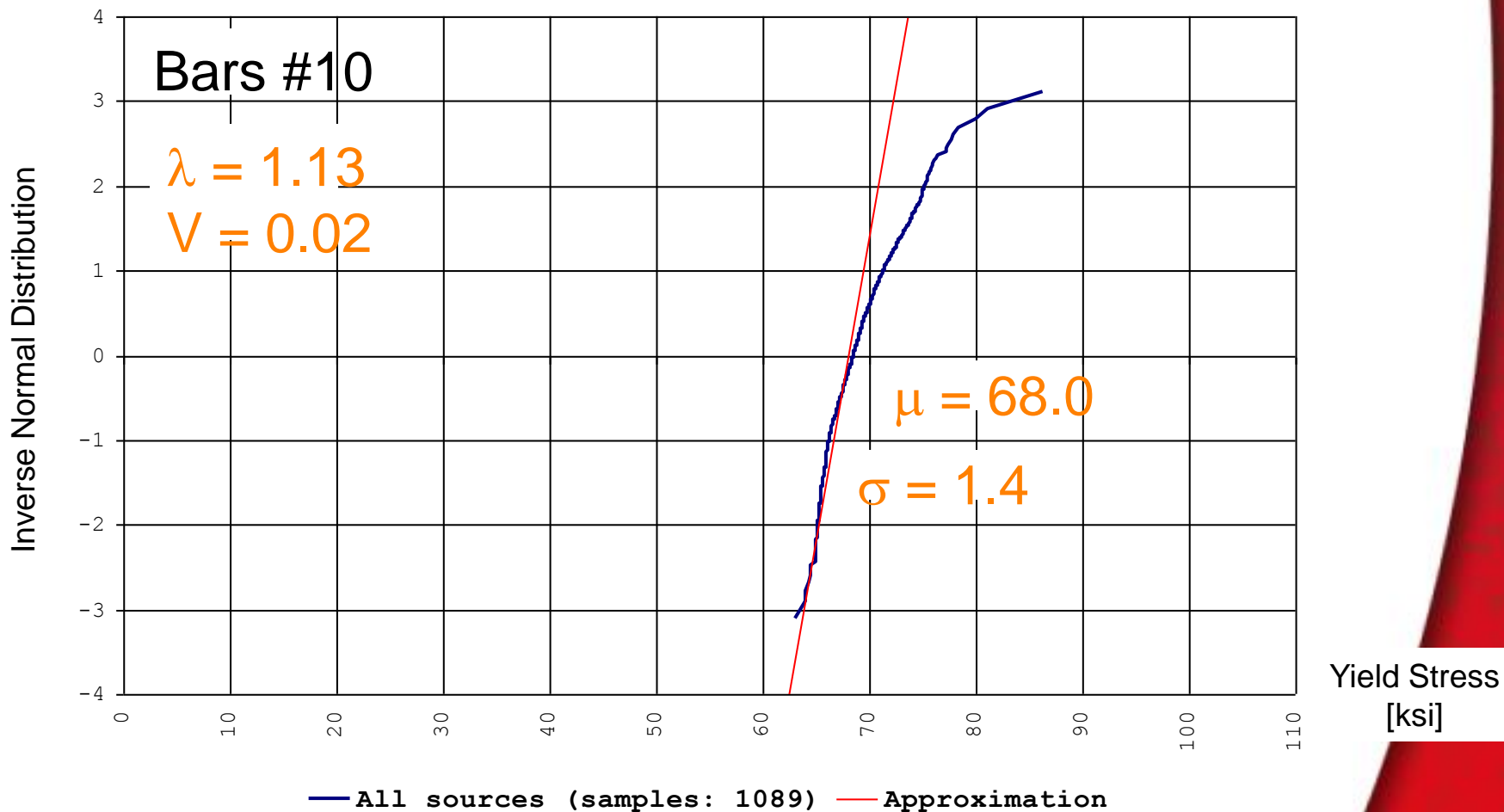
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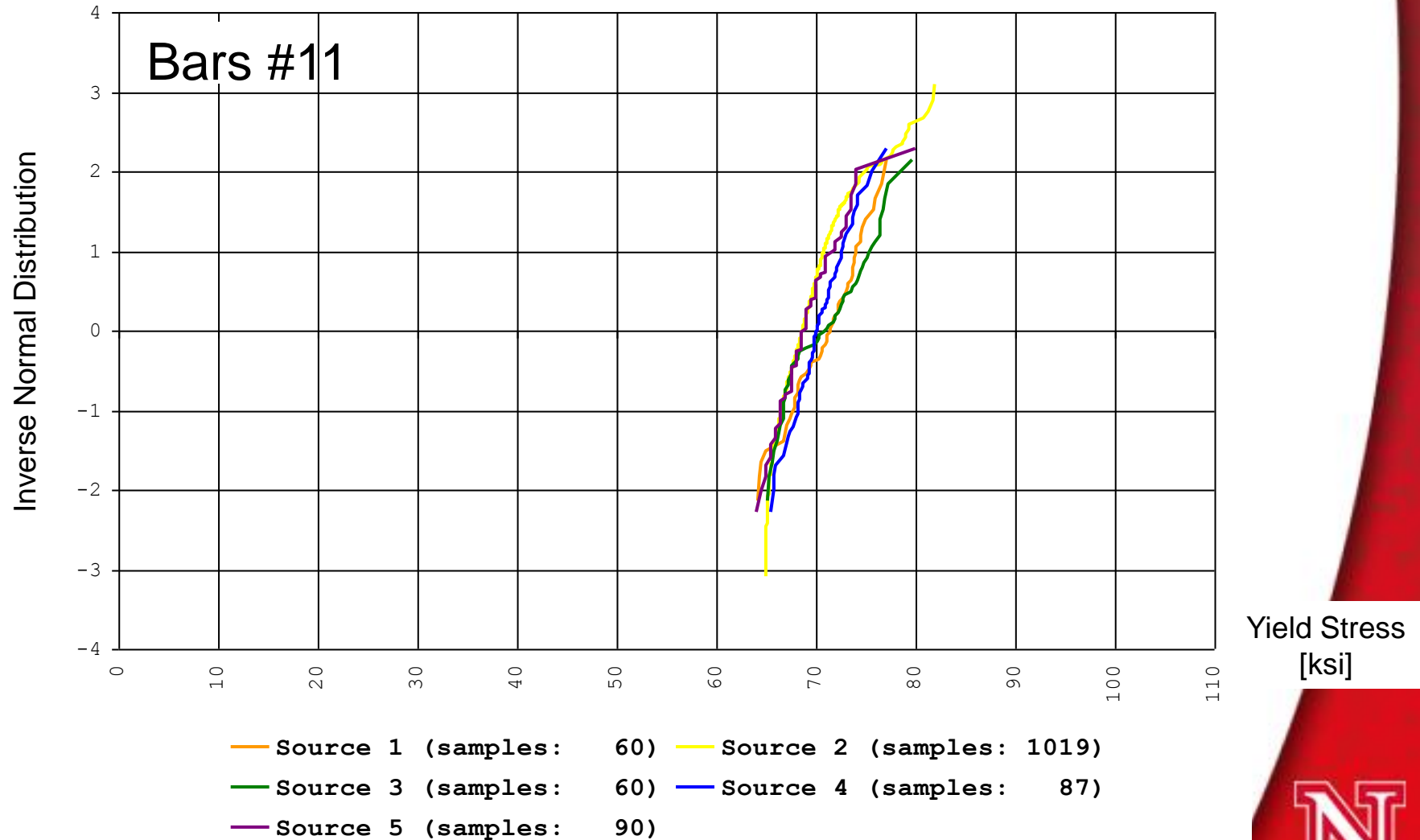
Reinforcing Steel Bars, Grade 60 – CDF of Yield Stress



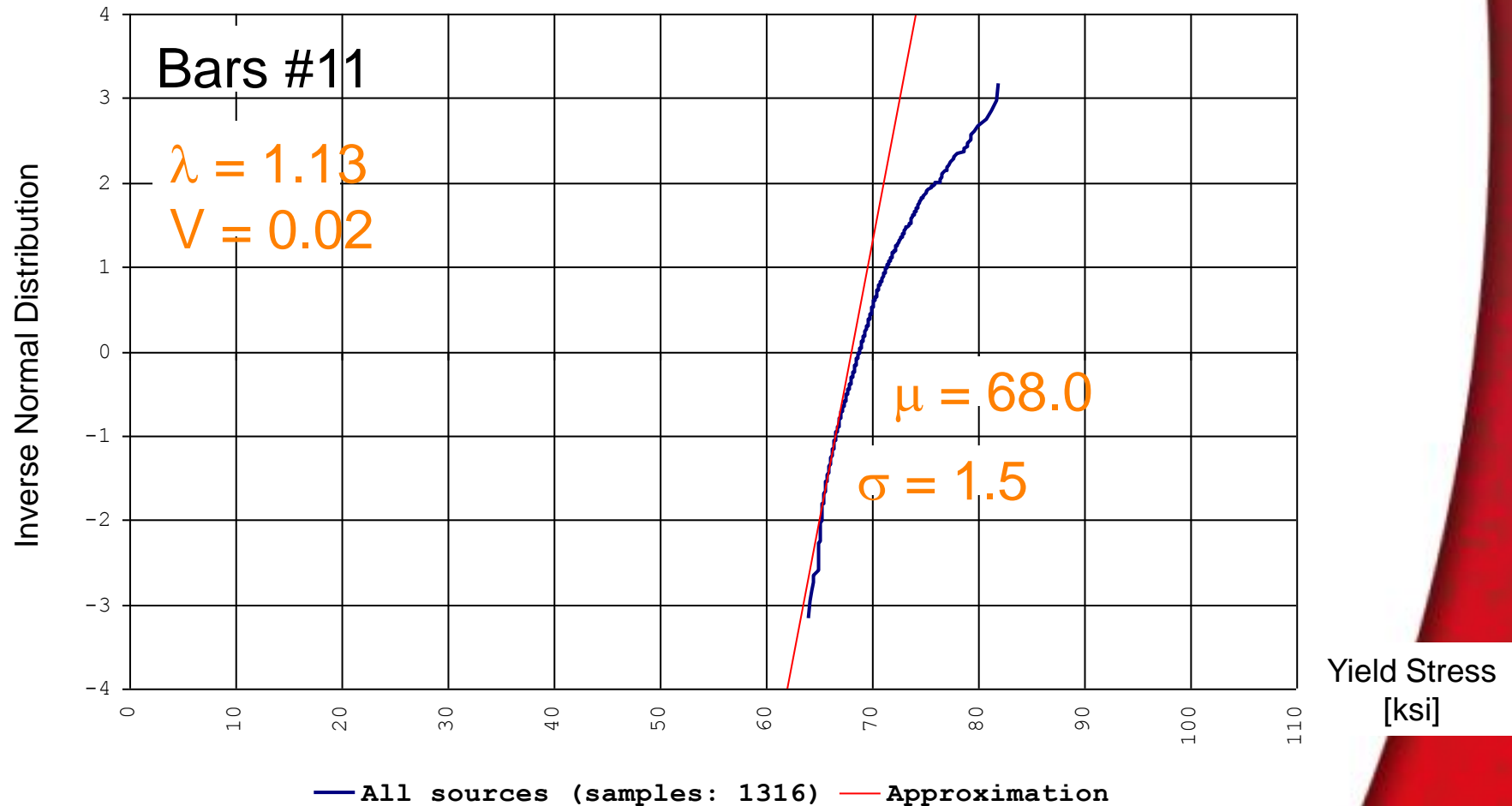
Reinforcing Steel Bars, Grade 60 – CDF of Yield Stress



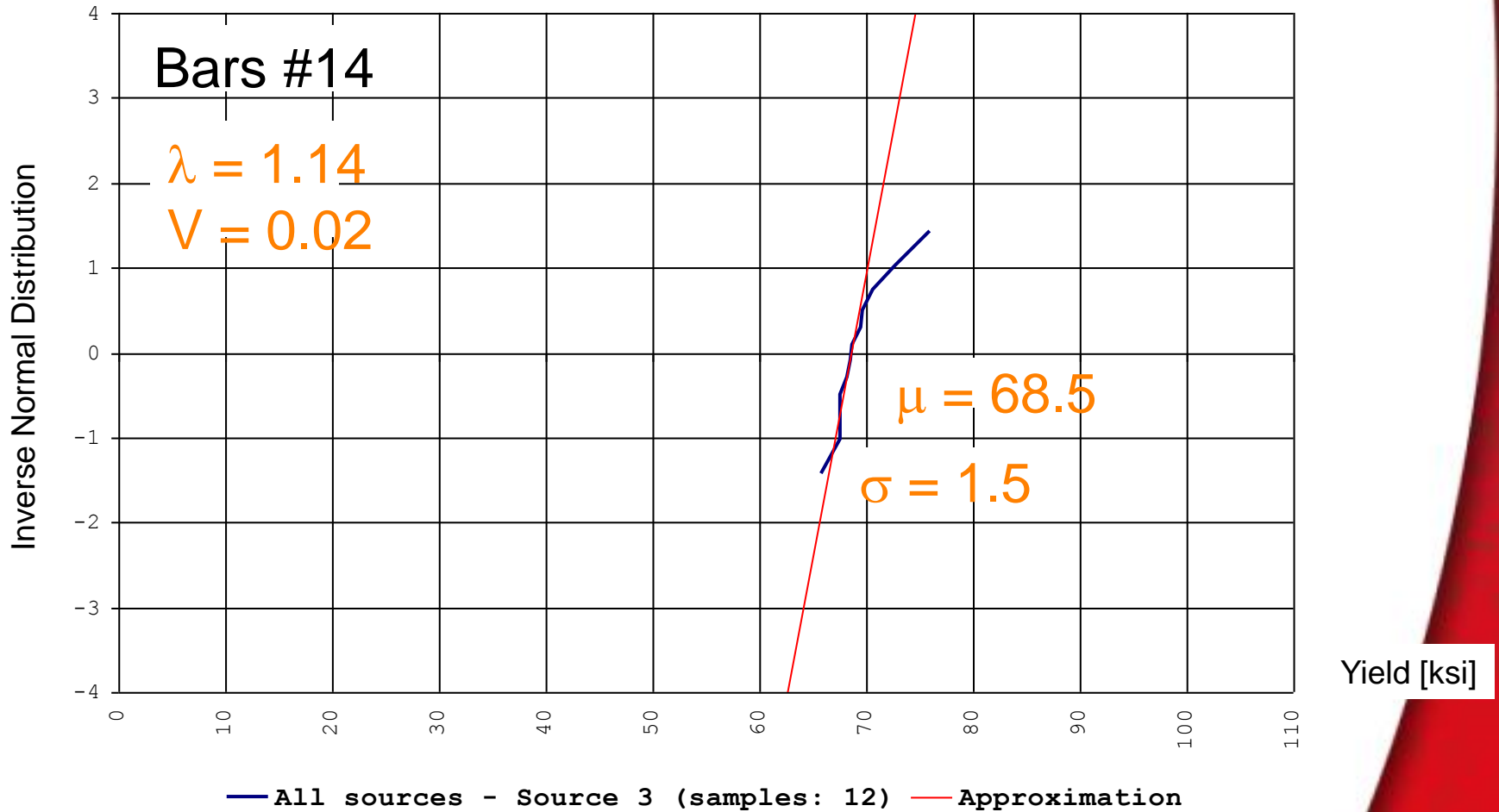
Reinforcing Steel Bars, Grade 60 – CDF of Yield Stress



Reinforcing Steel Bars, Grade 60 – CDF of Yield Stress

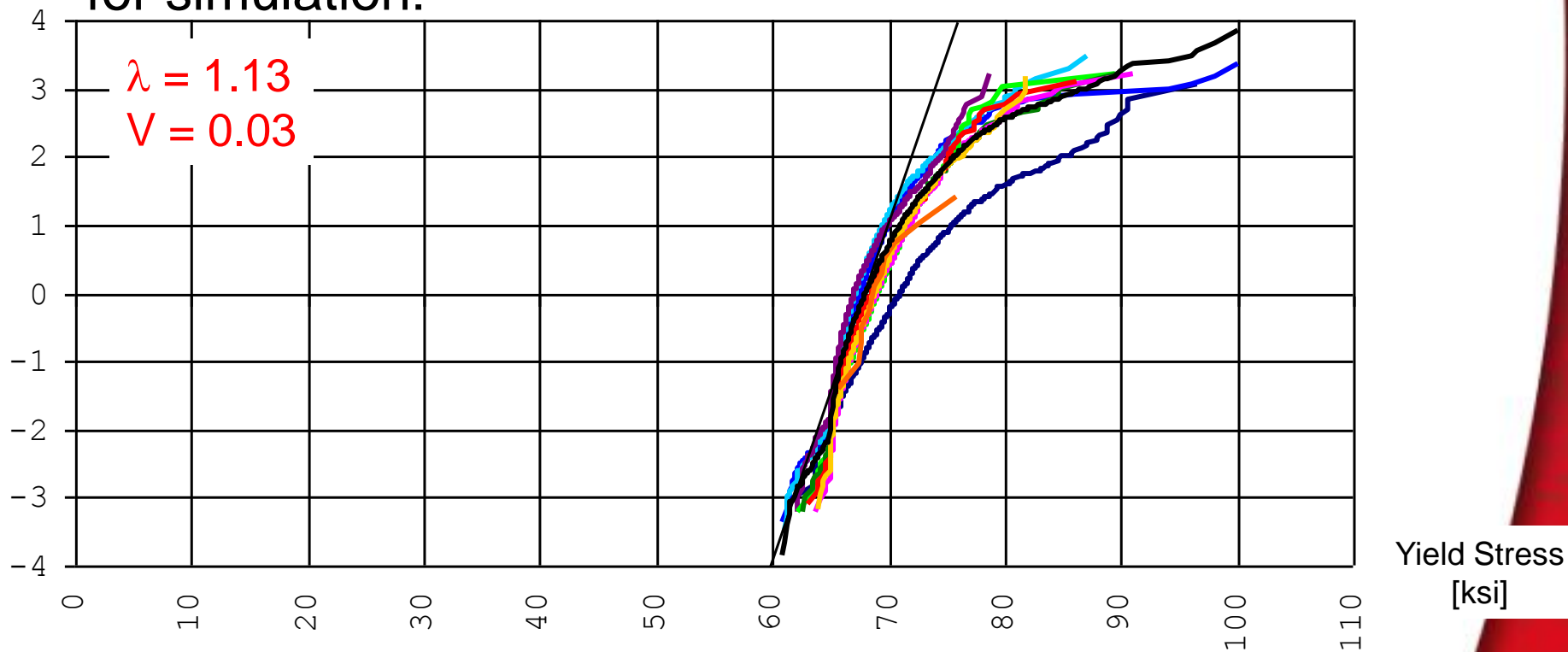


Reinforcing Steel Bars, Grade 60 – CDF of Yield Stress



Reinforcing Steel Bars, Grade 60 – CDF of Yield Stress

for simulation:



Reinforcing Steel Bars, Grade 60 (420 MPa) – Statistical Parameters

Bar Size	λ	V
# 3	1.18	0.04
# 4	1.13	0.03
# 5	1.12	0.02
# 6	1.12	0.02
# 7	1.14	0.03
# 8	1.13	0.025
# 9	1.14	0.02
#10	1.13	0.02
#11	1.13	0.02
#14	1.14	0.02



Prestressing Strands Grade 270 (1800 MPa) – Number of Samples

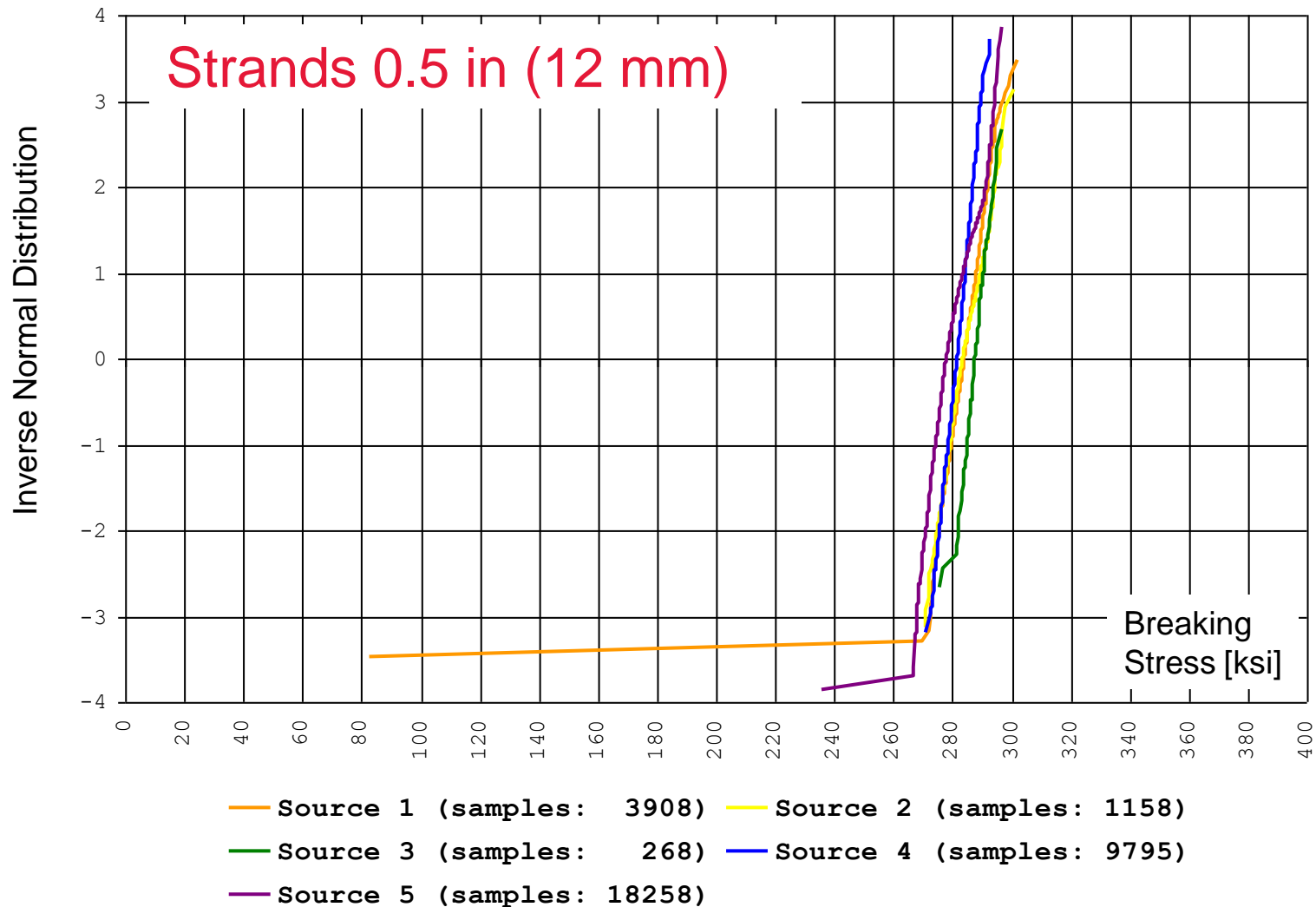
Source	Strand diameter	Number of samples	
		0.5in	0.6in
	Source 1	3,908	700
	Source 2	1,158	785
	Source 3	268	212
	Source 4	9,795	3,442
	Source 5	18,258	8,895
	Total	33,387	14,034

Total Number of Samples 47,421



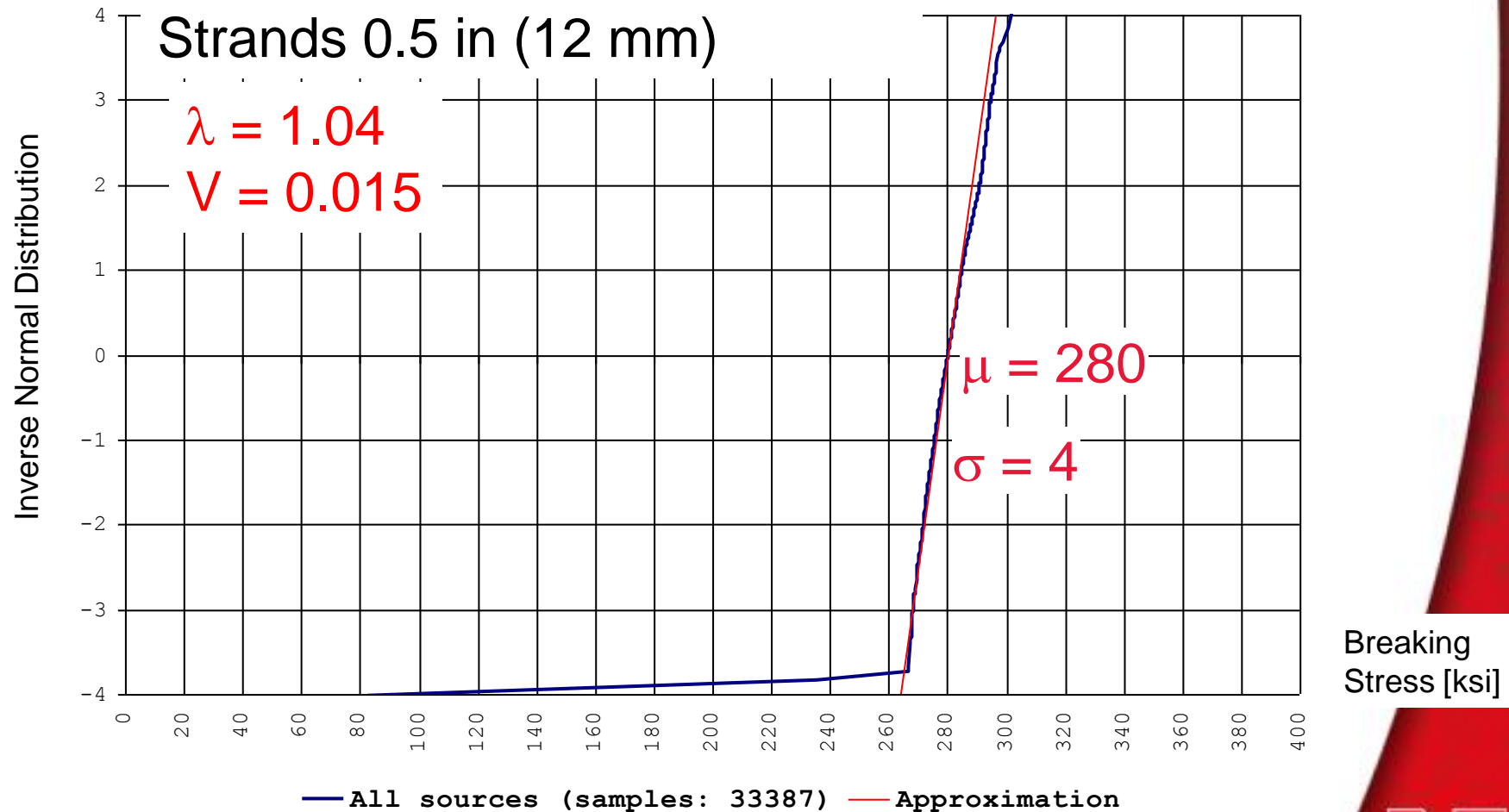
Prestressing Steel (7-wire strands), Grade 270

CDF of Breaking Stress



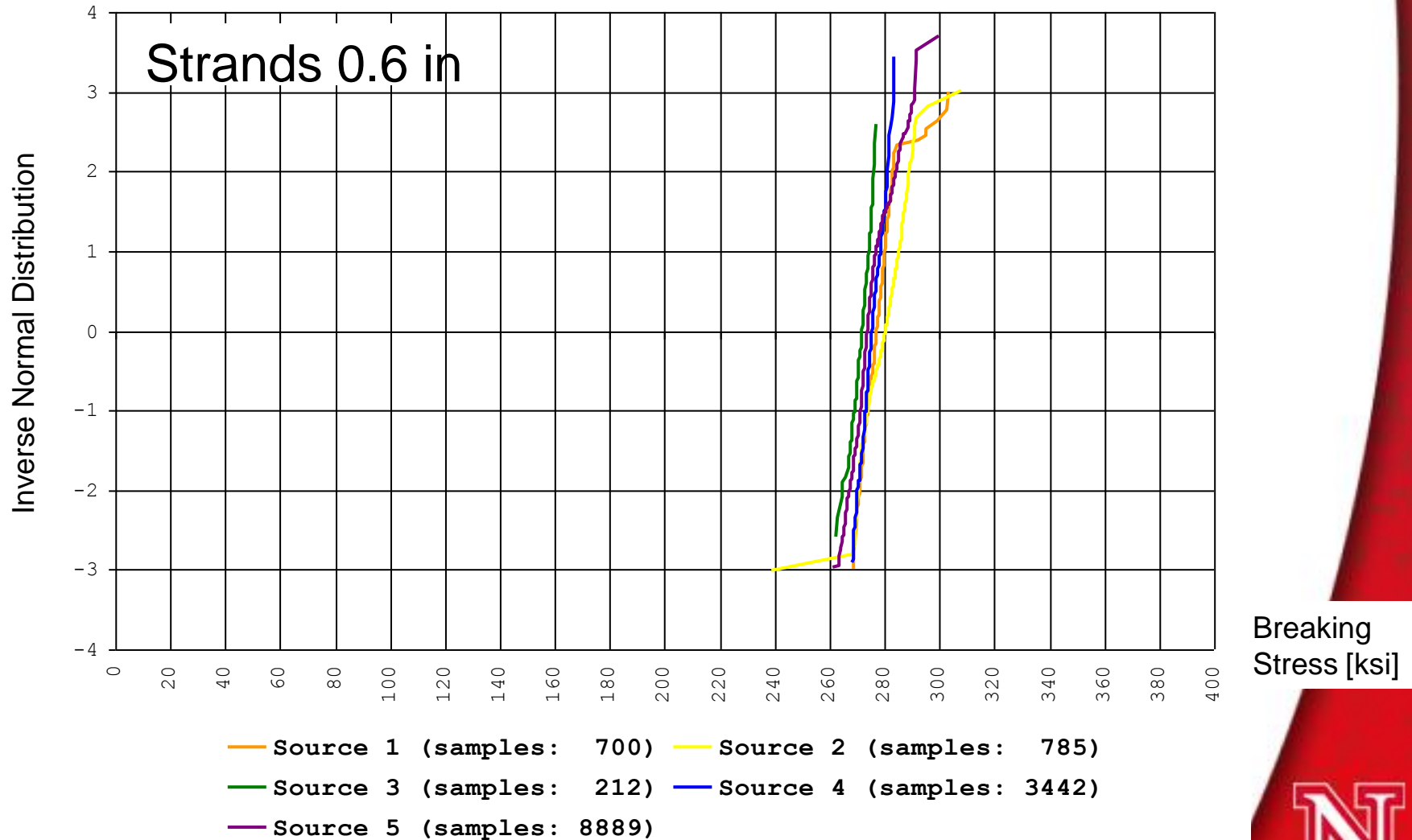
Prestressing Steel (7-wire strands), Grade 270

CDF of Breaking Stress



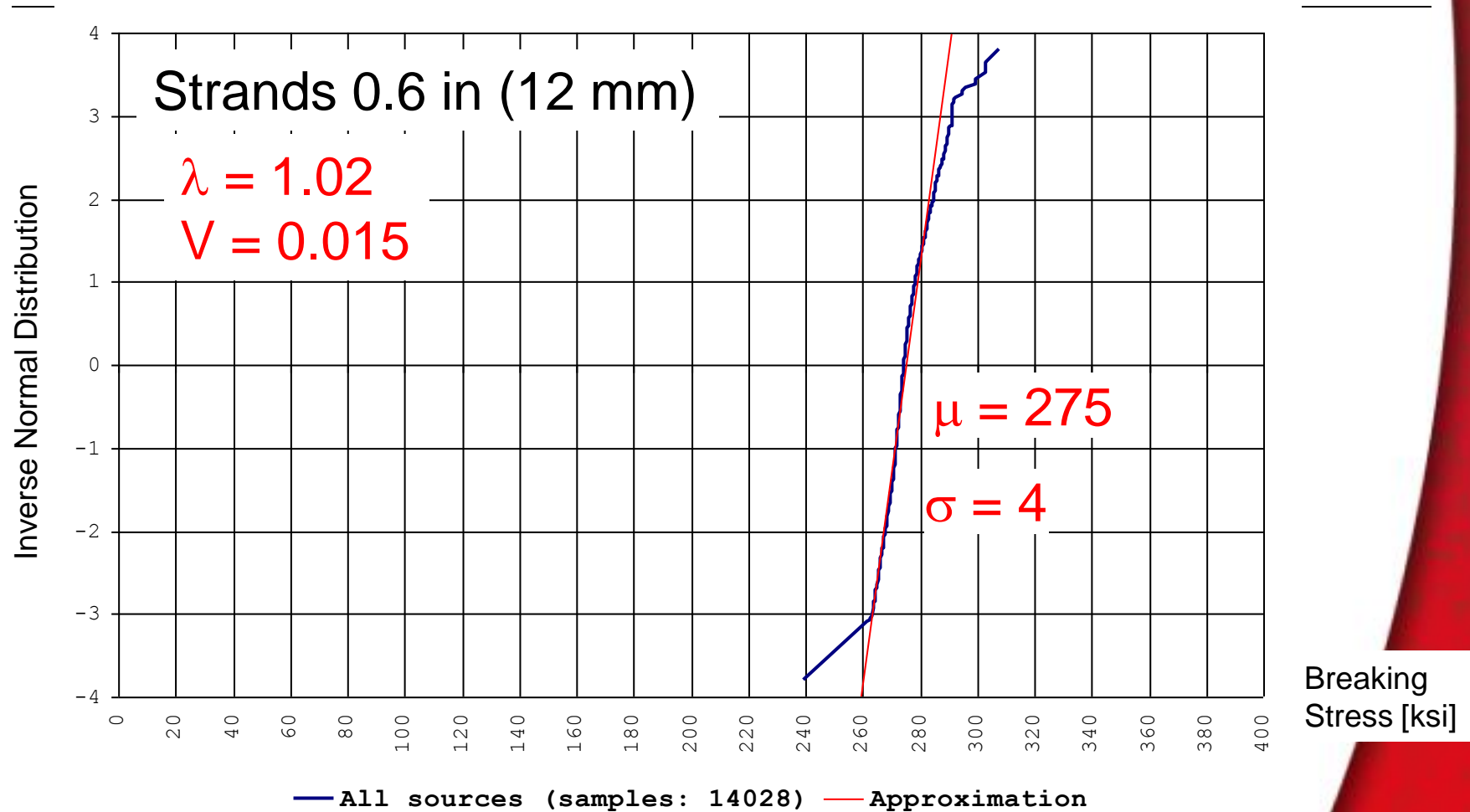
Prestressing Steel (7-wire strands), Grade 270

CDF of Breaking Stress



Prestressing Steel (7-wire strands), Grade 270

CDF of Breaking Stress



Prestressing Steel – Statistical Parameters

Grade	Size	Number of samples	Bias Factor	v
250 ksi (1750 MPa)	1/4 (6.25 mm)	22	1.07	0.01
	3/8 (9.5 mm)	83	1.11	0.025
	7/16(11 mm)	114	1.11	0.01
	1/2 (12.5 mm)	66	1.12	0.02
270 ksi (1900 MPa)	3/8 (9.5 mm)	54	1.04	0.02
	7/16 (11 mm)	16	1.07	0.02
	1/2 (12.5 mm)	33570	1.04	0.015
	0.6 (15 mm)	14028	1.02	0.015



Structural elements and limit states

- Reinforced concrete beams - flexure
- Reinforced concrete beams - shear (w/o stirrups)
- Reinforced concrete beams - shear (with stirrups)
- Axially loaded columns, tied
- Axially loaded columns, spiral
- One way slabs - flexure
- One way slabs - shear
- Two way slabs – shear
- Bearing strength



Bending Moment Resistance

$$R = (A_s \times f_y) \left(d - \frac{a}{2} \right)$$

$$a = \frac{A_s \cdot f_y}{0.85 f'_c \cdot b}$$

for beams $\rho = 0.6$ and 1.6% ,
for slabs $\rho = 0.30\%$.

Shear Resistance of Flexural Members

$$R = V_n = V_c + V_s$$

$$V_c = 2\sqrt{f'_c} b_w \cdot d$$

$$V_s = \frac{A_v \cdot f_y \cdot d}{S}$$

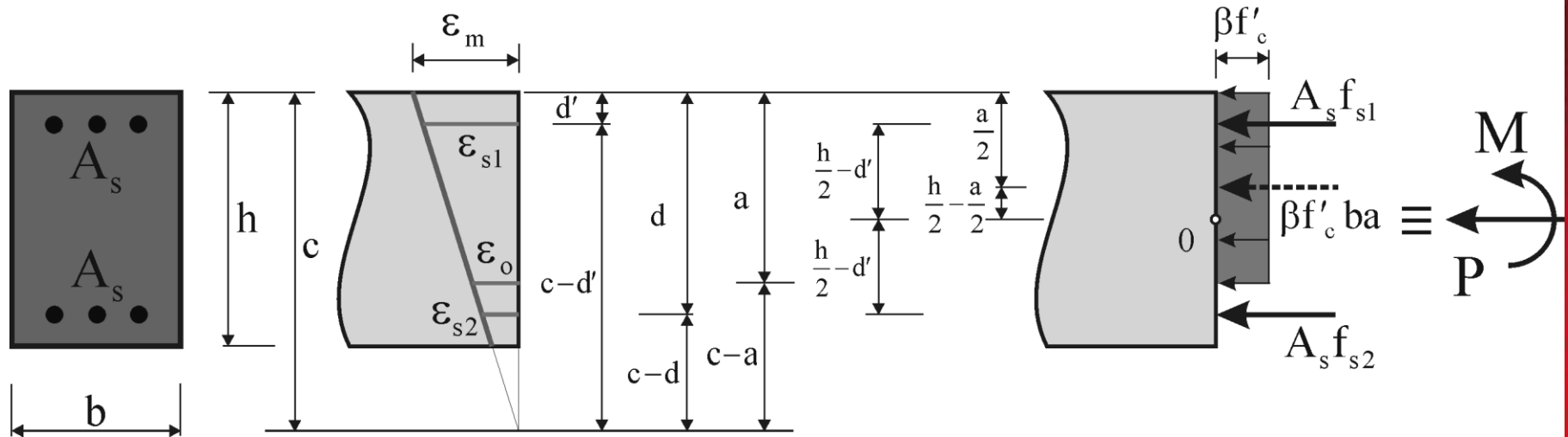
Shear Resistance of Slabs in Two-Way Shear

$$R = \min \left\{ \left(1 + \frac{2}{\beta_c} \right) \cdot 2\sqrt{f'_c} b_0 d, \left(\frac{\alpha_s d}{2b_0} + 1 \right) \cdot 2\sqrt{f'_c} b_0 d, 4 \cdot \sqrt{f'_c} b_0 d \right\}$$

$$\left(\sqrt{f'_c} \right)_{\text{simulations}} = 0.95 \left(\sqrt{f'_c} \right)_{\text{nominal}}$$

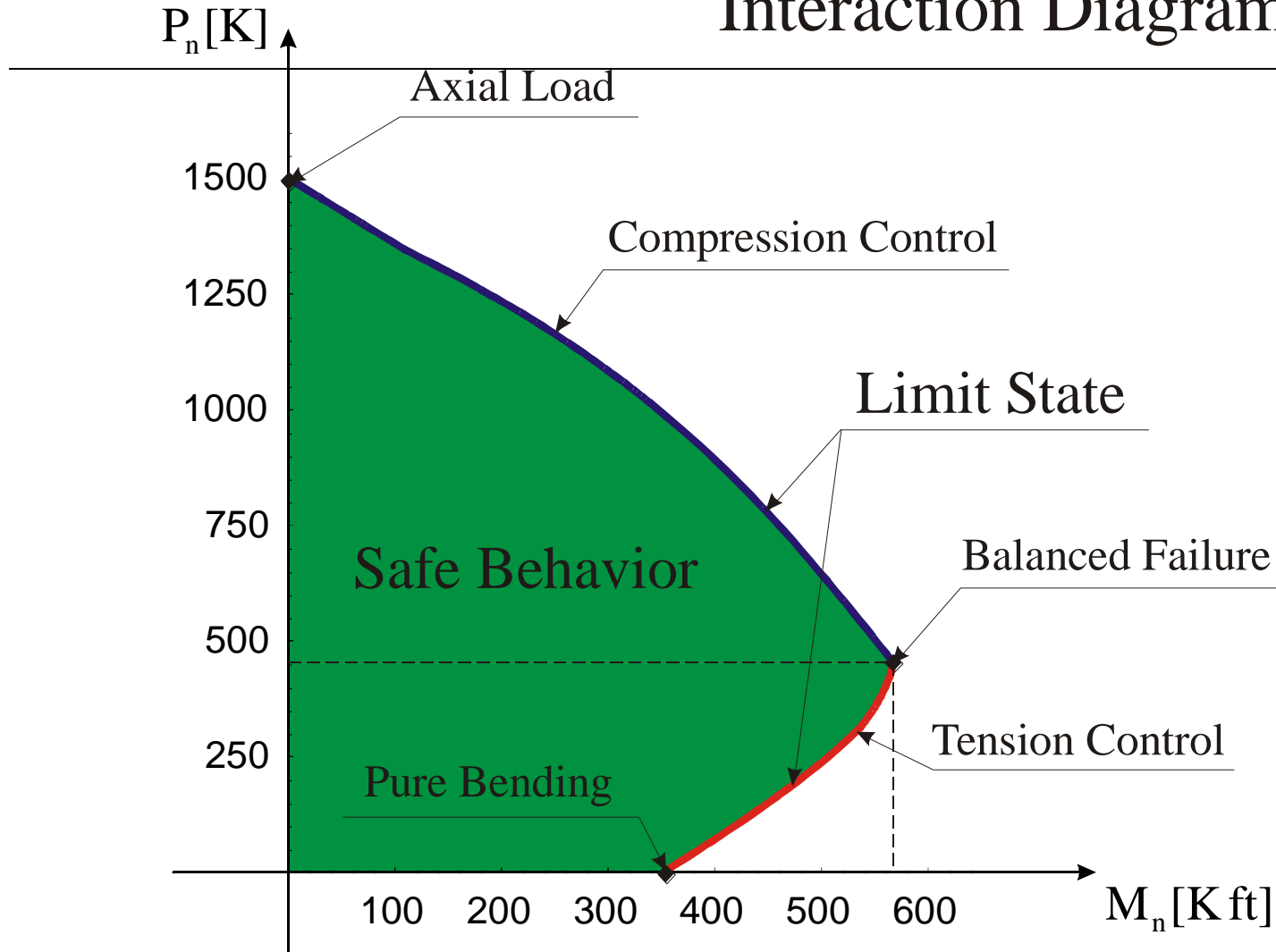
Eccentrically Loaded Columns

1. Basic Assumptions

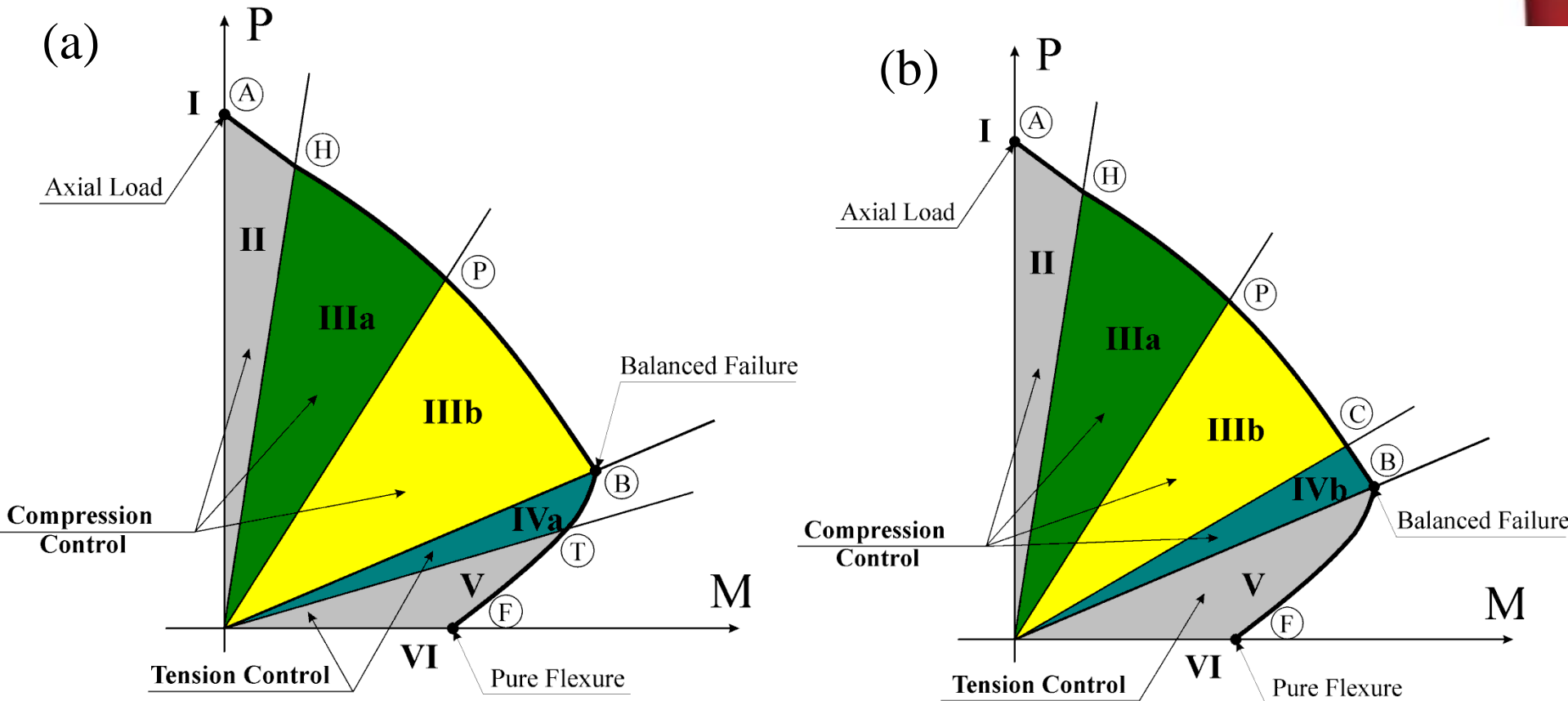


Columns

Interaction Diagram



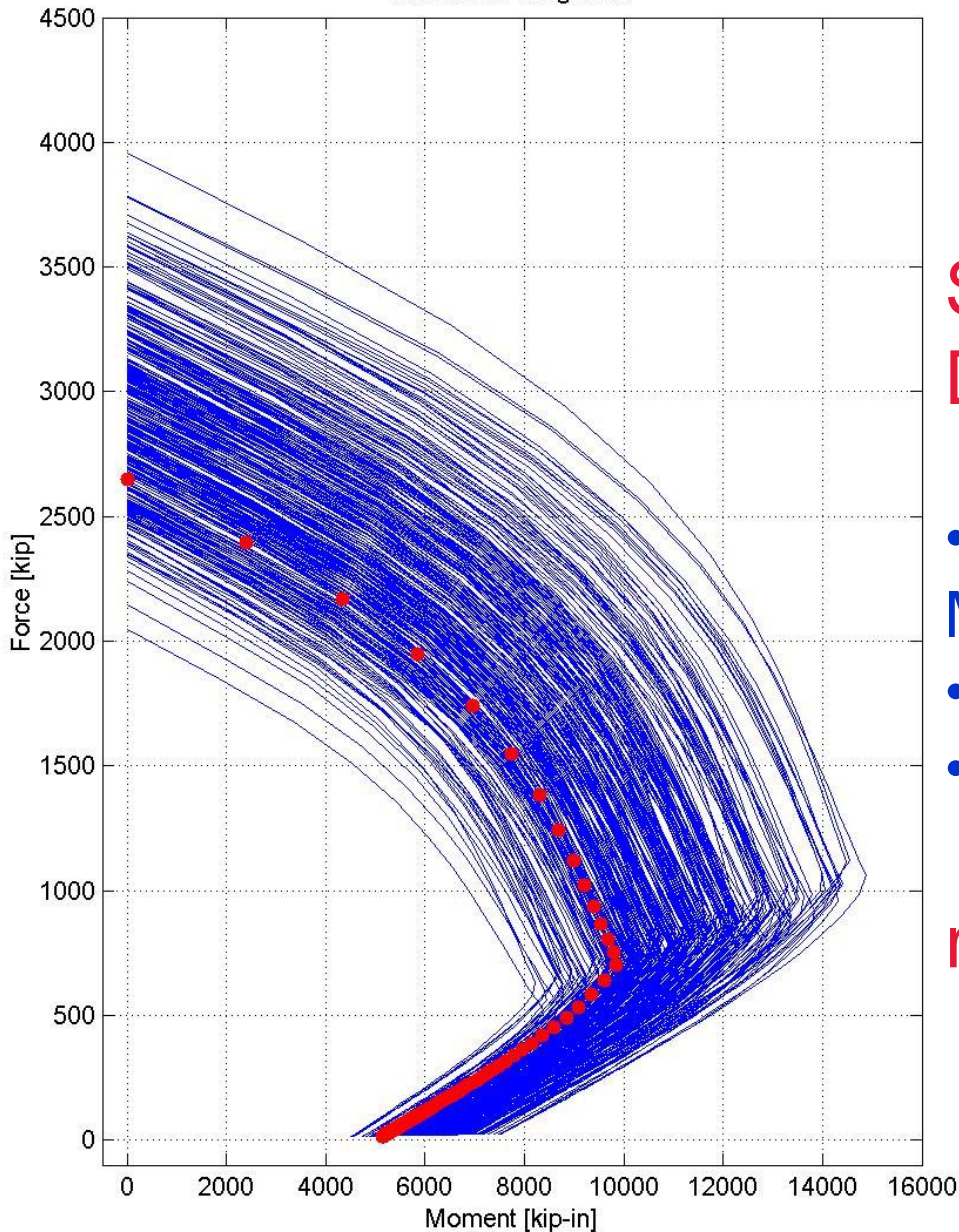
Analysis of Possible Cases of Cross Section Behavior



Interaction Diagram for Eccentrically Compressed Columns
(a) Cross Sections Type I, (b) Cross Sections Type II.



Interaction Diagrams

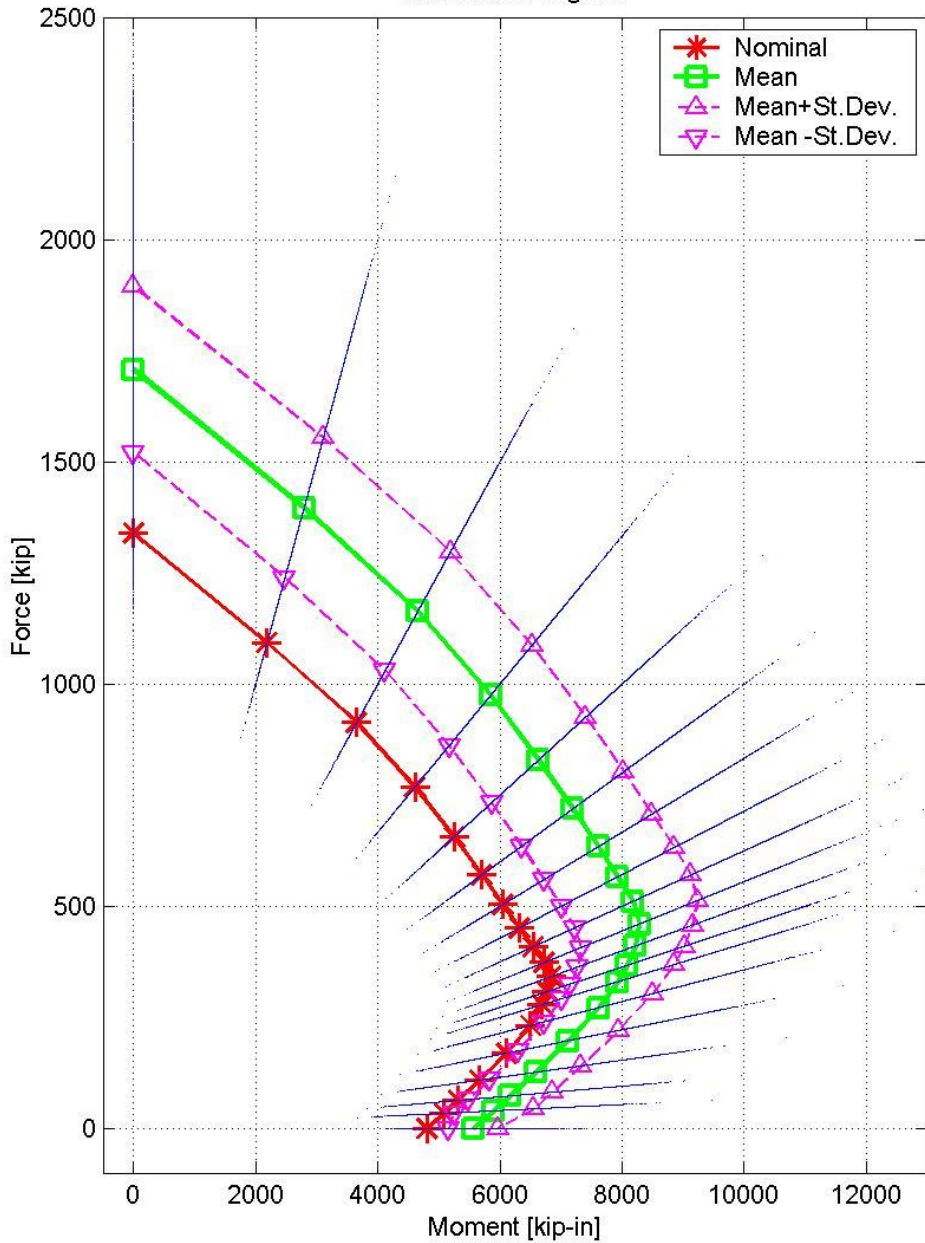


Simulated Interaction Diagrams

- concrete strength of 8 ksi (55 MPa)
- tied columns
- cast-in-place

red dots = nominal values

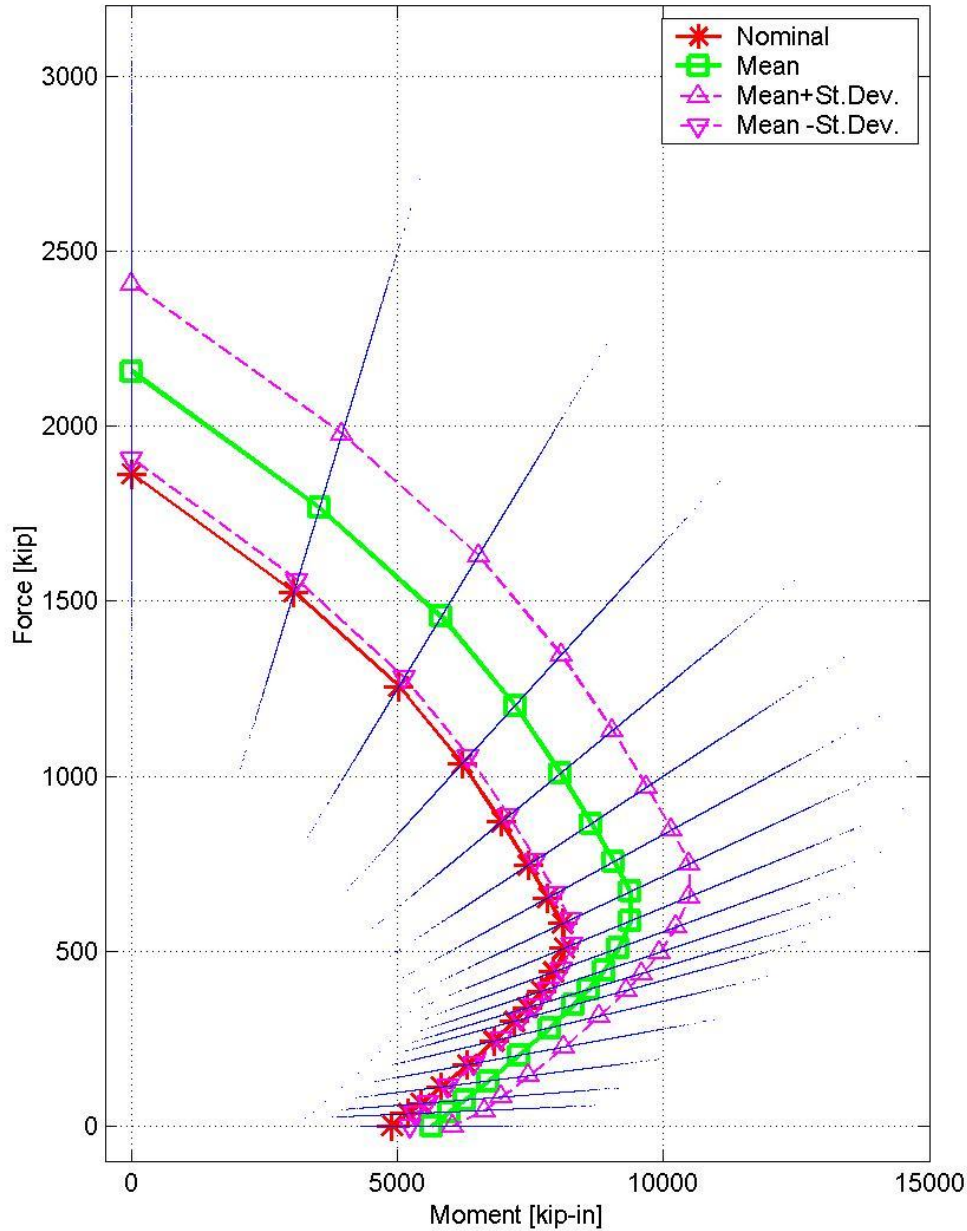
Interaction Diagram



Interaction Diagrams
For Concrete 3 ksi (21 MPa)
(tied columns, cast-in-place)



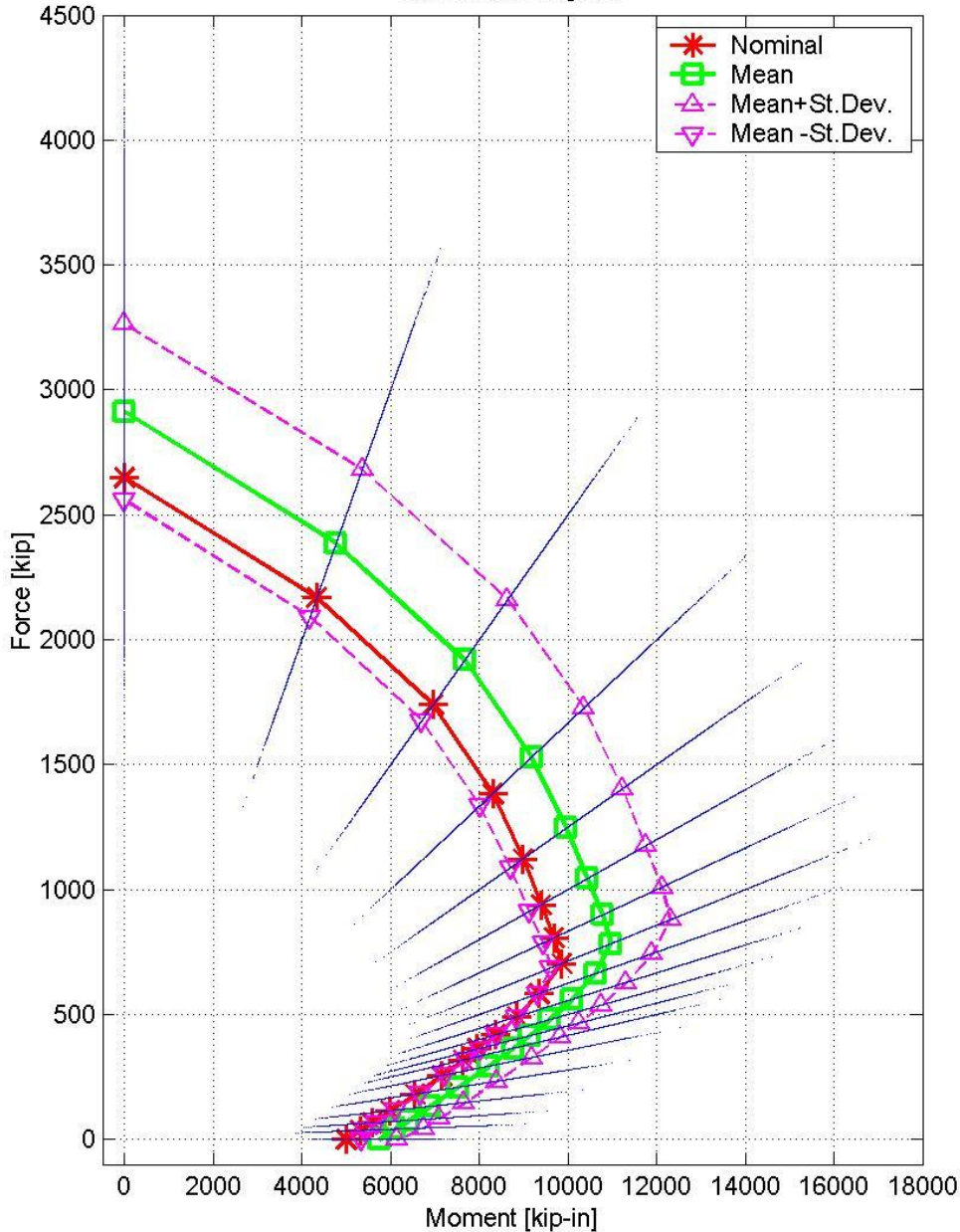
Interaction Diagram



Interaction Diagrams
For Concrete 5 ksi (35 MPa)
(tied columns, cast-in-place)

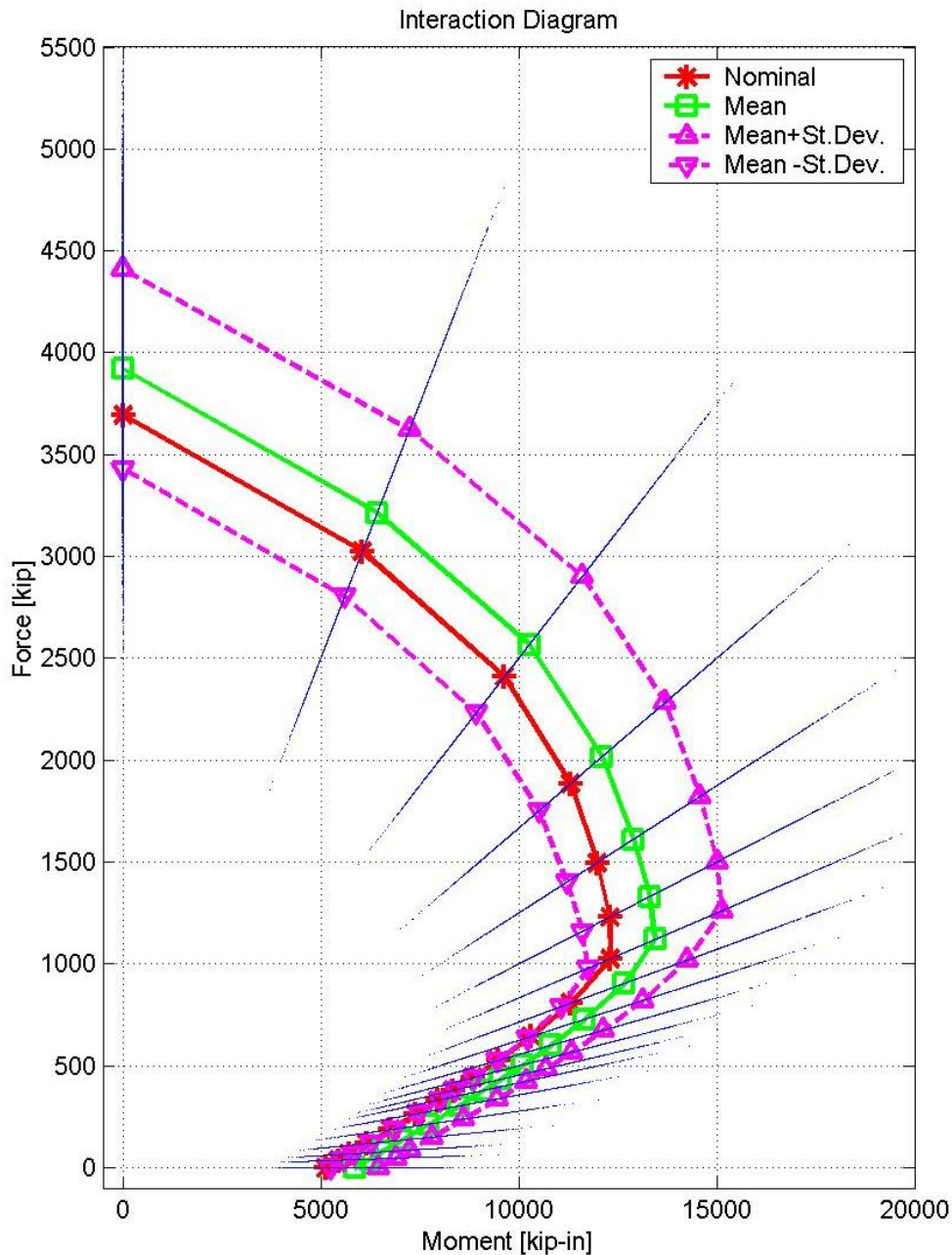


Interaction Diagram



Interaction Diagrams
For Concrete 8 ksi (55 MPa)
(tied columns, cast-in-place)



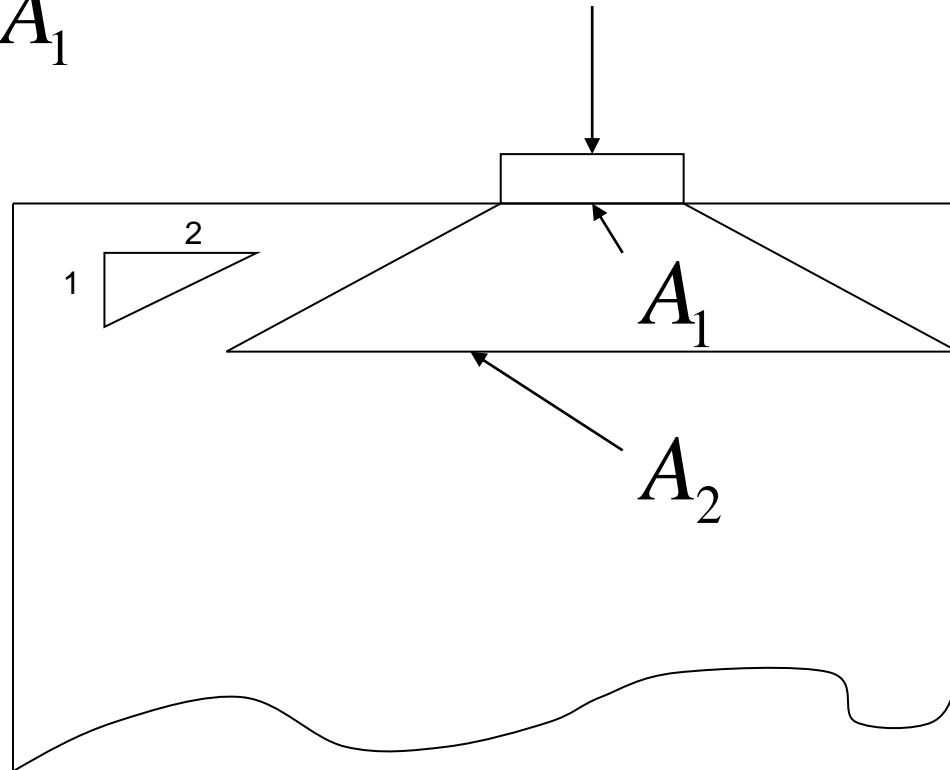


Interaction Diagrams

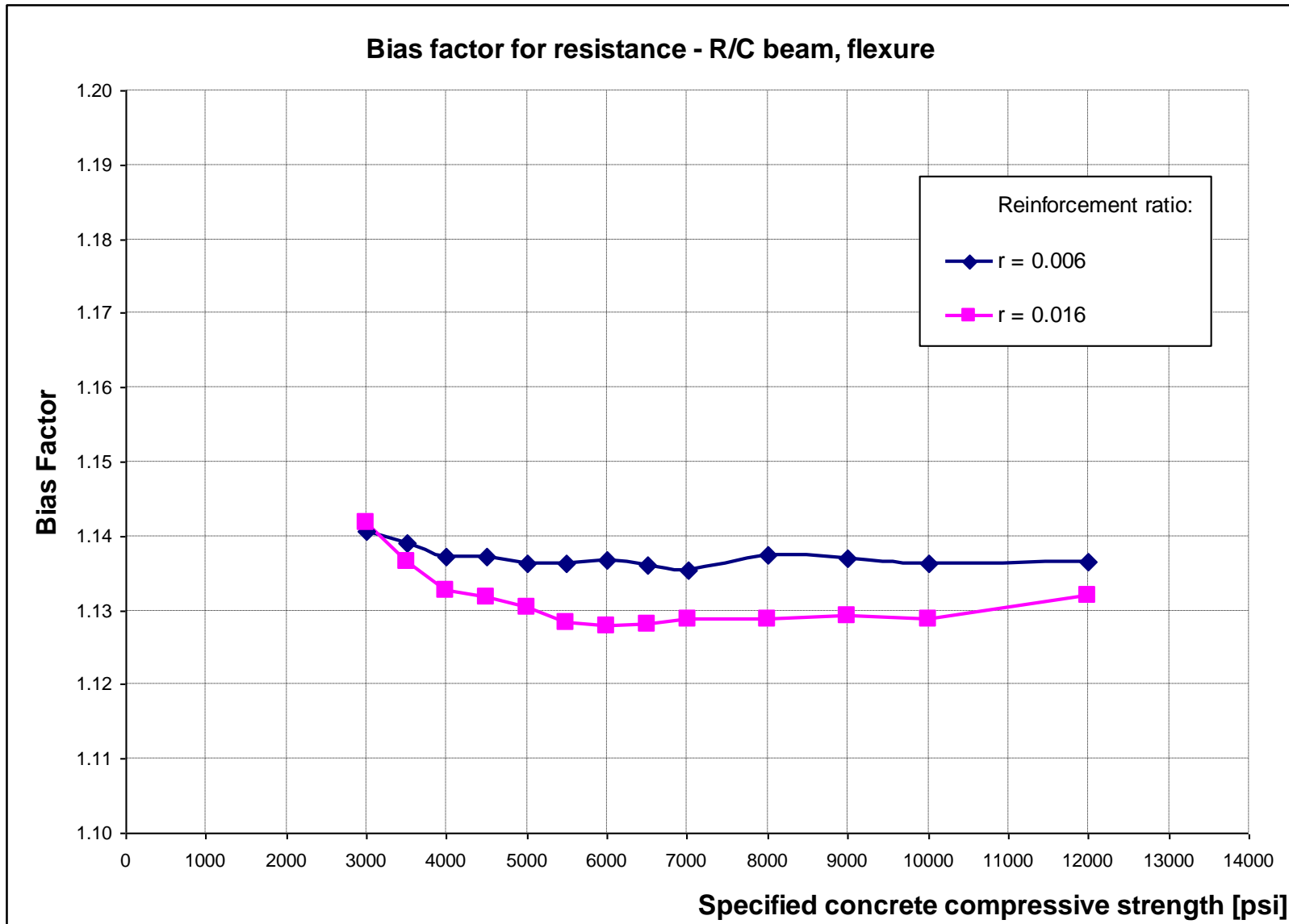
- concrete 12 ksi (85 MPa)
- tied columns,
- cast-in-place

Bearing Resistance of Concrete

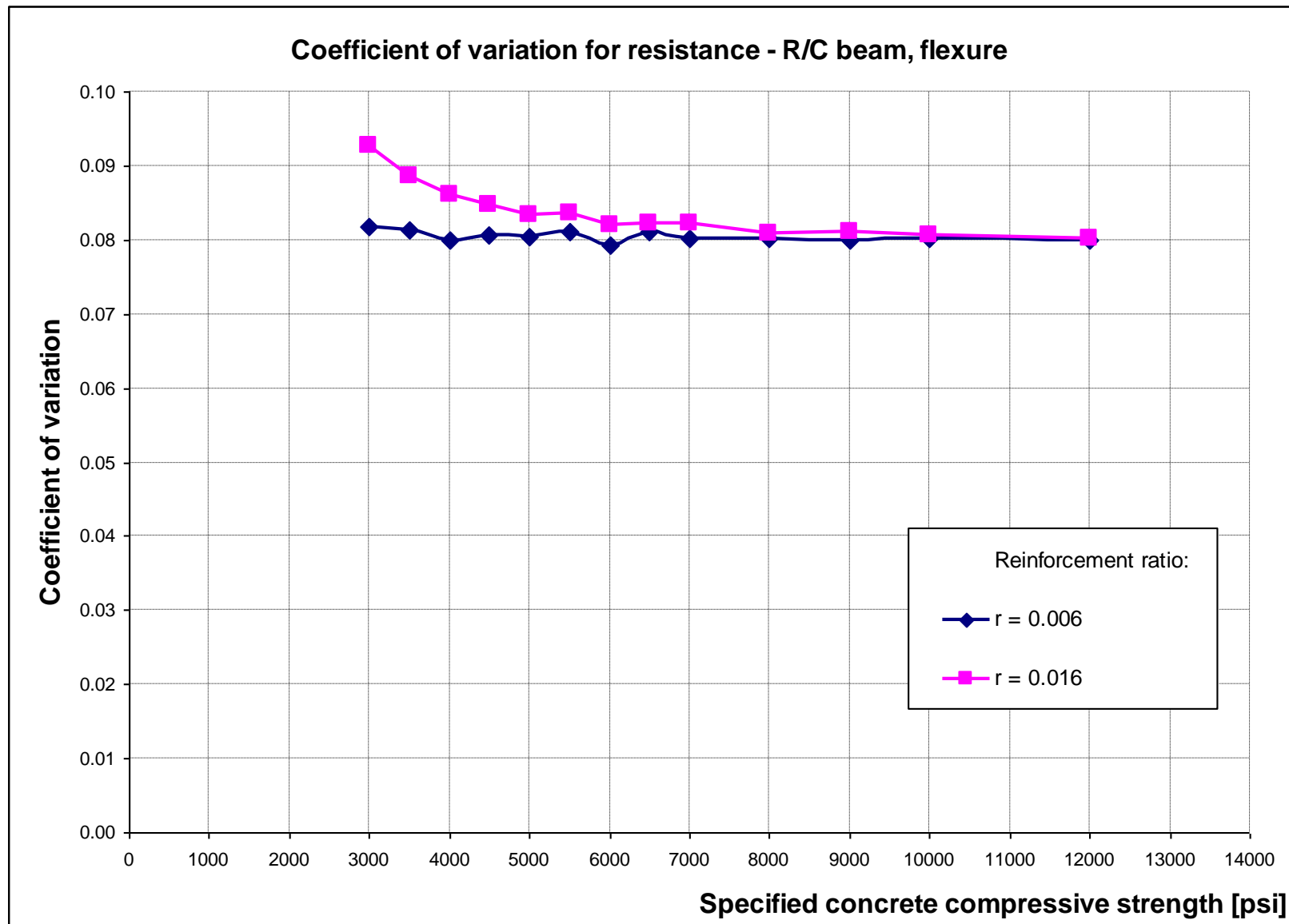
$$R = 0.85 f'_c A_1 \sqrt{\frac{A_2}{A_1}}$$



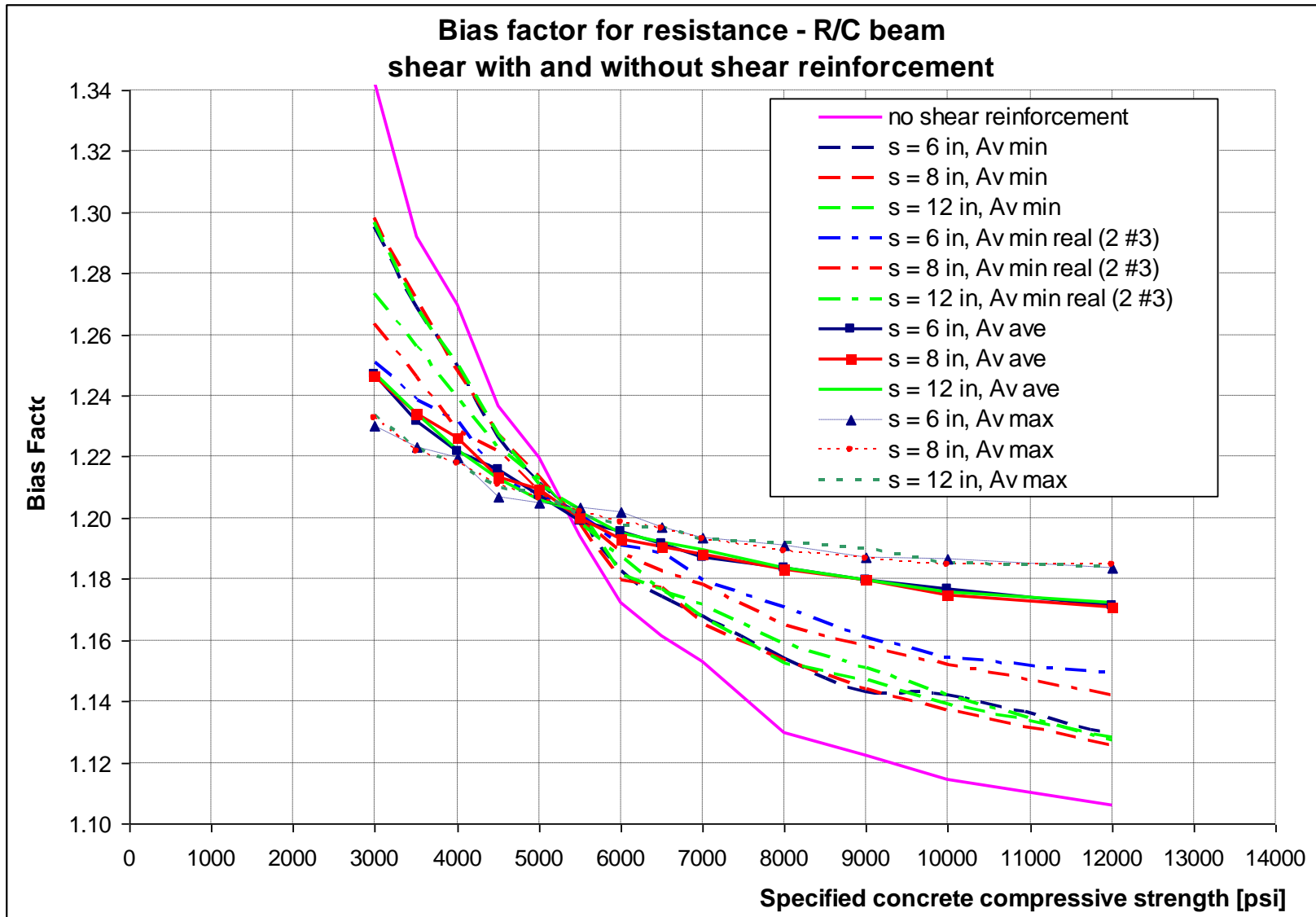
Bias Factor of Resistance for Beams, Flexure



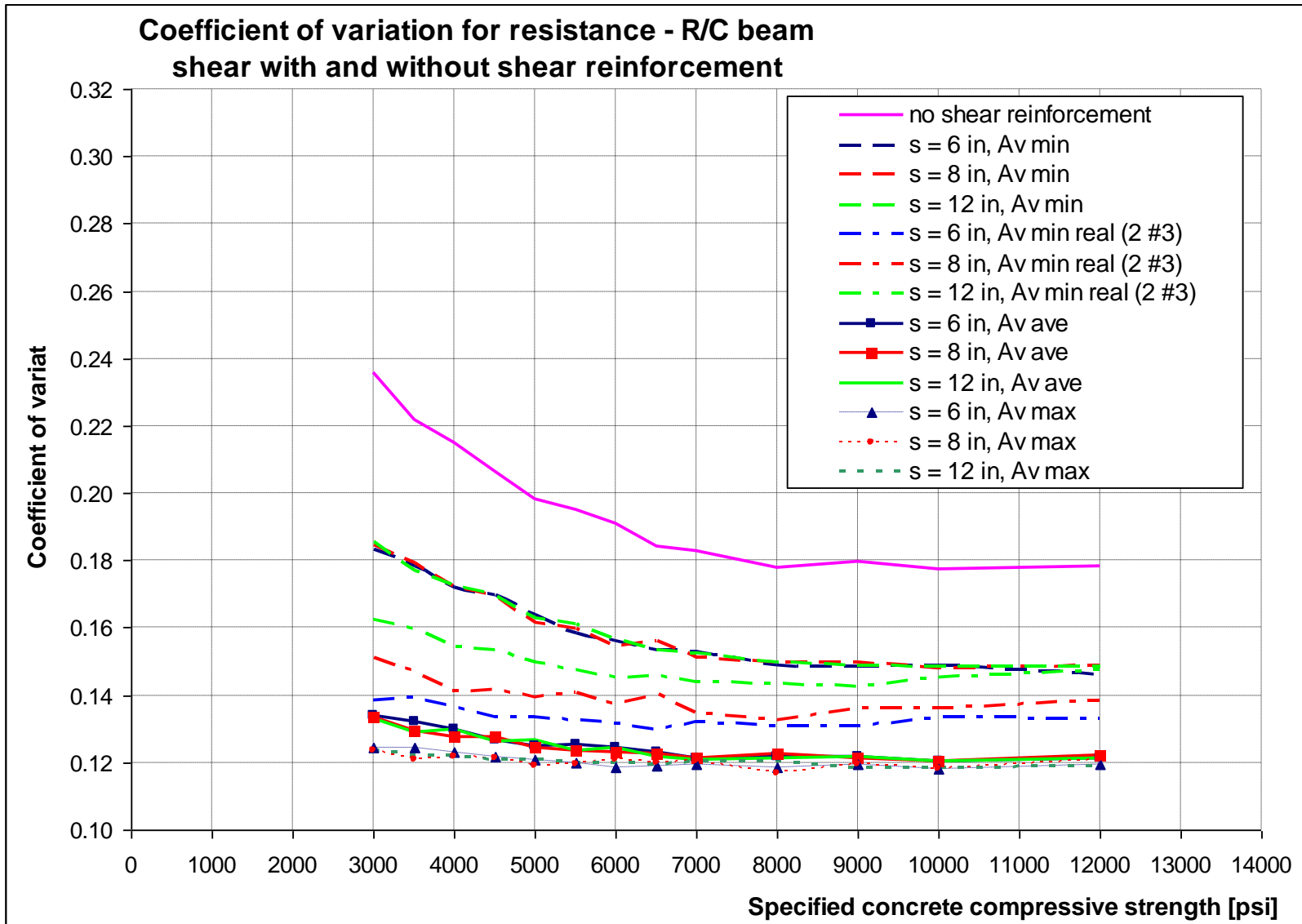
Coefficient of Variation of Resistance for Beams, Flexure



Bias Factor of Resistance for Beams, Shear

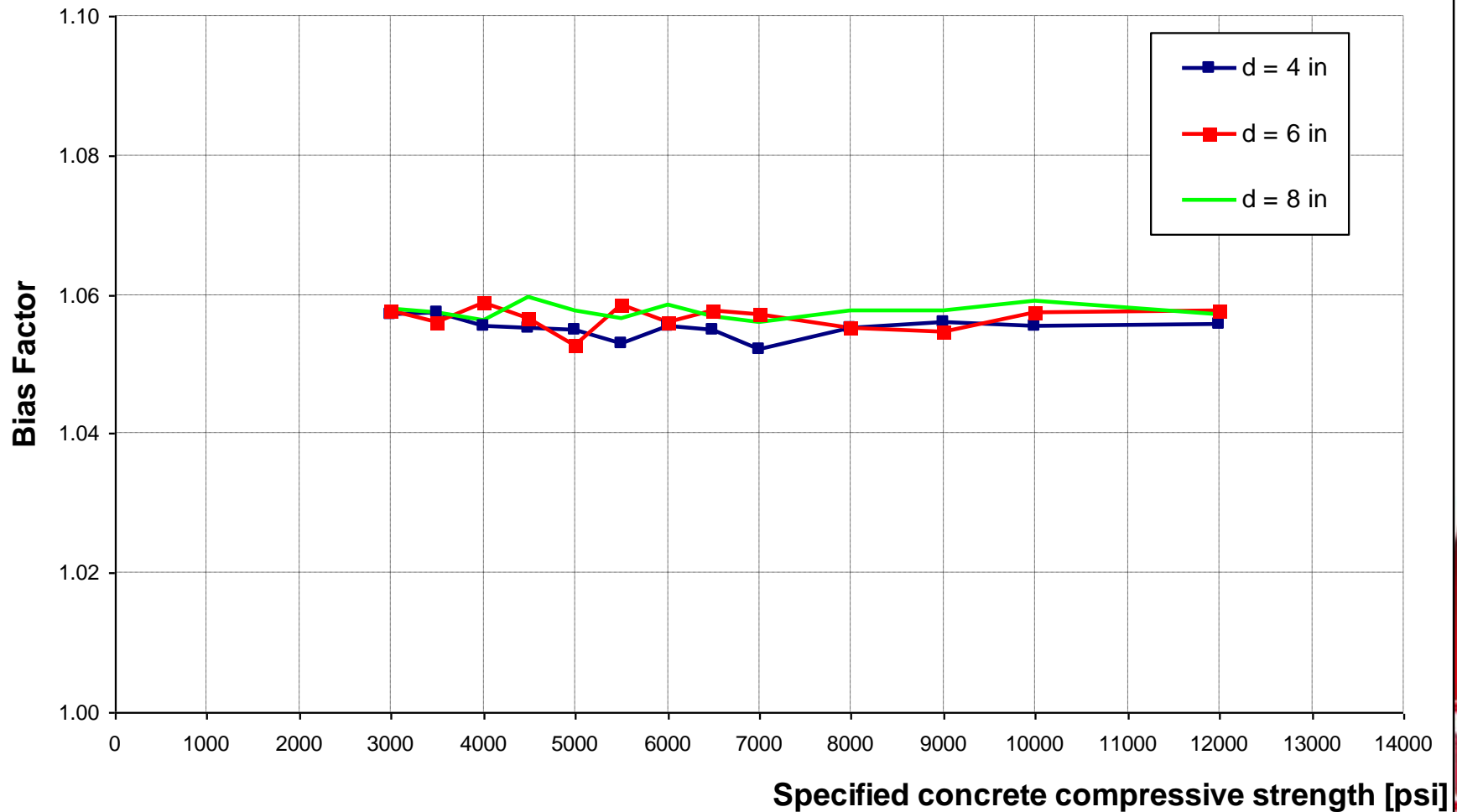


Coefficient of Variation of Resistance for Beams, Shear



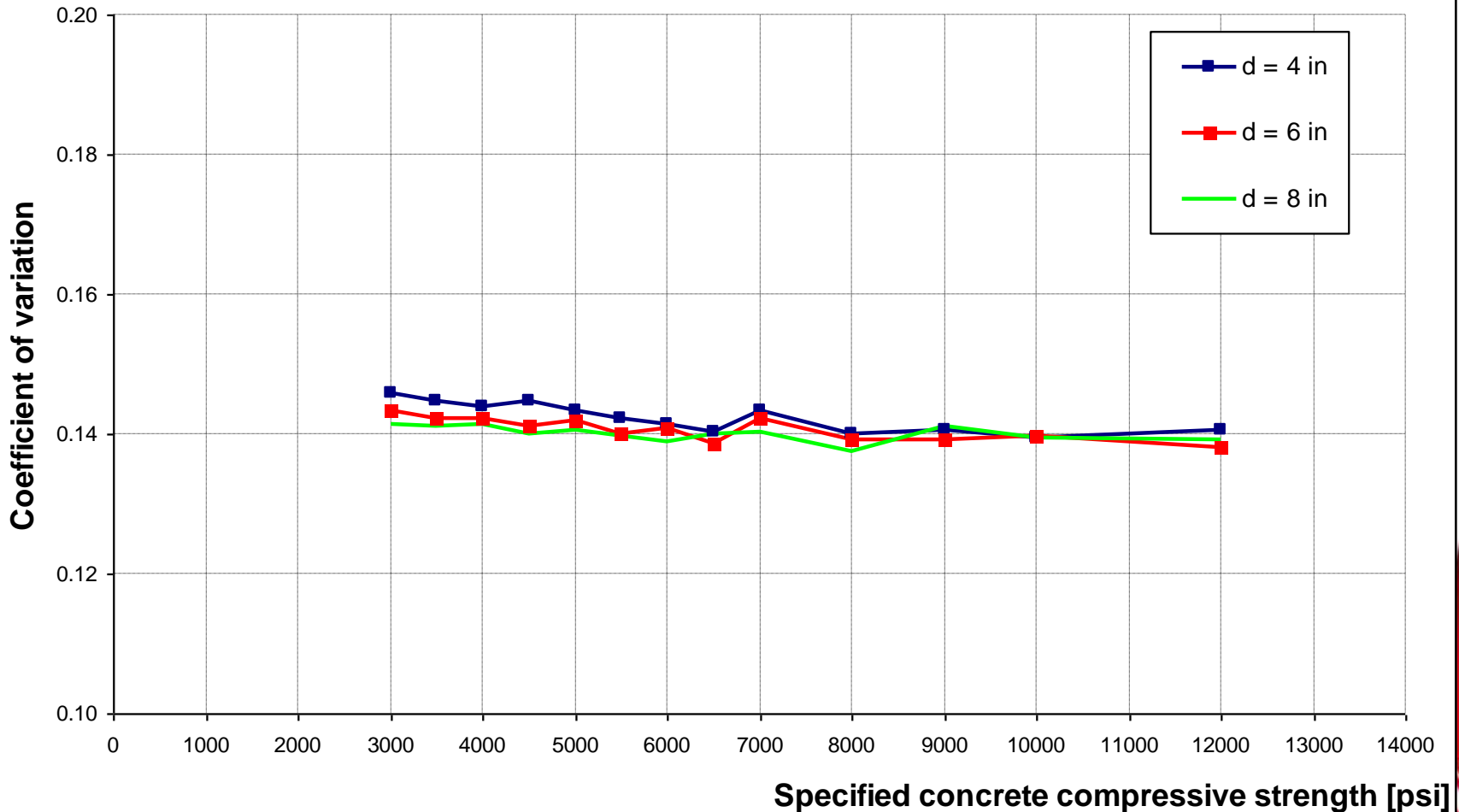
Bias Factor of Resistance for One way Slab, Flexure

Bias factor for resistance - R/C slab, 1-way flexure



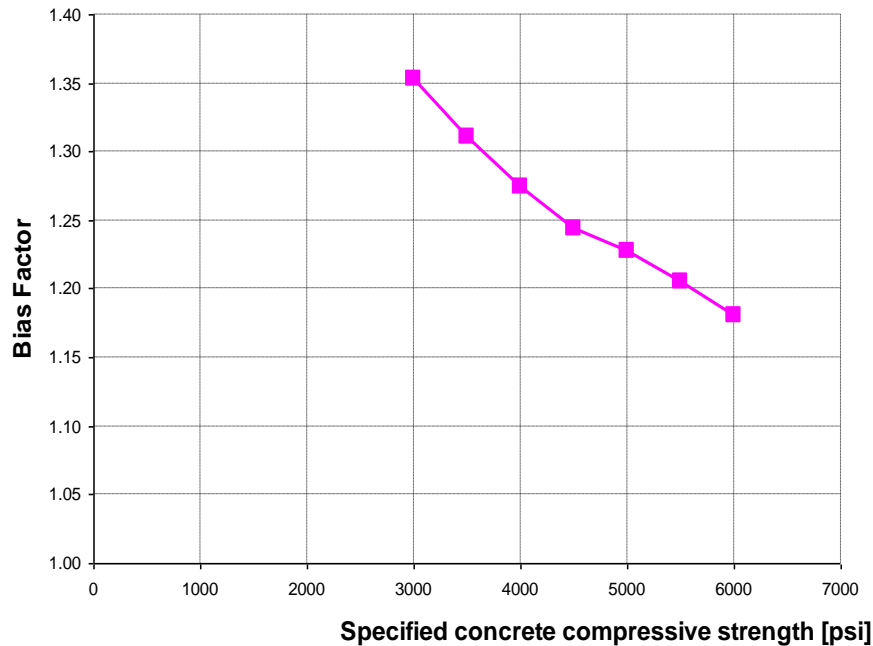
Coefficient of Variation of Resistance for One way slab, Flexure

Coefficient of variation for resistance - R/C slab, 1-way flexure

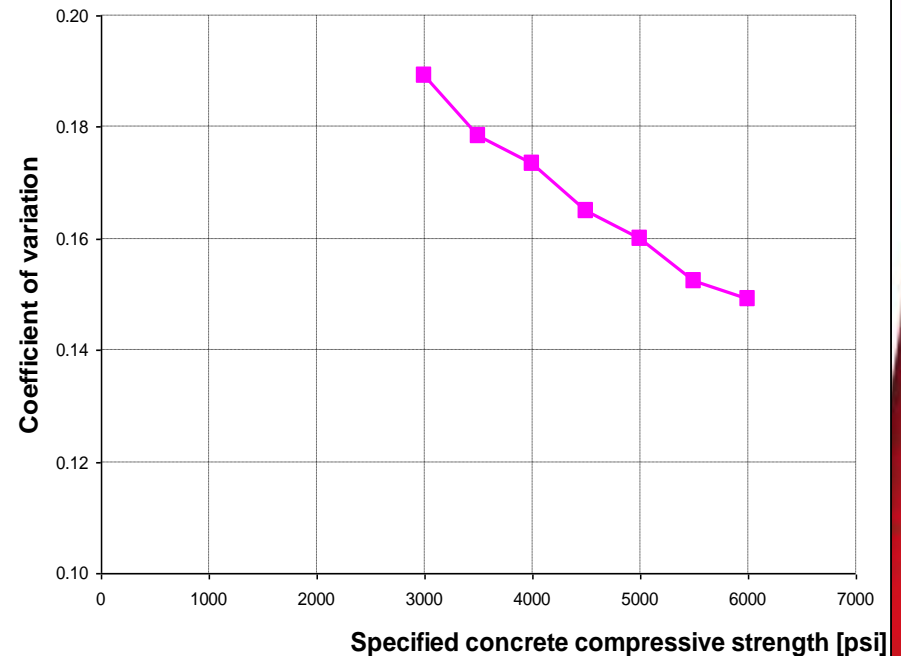


Bias Factor and Coefficient of Variation of Resistance for Concrete Bearing Strength

Bias factor for resistance - concrete bearing



Coefficient of variation for resistance - concrete bearing



Statistical Parameters of Fabrication Factor (Ellingwood, Galambos, MacGregor, Cornell)

	λ	V
width of beam, b	1.01	0.04
effective depth of beam, d	0.99	0.04
effective depth of one-way slab, d	0.92	0.12
effective depth of two-way slab, d		
$d = 4$ in	1.03	0.09
$d = 6$ in	1.02	0.06
$d = 8$ in	1.015	0.04
depth and width of column, b_1, b_2	1.005	0.04
area of reinforcement, A_s, A_v	1.00	0.015
spacing of shear reinforcement, s	1.00	0.04



Statistical Parameters of Professional Factor (Ellingwood, Galambos, MacGregor, Cornell)

	λ	V
R/C beams - flexure	1.02	0.06
R/C beams - shear without stirrups	1.16	0.11
R/C beams - shear with stirrups	1.075	0.10
Axially loaded columns, tied	1.00	0.08
Axially loaded columns, spiral	1.05	0.06
One way slabs - flexure	1.02	0.06
One way slabs - shear	1.16	0.11
Two way slabs - shear	1.16	0.11
Bearing strength	1.02	0.06



Monte Carlo Simulation Results - Examples

Resistance parameters for concrete $f_c' = 4000$ psi (28 MPa)

	λ	V
R/C beams - flexure	1.14	0.08
R/C beams - shear without stirrups	1.27	0.23
R/C beams - shear with stirrups	1.235	0.15
Axially loaded columns, tied	1.22	0.145
Axially loaded columns, spiral	1.29	0.14
One way slabs - flexure	1.055	0.14
One way slabs - shear	1.165	0.255
Two way slabs - shear	1.305	0.24
Bearing strength	1.275	0.17



Basic questions:

- How can we measure safety of a structure?
- How safe is safe enough? What is the target reliability?
- How to implement the optimum safety level?

Reliability Index, β

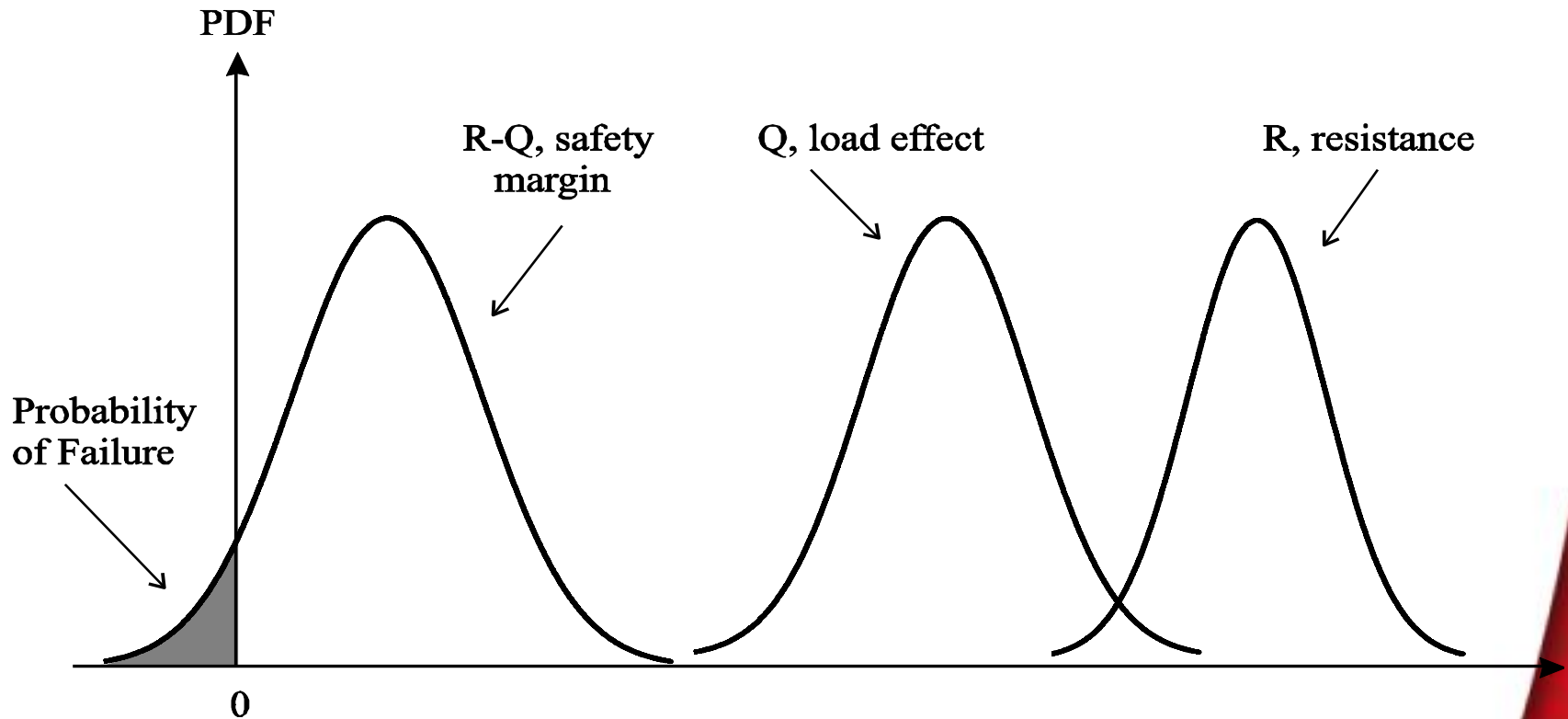


Figure 5-8 PDFs of load, resistance, and safety margin.
Department of Civil Engineering

Reliability Index, β

For a linear limit state function, $g = R - Q = 0$, and R and Q both being normal random variables

$$\beta = \frac{(\mu_R - \mu_Q)}{\sqrt{\sigma_R^2 + \sigma_Q^2}}$$

μ_R = mean resistance

μ_Q = mean load

σ_R = standard deviation of resistance

σ_Q = standard deviation of load



Reliability index and probability of failure

P_F	β
10^{-1}	1.28
10^{-2}	2.33
10^{-3}	3.09
10^{-4}	3.71
10^{-5}	4.26
10^{-6}	4.75
10^{-7}	5.19
10^{-8}	5.62
10^{-9}	5.99



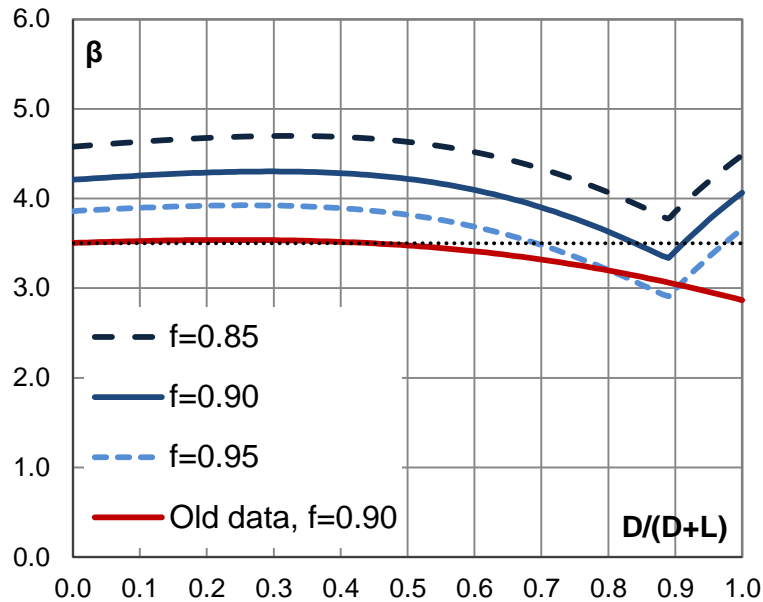
Reliability Analysis Procedures

- Closed-form equations – accurate results only for special cases
- First Order Reliability Methods (FORM), reliability index is calculated by iterations
- Second Order Reliability Methods (SORM), and other advanced procedures
- Monte Carlo method - values of random variables are simulated (generated by computer), accuracy depends on the number of computer simulations

Reliability Indices for R/C Beams, Flexure, (D+L)

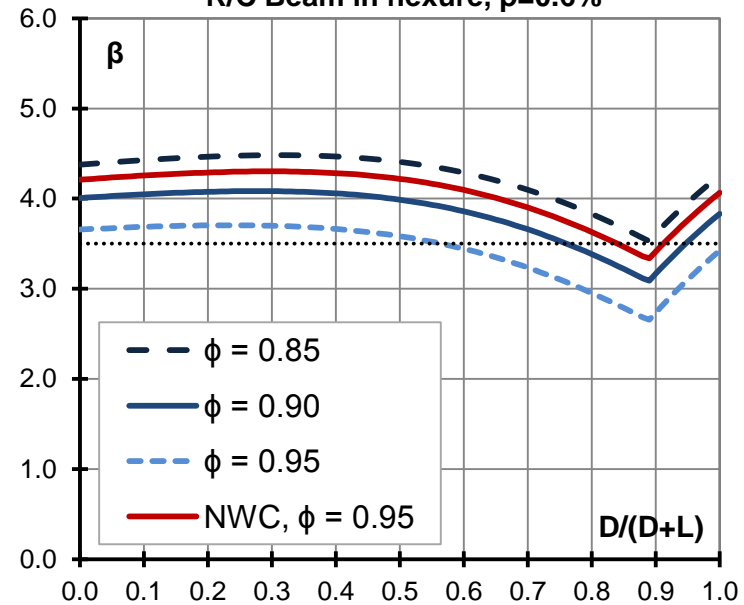
Ordinary concrete

R/C Beam in flexure, $\rho=0.6\%$



Lightweight concrete

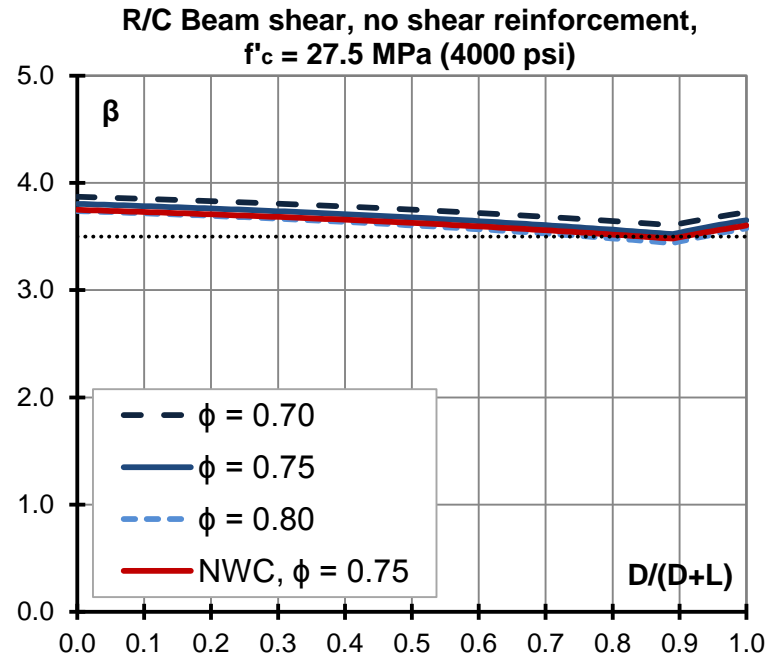
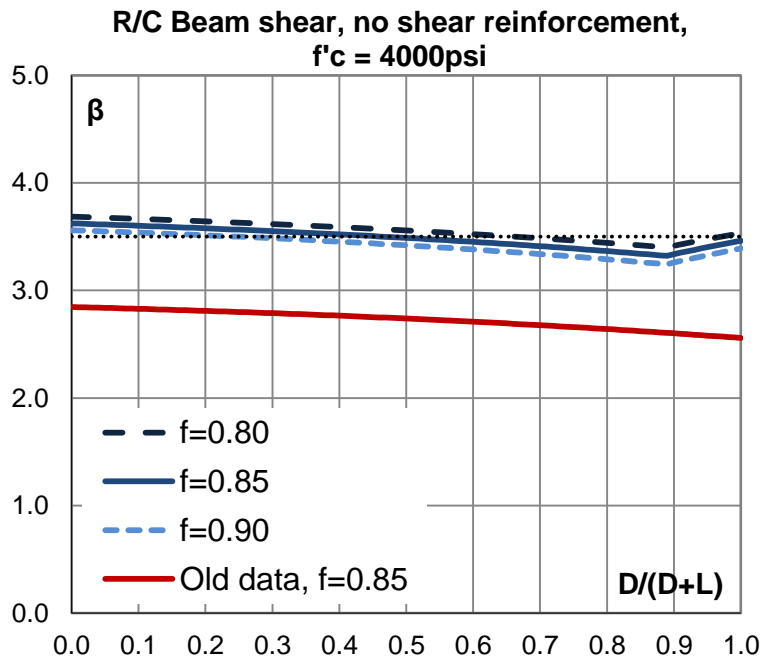
R/C Beam in flexure, $\rho=0.6\%$



Reliability Indices for R/C Beams, Shear, (D+L)

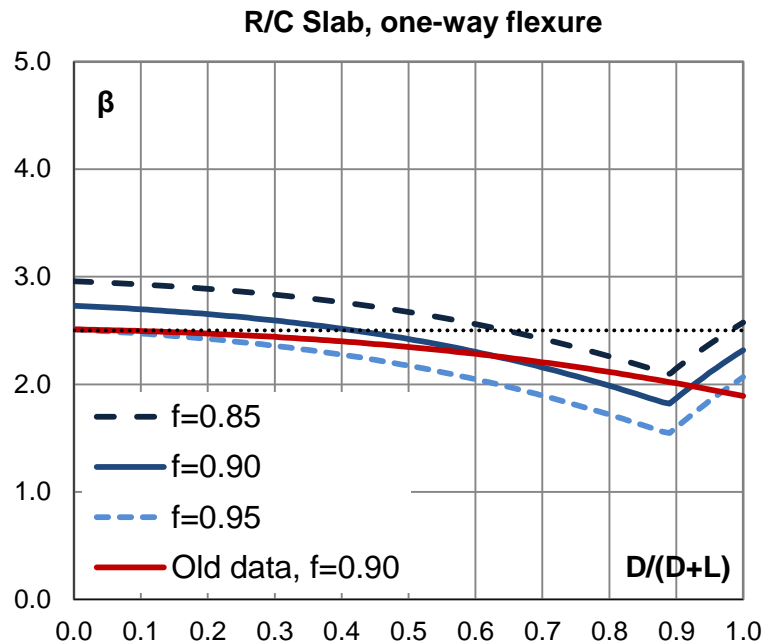
Ordinary concrete

Lightweight concrete

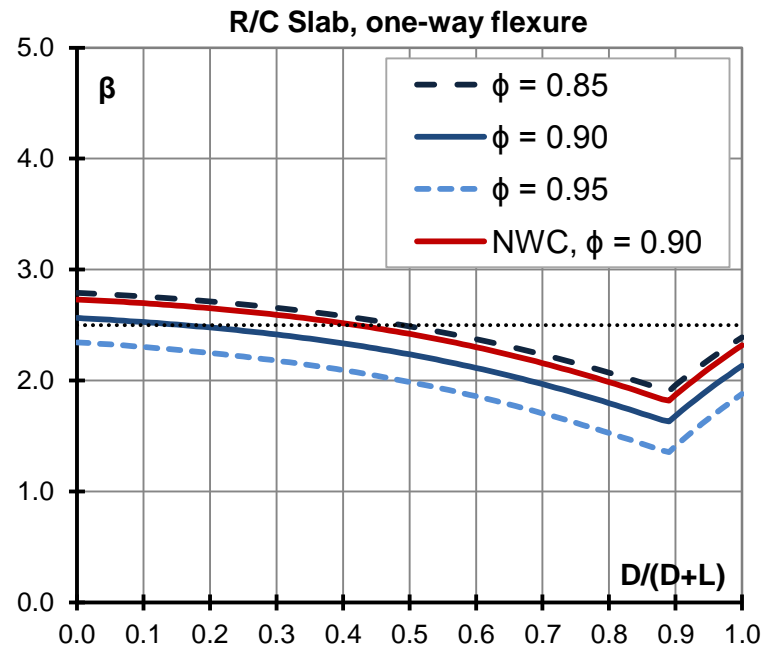


Reliability Indices for R/C Slab, flexure, (D+L)

Ordinary concrete

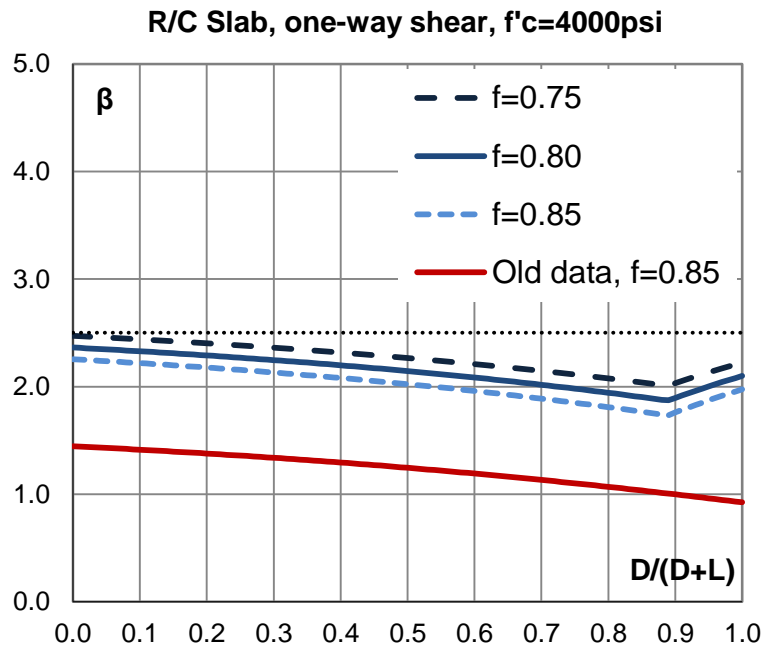


Lightweight concrete

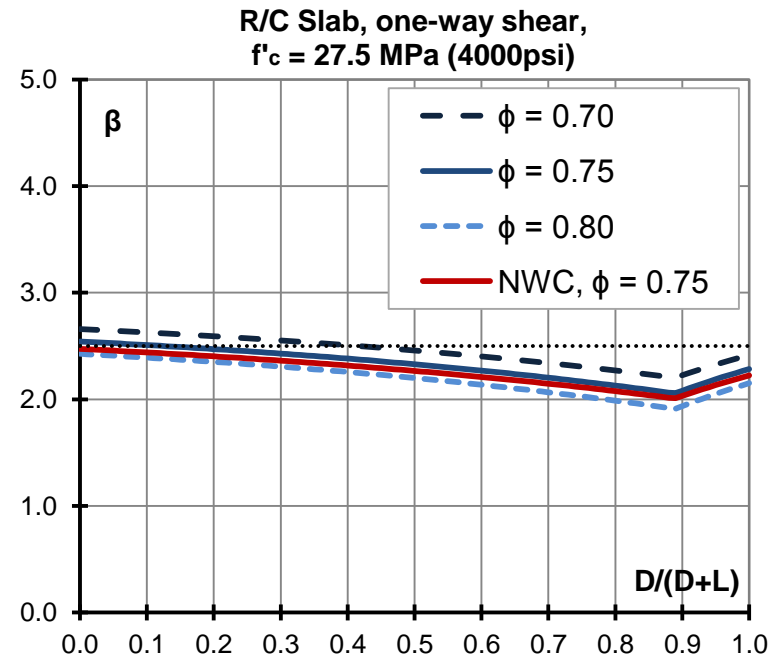


Reliability Indices for R/C Slab, one-way shear, (D+L)

Ordinary concrete

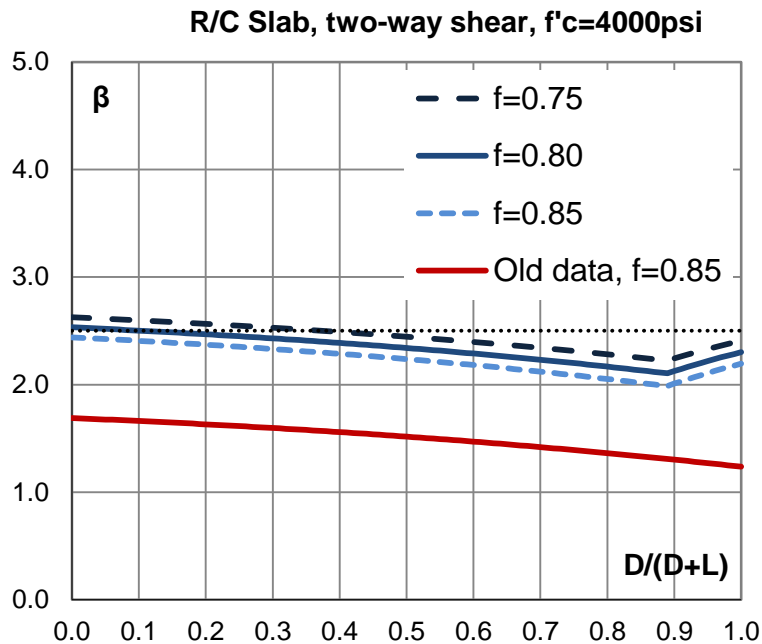


Lightweight concrete

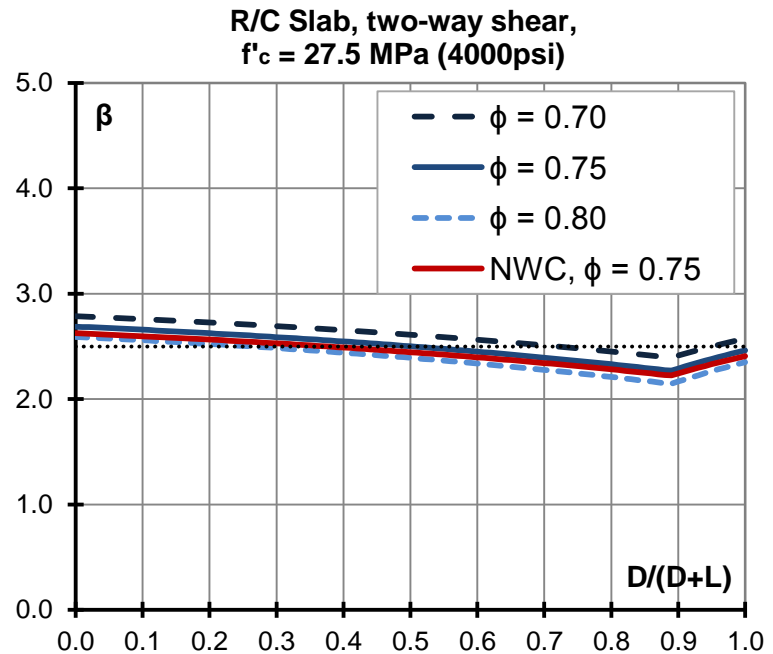


Reliability Indices for R/C Slab, two-way shear, (D+L)

Ordinary concrete

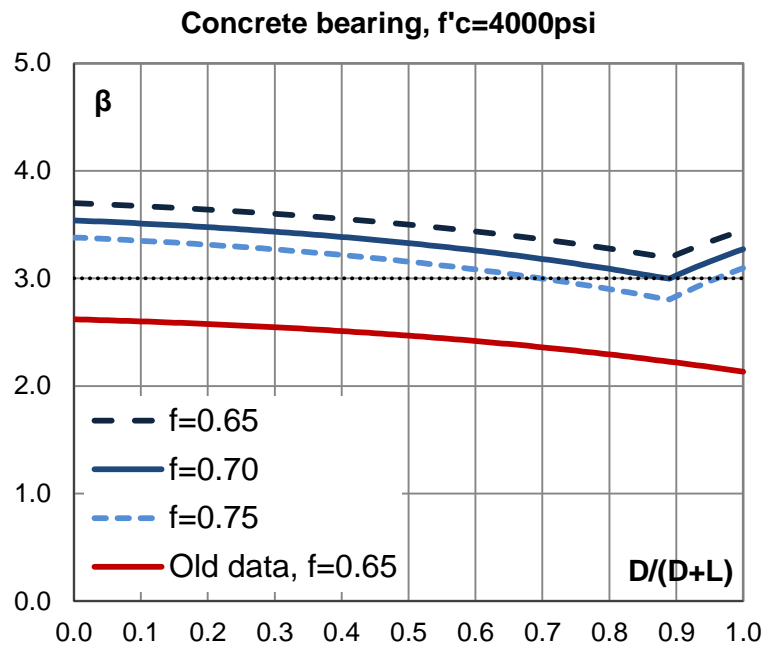


Lightweight concrete

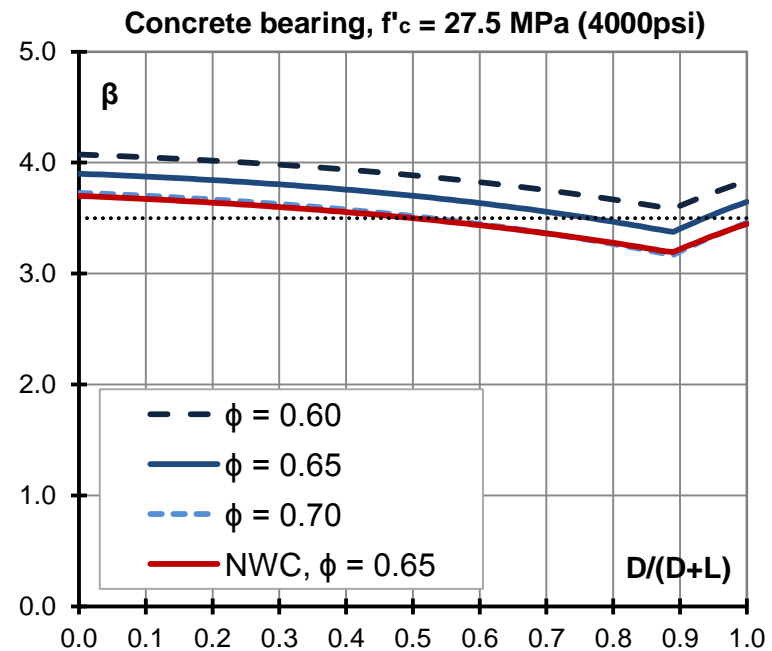


Reliability Indices for Concrete bearing, (D+L)

Ordinary concrete



Lightweight concrete



What is Optimum Reliability?

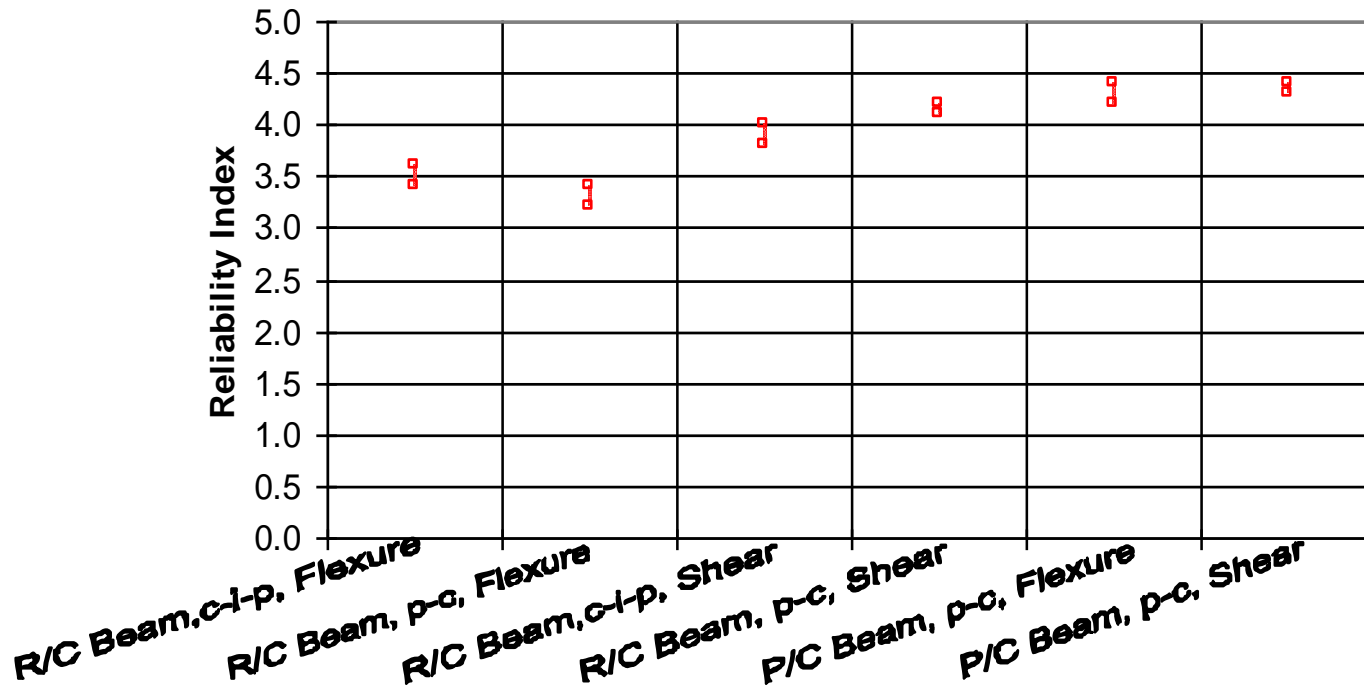
- If reliability index is too small – there are problems, even structural failures
- If reliability index is too large – the structures are too expensive

Target Reliability

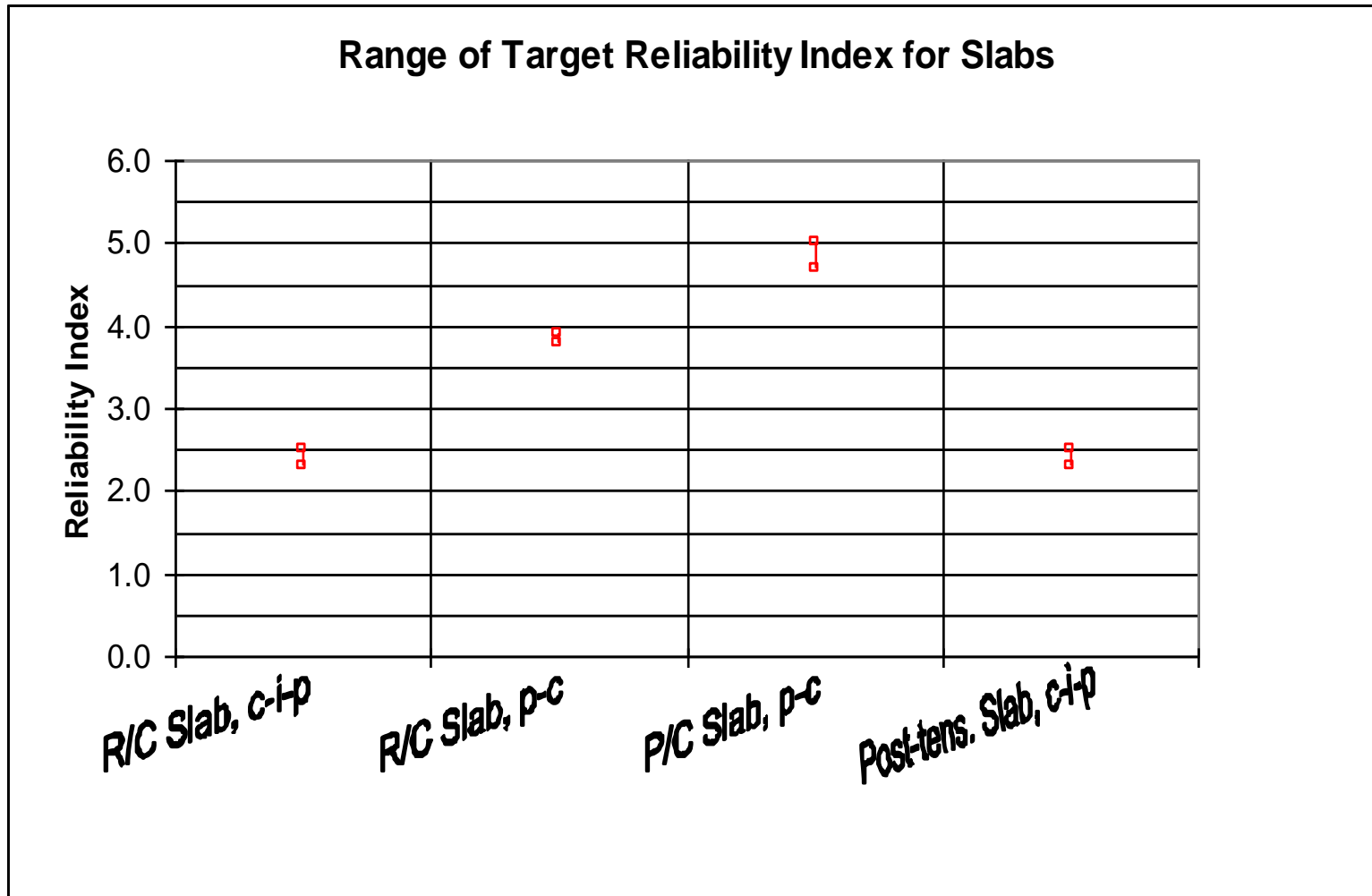
- Consequences of failure
- Economic analysis
- Past practice
- Human perception
- Social/political decisions

Selected Range of Reliability Indices for Beams, designed according to “old” ACI 318

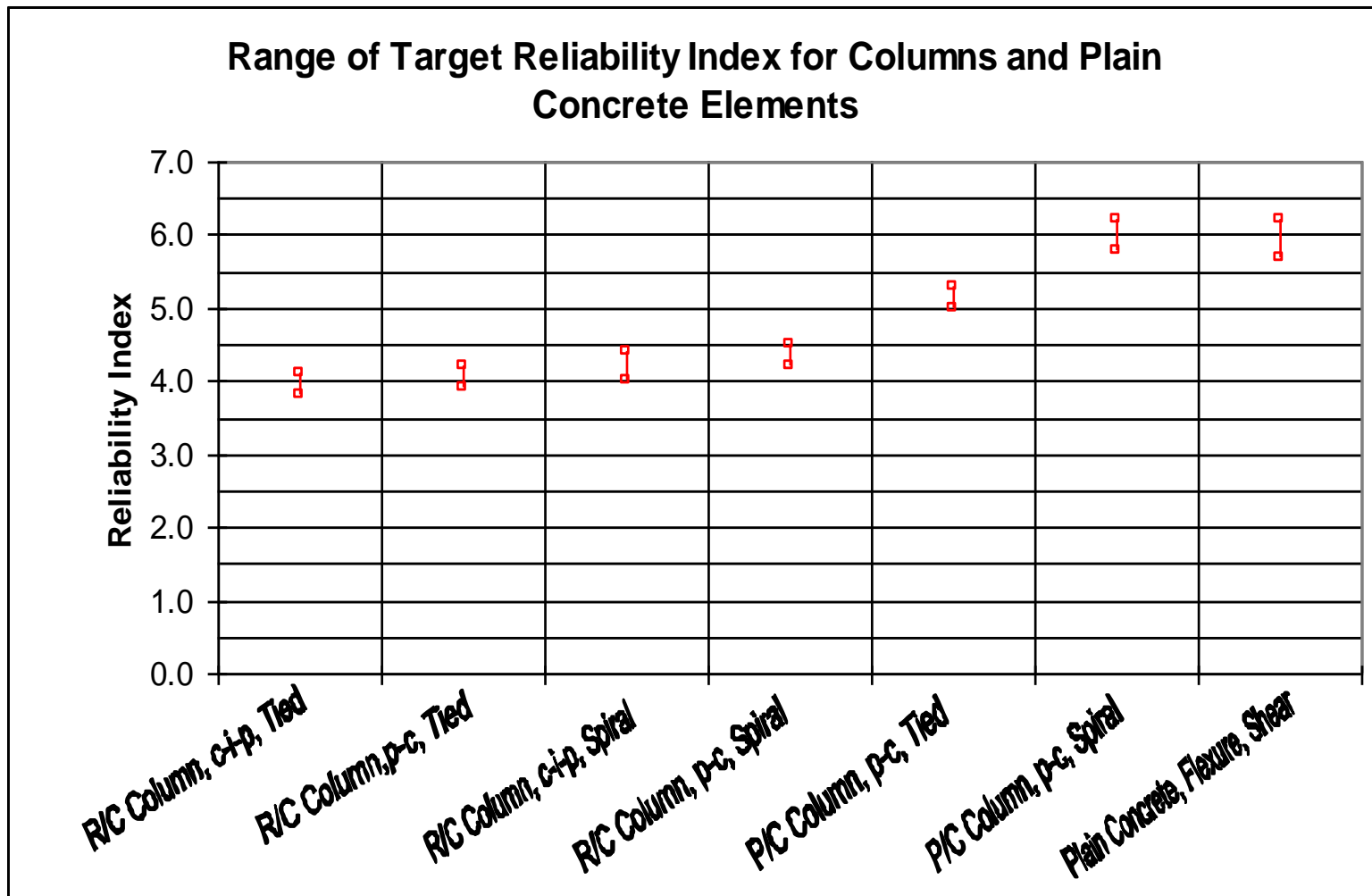
Range of Target Reliability Index for Beams



Selected Range of Reliability Indices for Slabs, designed according to “old” ACI 318



Selected Range of Reliability Indices for Columns and Plain Concrete Elements, designed according to “old” ACI 318



Calibration Results

	ACI 318-99	ACI 318-05	Recommended	
	ϕ	ϕ	ϕ	β_T
• R/C beams – flexure	0.90	0.90	0.90	3.5
• R/C beams - shear w/o stirrups	0.85	0.75	0.85	2.5
• R/C beams - shear with stirrups	0.85	0.75	0.85	3.5
• Axially loaded columns, tied	0.70	0.65	0.70	4.0
• Axially loaded columns, spiral	0.75	0.70	0.75	4.0
• One way slabs – flexure	0.90	0.90	0.90	2.5
• One way slabs – shear	0.85	0.75	0.85	2.5
• Two way slabs – shear	0.85	0.75	0.85	2.5
• Bearing strength	0.70	0.65	0.70	3.0



Load factors specified by ACI 318 and ASCE 7

The design formula specified
by ACI 318-99 Code

$$1.4 D + 1.7 L < \phi R$$

$$0.75 (1.4 D + 1.7 L + 1.7 W) < \phi R$$

$$0.9 D + 1.3 W < \phi R$$

$$0.75 (1.4 D + 1.7 L + 1.87 E) < \phi R$$

The design formula specified
by ASCE-7 Standard

$$1.4 D < \phi R$$

$$1.2 D + 1.6 L < \phi R$$

$$1.2 D + 1.6 L + 0.5 S < \phi R$$

$$1.2 D + 0.5 L + 1.6 S < \phi R$$

$$1.2 D + 1.6 W + 0.5 L + 0.5 S < \phi R$$

$$1.2 D + 1.0 E + 0.5 L + 0.2 S < \phi R$$

$$0.9 D - (1.6 W \text{ or } 1.0 E) < \phi R$$



American Concrete Institute (ACI)

ACI 318-11

**Building Code Requirements for
Structural Concrete (ACI 318-11)**

An ACI Standard

and Commentary

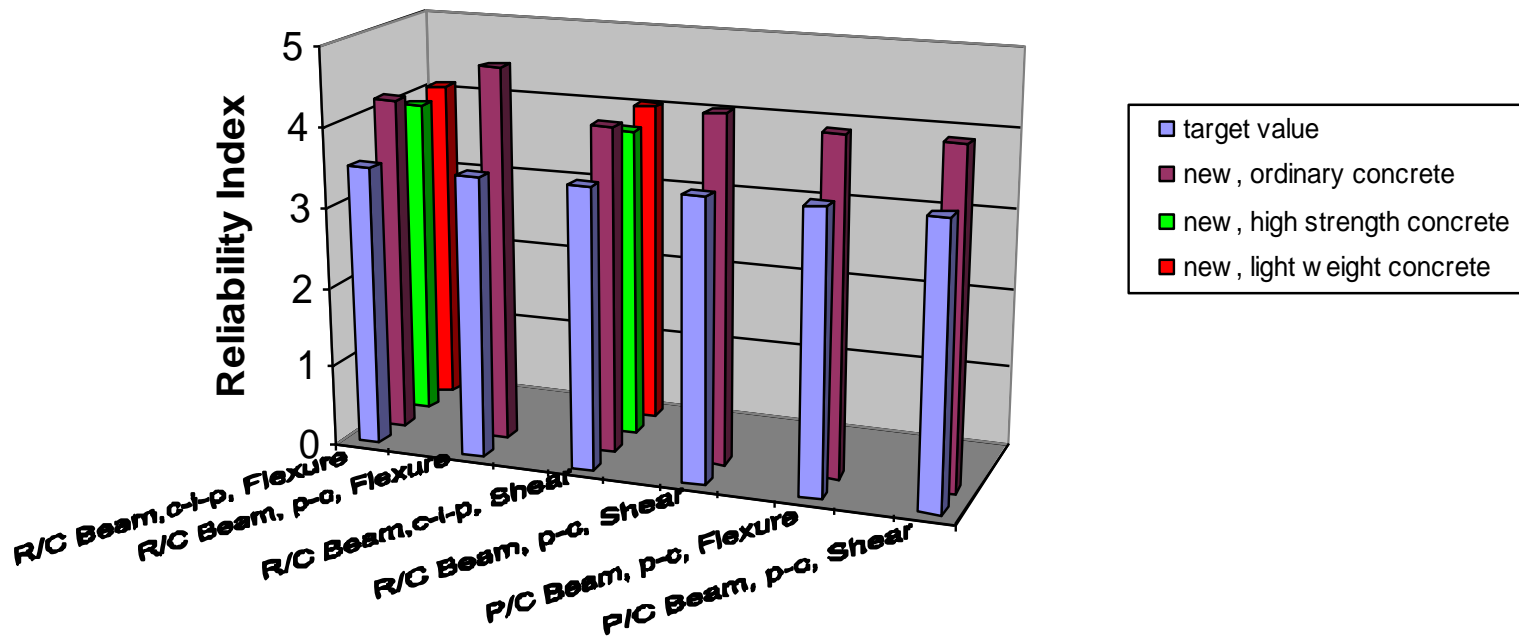
Reported by ACI Committee 318



American Concrete Institute®

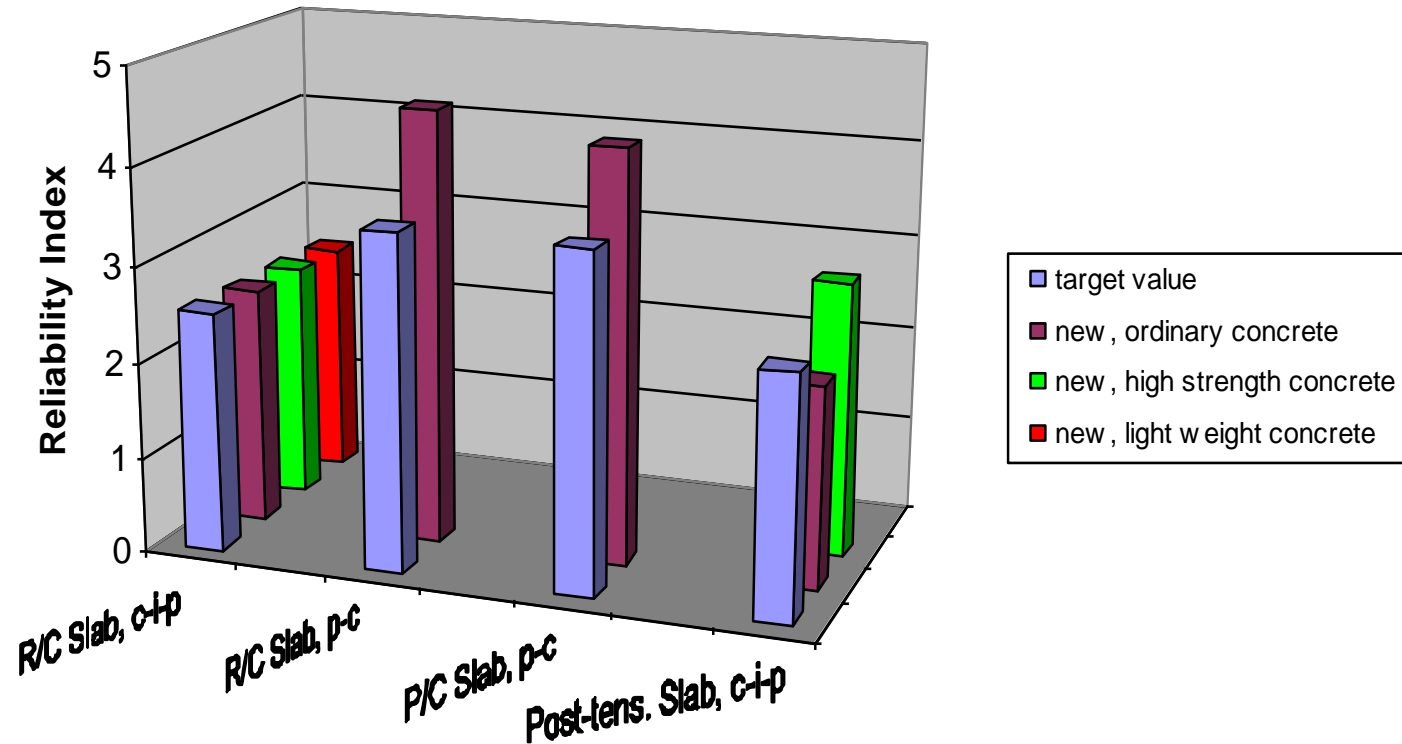
Reliability Indices for Beams, designed according to the “new” ACI 318

Reliability Indices for Beams



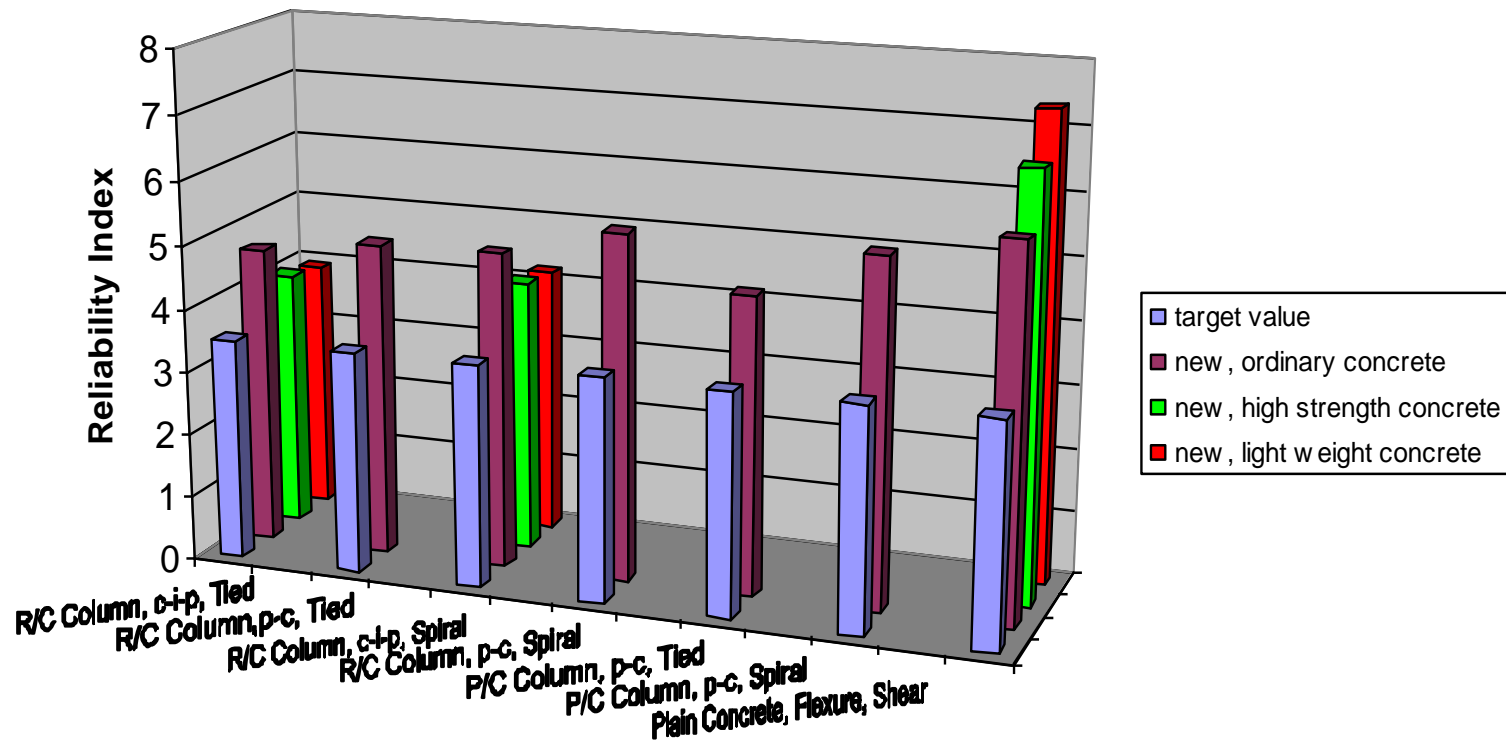
Reliability Indices for Slabs, designed according to the “new” ACI 318

Reliability Indices for Slabs



Reliability Indices for Columns and Plain Concrete Elements, designed according to the "new" ACI 318

Reliability Indices for Columns and Plain Concrete Elements



Load factors specified by ACI 318 and Proposed Design Formula

The design formula specified
by ACI 318-99 Code

$$1.4 D + 1.7 L < \phi R$$

$$0.75 (1.4 D + 1.7 L + 1.7 W) < \phi R$$

$$0.9 D + 1.3 W < \phi R$$

$$0.75 (1.4 D + 1.7 L + 1.87 E) < \phi R$$

Proposed design formula

$$1.4 (D + L) < \phi R$$

$$1.2 D + 1.6 L < \phi R$$

$$1.2 D + 1.6 L + 0.5 S < \phi R$$

$$1.2 D + 0.5 L + 1.6 S < \phi R$$

$$1.2 D + 1.6 W + 0.5 L + 0.5 S < \phi R$$

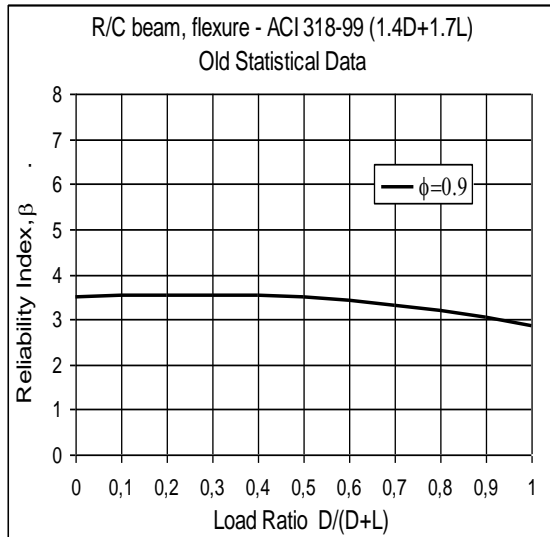
$$1.2 D + 1.0 E + 0.5 L + 0.2 S < \phi R$$

$$0.9 D - (1.6 W \text{ or } 1.0 E) < \phi R$$

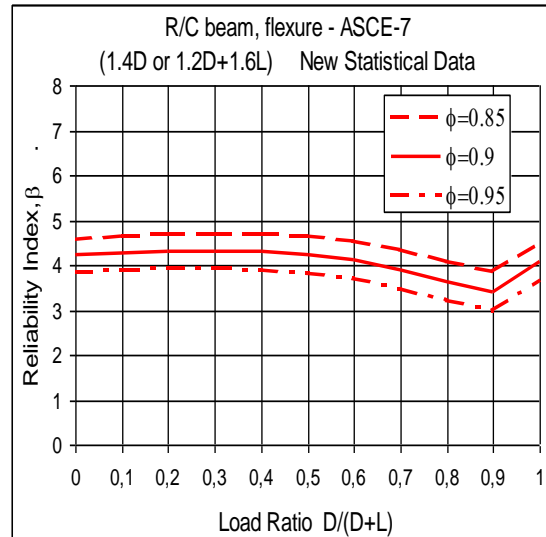


Examples of the Reliability Analysis

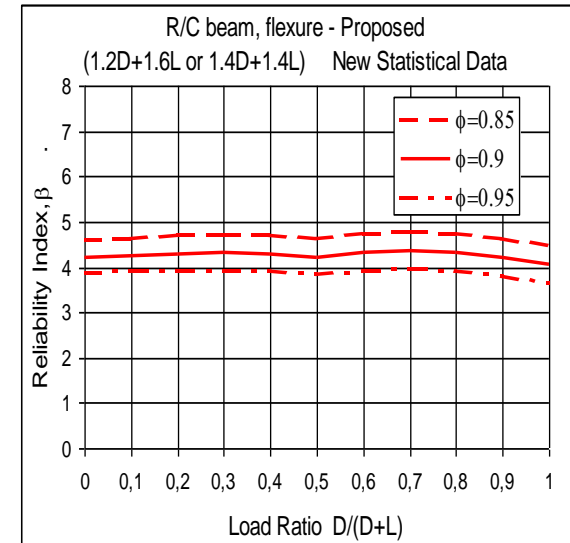
ACI 318-99
Old Statistical Data



ACI 318-05
New Statistical Data



ACI 318-05 with
new load factor,
1.4(D+L)



Conclusions for ACI 318 Calibration

- Quality of materials (concrete and reinforcing steel) have improved in the last 20-30 years
- Reliability of structures designed according to “old” ACI 318 is now higher than the minimum acceptable level
- Resistance factors can be increased by 10-15%. Therefore, for the new load factors (ASCE 7), “old” resistance factors are acceptable



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